



# Recent improvements in the understanding of water vapour feedback

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## Outlook

- Background
- Water vapour feedbacks in idealized cases :The “Simpson law”
- Clear-sky water vapour feedbacks in realistic cases
- Implication for the clear-sky lapse-rate feedback
- All sky multi-model results
- Conclusion

# First estimate of the water vapour feedback

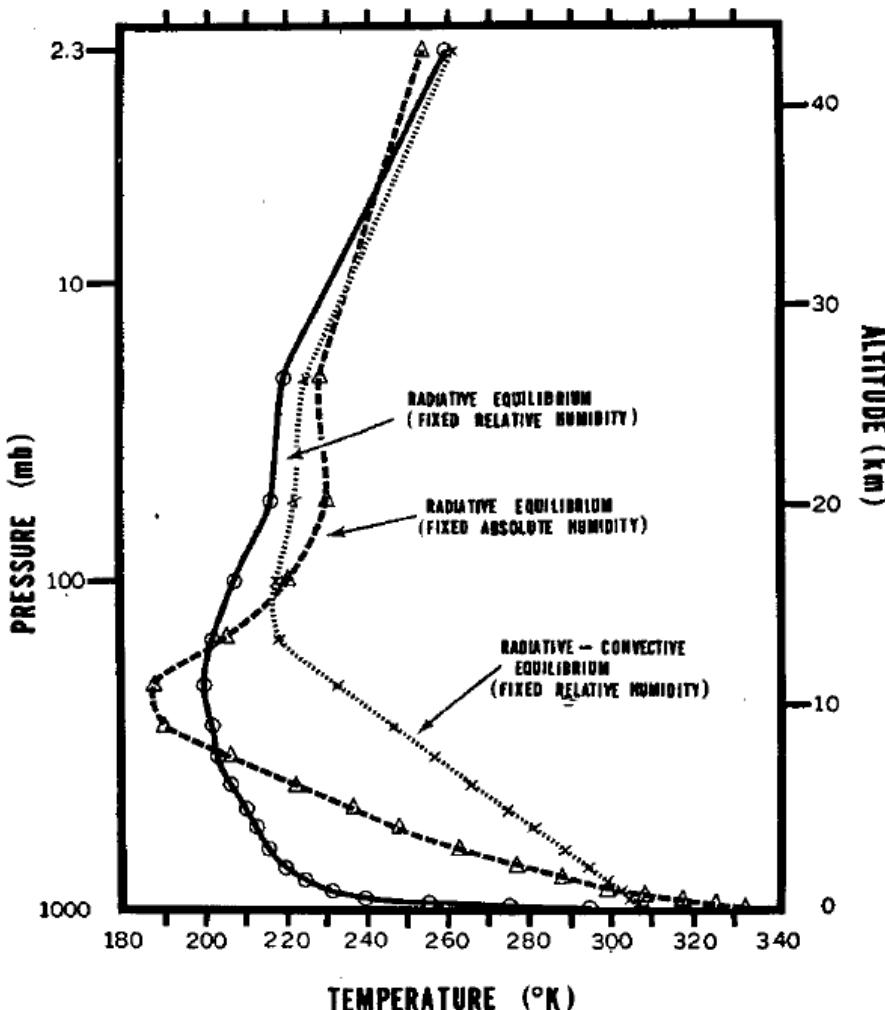


FIG. 5. Solid line, radiative equilibrium of the clear atmosphere with the given distribution of relative humidity; dashed line, radiative equilibrium of the clear atmosphere with the given distribution of absolute humidity; dotted line, radiative convective equilibrium of the atmosphere with the given distribution of relative humidity.

[Manabe & Wetherald, 1967]

TABLE 4. Equilibrium temperature of the earth's surface ( $^{\circ}\text{K}$ ) and the  $\text{CO}_2$  content of the atmosphere.

$\text{CO}_2$ content (ppm)	Average cloudiness		Clear	
	Fixed absolute humidity	Fixed relative humidity	Fixed absolute humidity	Fixed relative humidity
150	289.80	286.11	298.75	304.40
300	291.05	288.39	300.05	307.20
600	292.38	290.75	301.41	310.12

2) Generally speaking, the sensitivity of the surface equilibrium temperature upon the change of various factors such as solar constant, cloudiness, surface albedo, and  $\text{CO}_2$  content are almost twice as much for the atmosphere with a given distribution of relative humidity as for that with a given distribution of absolute humidity.

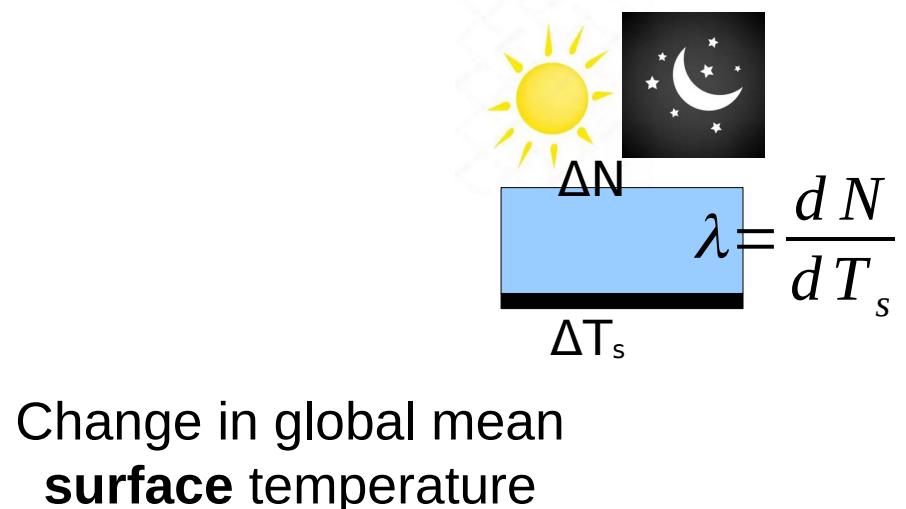
# Radiative forcing-feedback (or response) framework

The **radiative forcing**  $\Delta Q$  is the **change in the net radiative flux** (in  $\text{W.m}^{-2}$ ) at the top of atmosphere due to a change in an external forcing (a driver of climate change) **before surface temperature adjusts** to this perturbation

The “**climate feedback parameter**”  $\lambda$  is the **sensitivity of the net radiative flux** at the top of atmosphere **to a change in the global mean surface temperature  $T_s$**  (in  $\text{W.m}^{-2}.\text{K}^{-1}$ )

$$\Delta N = \Delta Q + \lambda \Delta T_s$$

Change in net flux at the TOA      radiative forcing      “climate feedback parameter”



⚠ Here  $\lambda < 0$ . The opposite sign convention is also used ⚠

The global mean surface temperature change at equilibrium:  $\Delta T_s^e = -\frac{\Delta Q}{\lambda}$

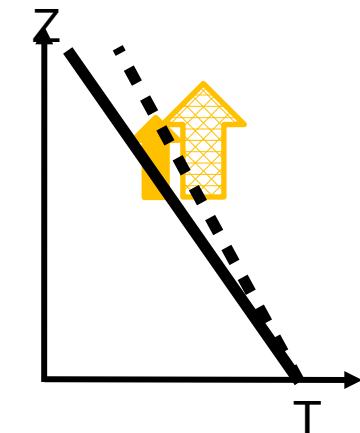
# Climate feedbacks

*Classical decomposition (specific humidity)*

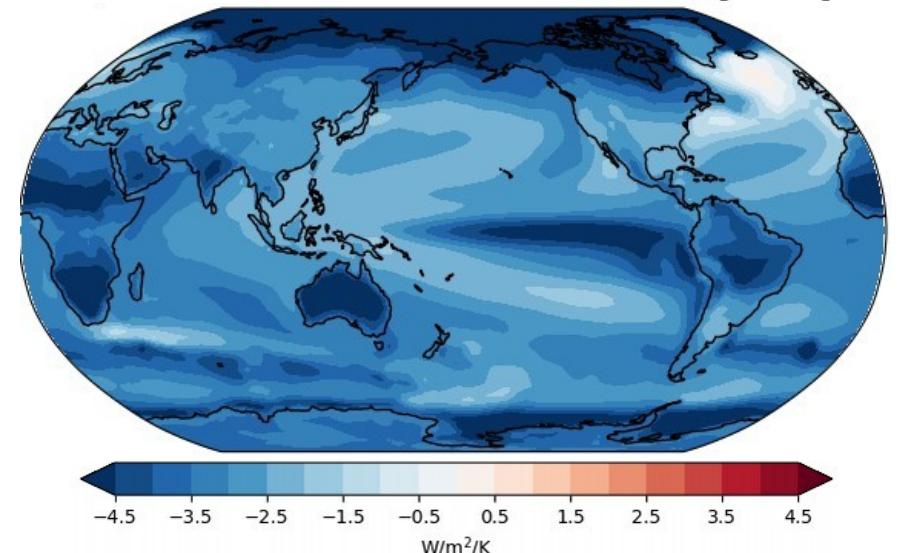
$$\lambda = \lambda_T + \lambda_W + \lambda_C + \lambda_\alpha$$

temperature      water vapor      clouds      surface albedo

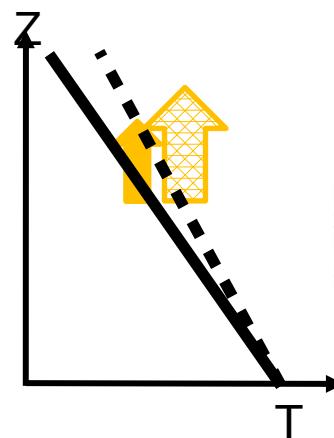
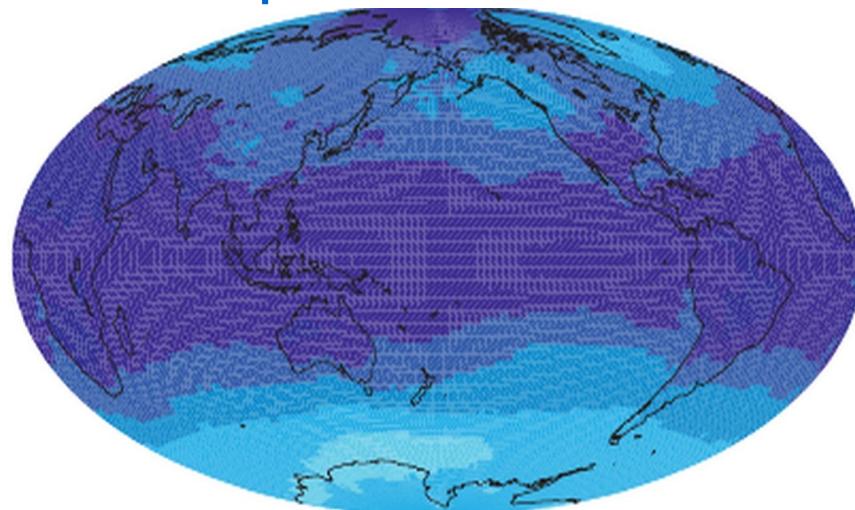
Uniform vertical temperature change  $\leftarrow \overbrace{\lambda_P + \lambda_L}^{\text{Planck}} \rightarrow$  Departure from uniform vertical temperature change



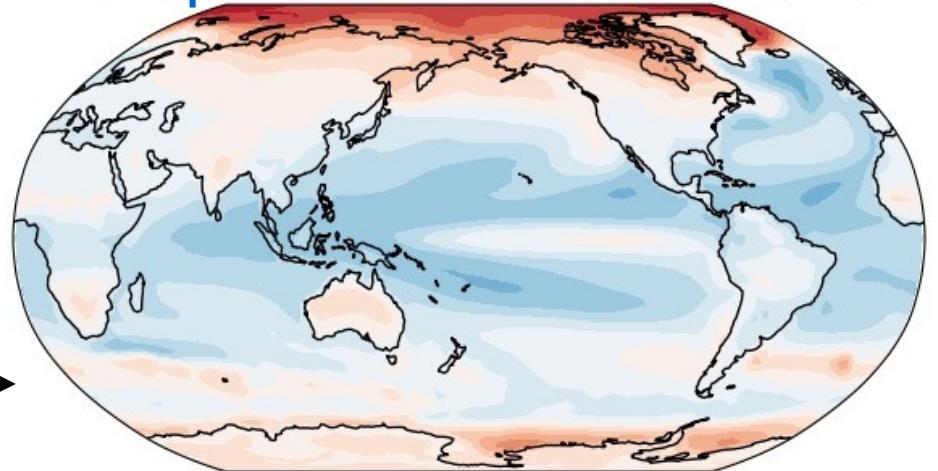
## Planck feedback (uniform temp change) [-3.28]



## Temperature feedback



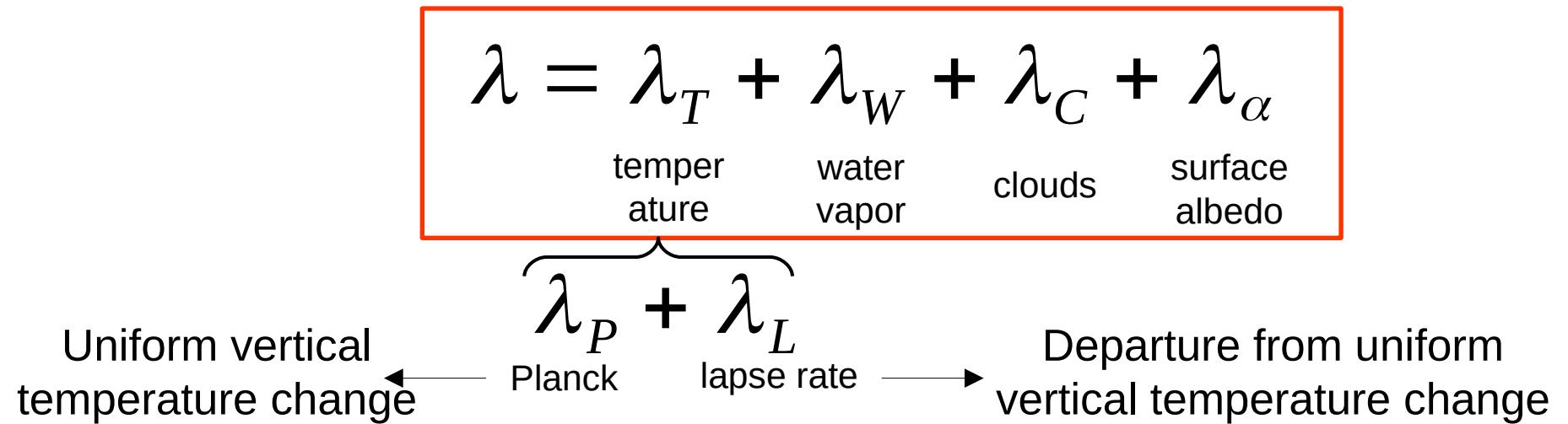
## Lapse-rate feedback [-0.5]



[courtesy of M. Zelinka 2021]  
(<https://doi.org/10.5281/zenodo.5206851>)

# Climate feedbacks

## *Classical* decomposition (*specific humidity*)

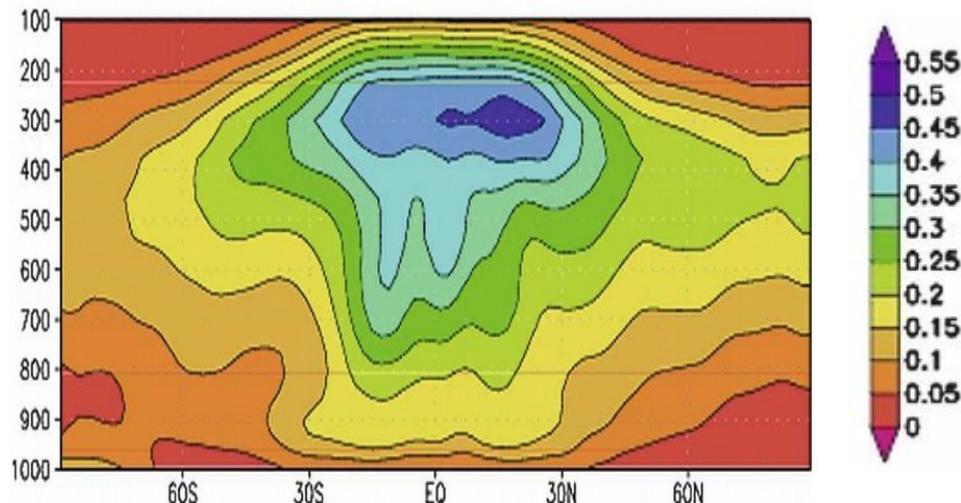


$$\lambda = \frac{dN}{dT_s} = \sum_x \frac{\partial N}{\partial x} \frac{\partial x}{\partial T_s}$$

radiative kernel computed by radiative codes      response to surface temperature change

The equation  $\lambda = \frac{dN}{dT_s} = \sum_x \frac{\partial N}{\partial x} \frac{\partial x}{\partial T_s}$  represents the radiative kernel method for calculating feedback. It shows that the total feedback is the sum of the products of the radiative kernel (partial N/partial x) and the response of each climate variable (partial x/partial T<sub>s</sub>). Blue annotations explain the first part as the "radiative kernel computed by radiative codes" and the second part as the "response to surface temperature change".

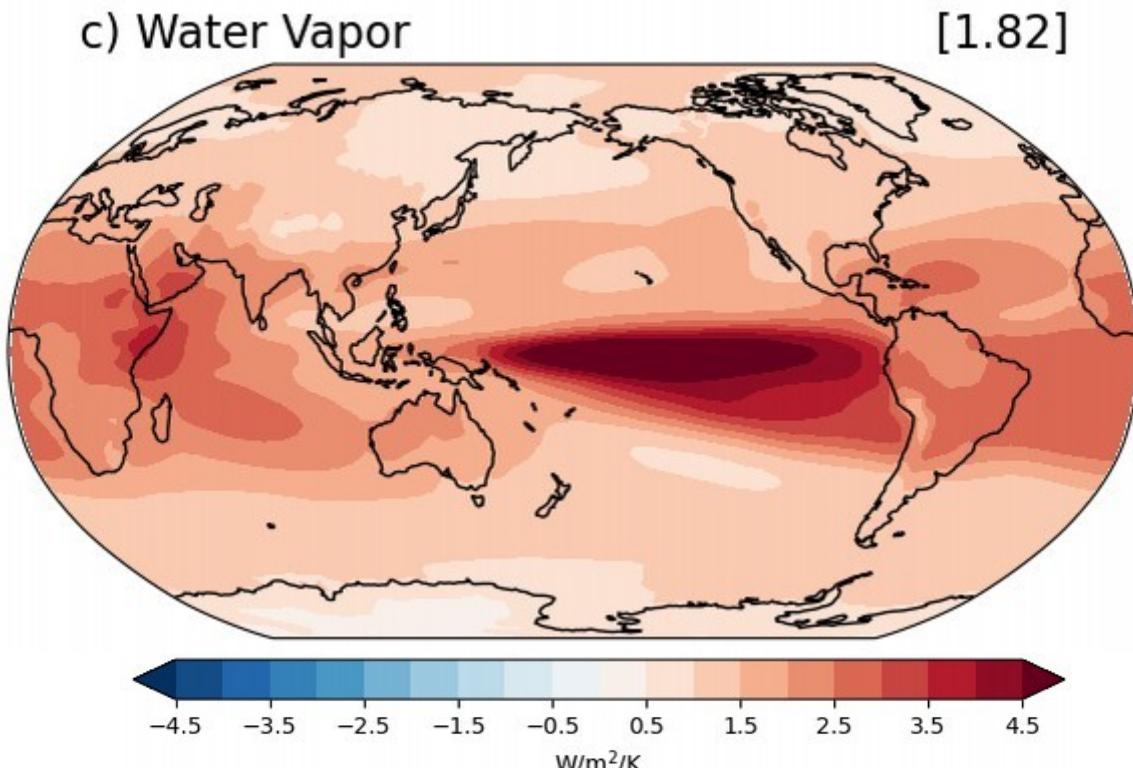
# Water vapour feedback



$$\frac{\partial R}{\partial Q_a(P)} \frac{dQ_a(P)}{dT_s}$$

W/m<sup>2</sup>/K/(100hPa)

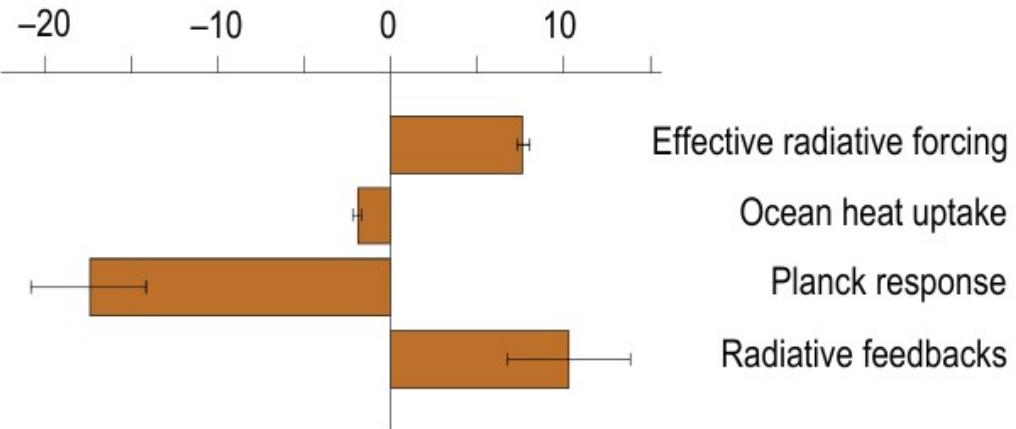
*Soden et al., J. Climate, 2008*



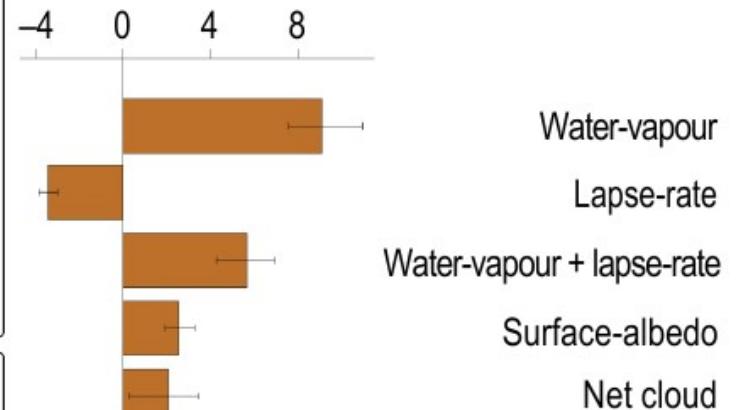
[courtesy of M. Zelinka 2021]

# How much individual feedbacks contribute to global warming (year 100 after abrupt 4xCO<sub>2</sub>)

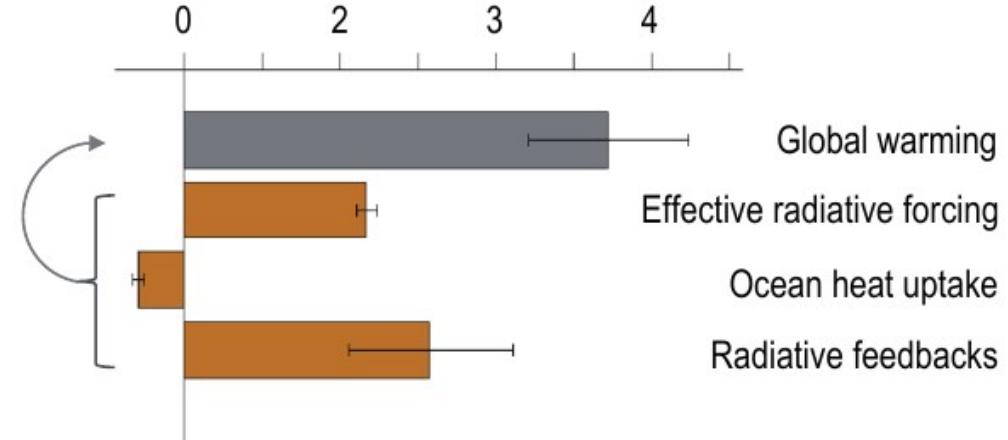
(a) Global atmospheric energy inputs (W m<sup>-2</sup>)



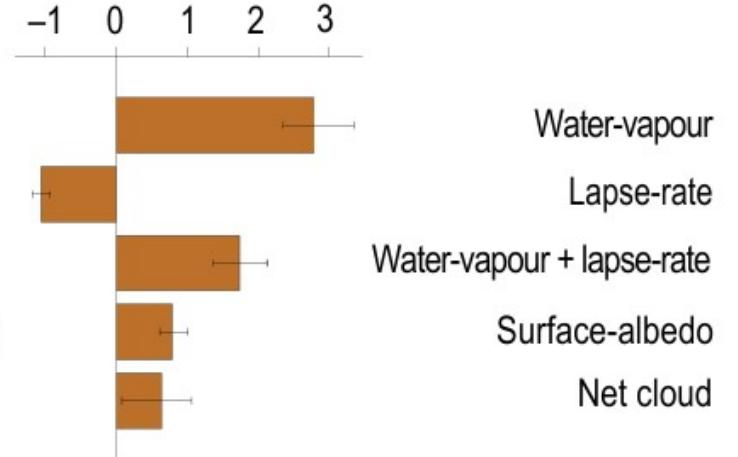
Global energy inputs from individual radiative feedbacks (W m<sup>-2</sup>)



(b) Global warming contributions (°C)



Global warming contributions from individual radiative feedbacks (°C)



# Emission height and emission temperature

Flux TOA has been emitted by:


$$F = \Gamma_s B_s + \int_0^H \frac{\partial \Gamma(z)}{\partial z} B(z) dz$$

where **B** is the **Planck** function,  $\Gamma_s \equiv \Gamma(0)$  and  $\Gamma(z)$  is the hemispherical **transmission function** between altitude  $z$  and the TOA:

$$\Gamma(z) = 2 \int_0^1 \exp(-\tau(z, \mu)) \mu d\mu$$

$\tau(z, \mu)$  is the optical thickness between the TOA and altitude  $z$ .

# Emission height and emission temperature

Flux TOA has been emitted by:


$$F = \Gamma_s B_s + \int_0^H \frac{\partial \Gamma(z)}{\partial z} B(z) dz$$

May be rewritten as:

$$F = \Gamma_s B_s + (1 - \Gamma_s) B_e$$

$$B_e = \int_0^H B(z) \omega(z) dz$$

$$\omega(z) = \frac{1}{1 - \Gamma_s} \frac{\partial \Gamma(z)}{\partial z}$$

# Emission height and emission temperature

Flux TOA has been emitted by:

The diagram shows a downward-pointing arrow labeled "Flux TOA". Above it, a blue bracket labeled "the surface" spans the first few kilometers of the atmosphere. A red bracket labeled "the atmosphere" spans the entire vertical extent from the surface up to the top of the atmosphere.

$$F = \Gamma_s B_s + \int_0^H \frac{\partial \Gamma(z)}{\partial z} B(z) dz$$

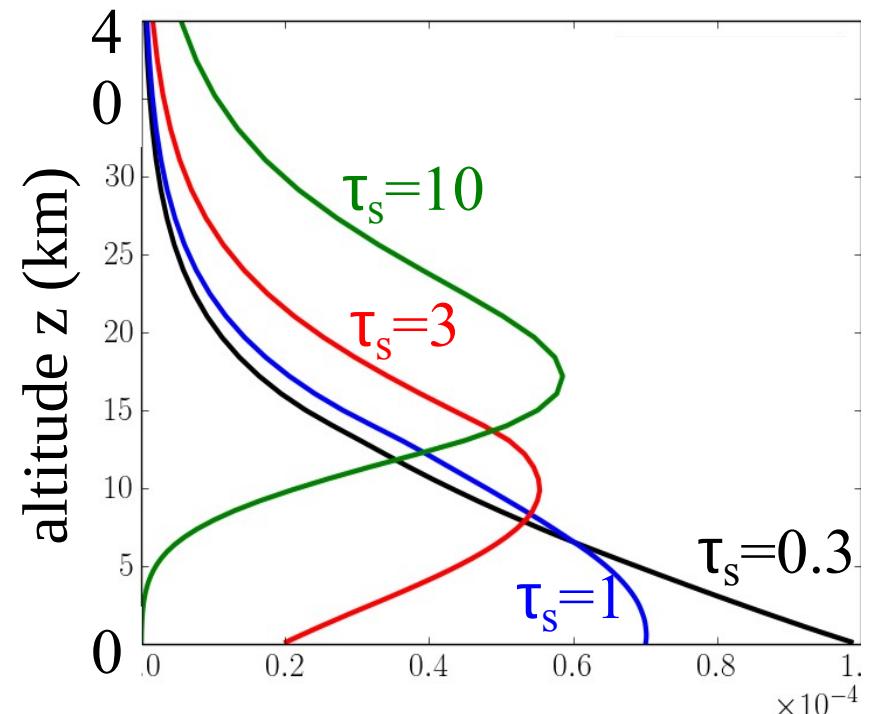
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MLS atmospheric profile with a  
**uniform mass absorption  
coefficient k (m<sup>2</sup>/kg)**



$\omega(z)$  : optical exchange factor between  $z$  and the TOA. Also the **conditional probability that photons emitted at  $z$  reach the TOA**

# Emission height and emission temperature

Flux TOA has been emitted by:

The diagram shows a downward-pointing arrow representing flux TOA. A blue bracket above the arrow is labeled "the surface". A red bracket above the arrow is labeled "the atmosphere".

$$F = \Gamma_s B_s + \int_0^H \frac{\partial \Gamma(z)}{\partial z} B(z) dz$$

May be rewritten as:

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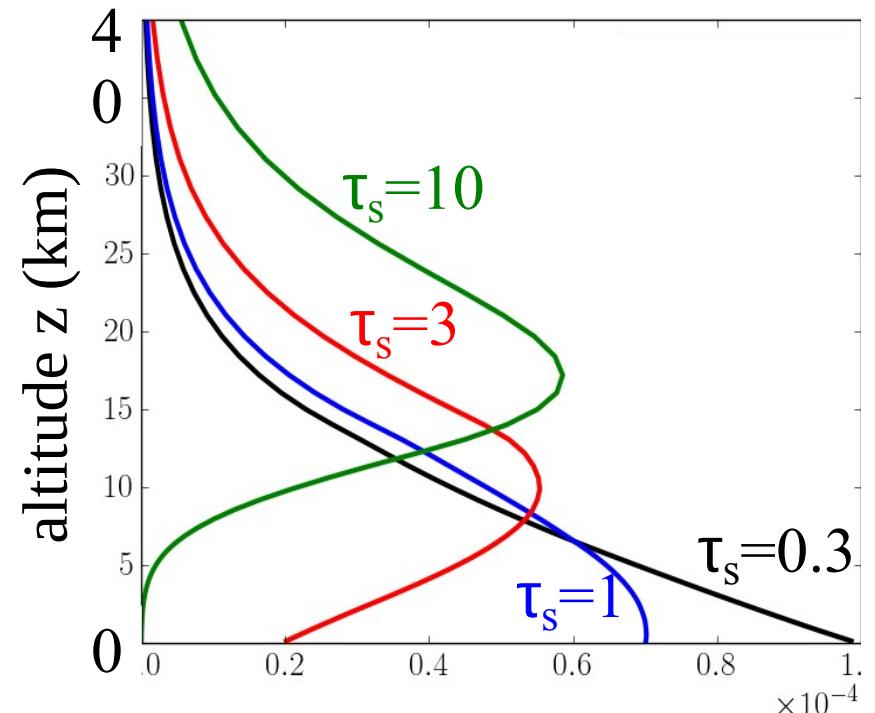
**Emission temperature Te:**  $B(Te) = B_e$

A common approximation:

**Emission height Ze:** altitude where the optical thickness between Ze and the TOA is 1

**Emission temperature Te:** temperature at altitude Ze

MLS atmospheric profile with a  
**uniform mass absorption  
coefficient k** ( $\text{m}^2/\text{kg}$ )

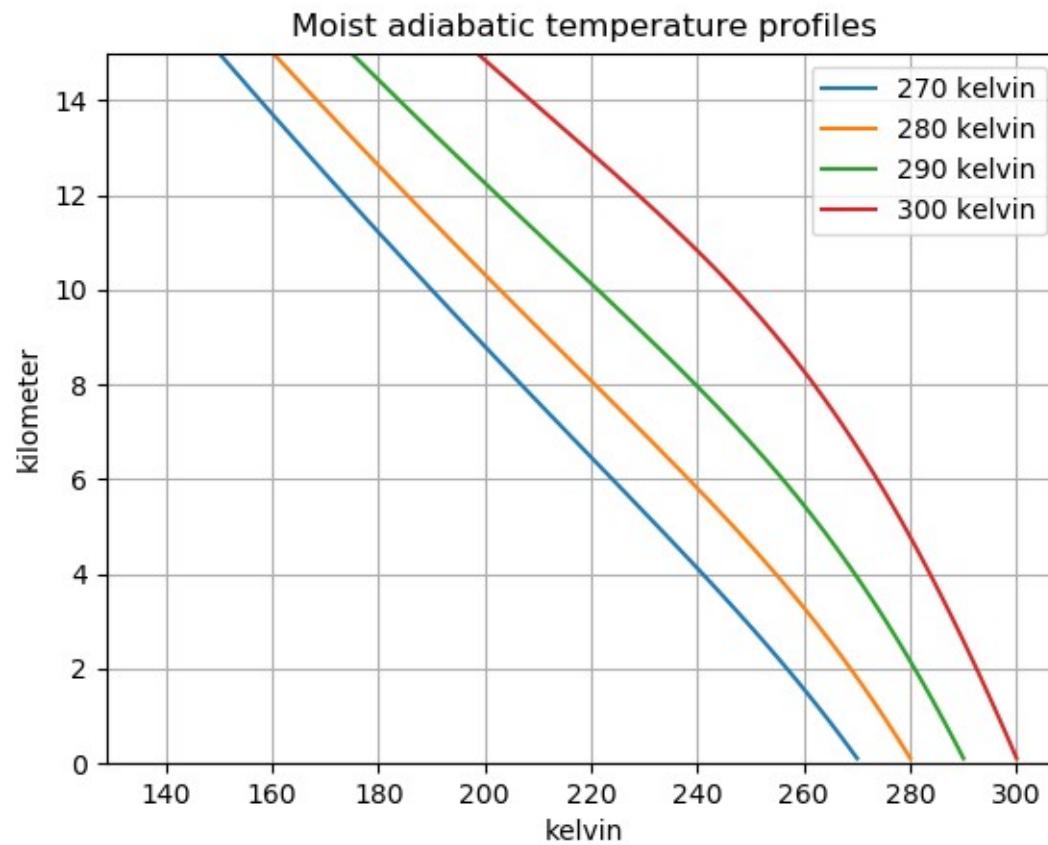


$\omega(z)$  : optical exchange factor between  $z$  and the TOA. Also the **conditional probability that photons emitted at  $z$  reach the TOA**

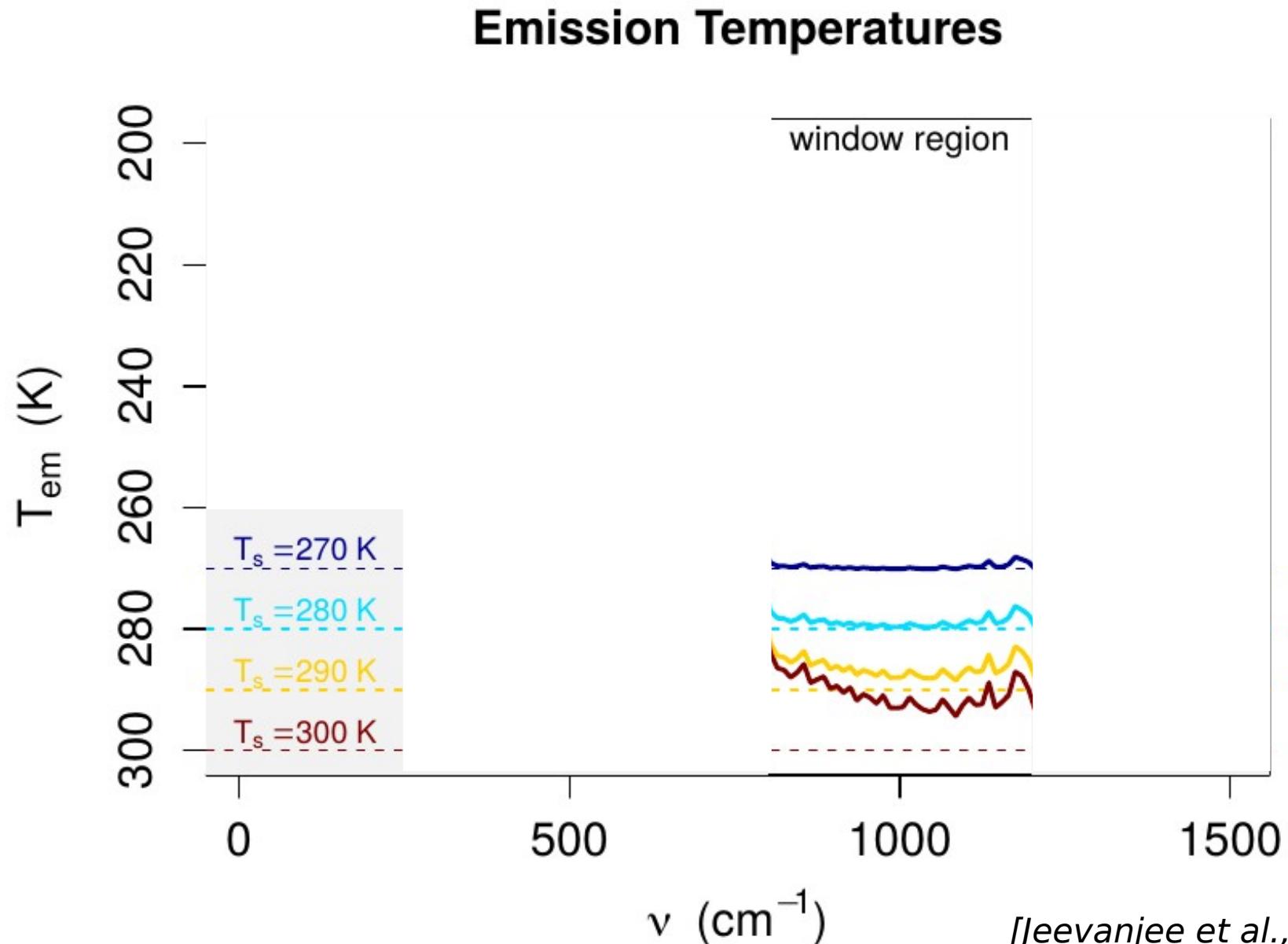
# Outlook

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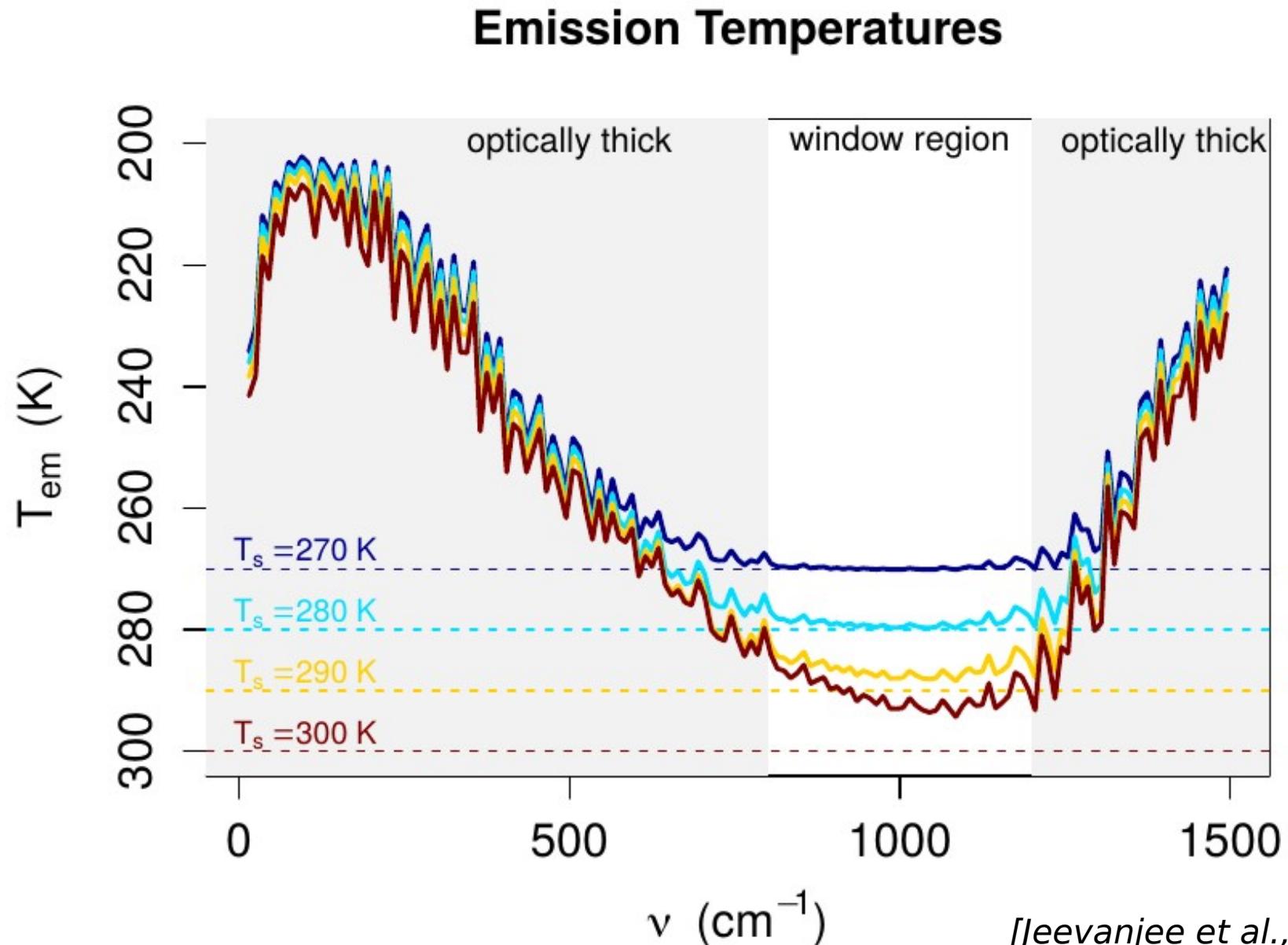
# *Idealized clear sky tropical atmospheres with constant relative humidity*



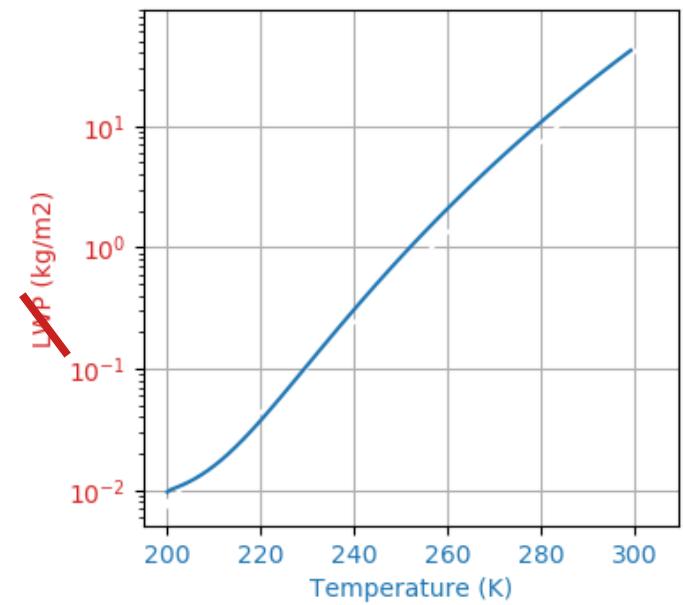
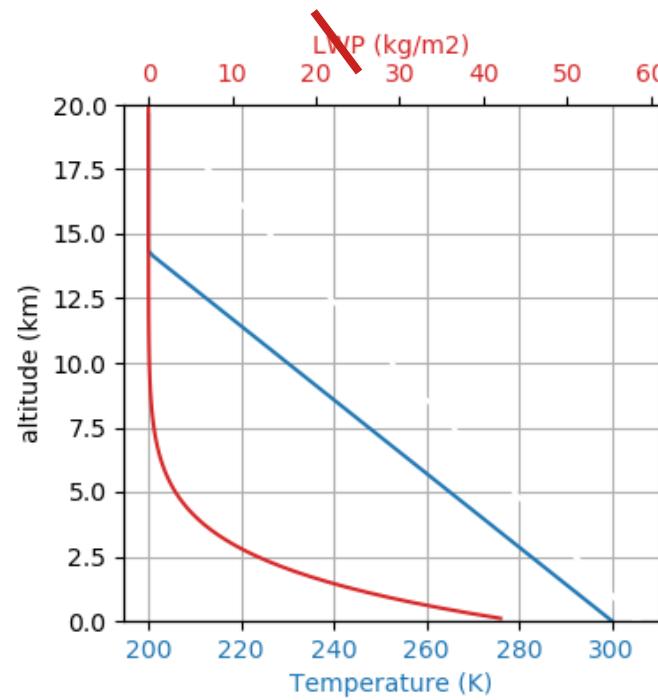
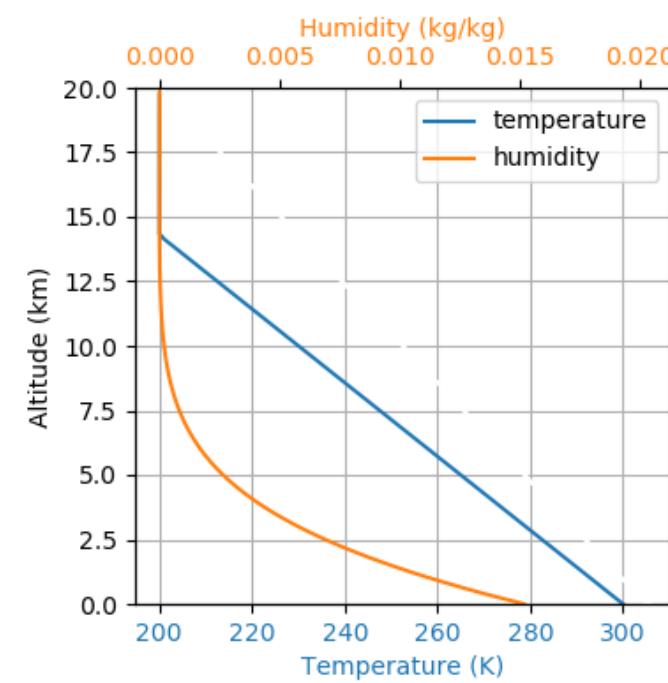
# Idealized clear sky tropical atmospheres with constant relative humidity



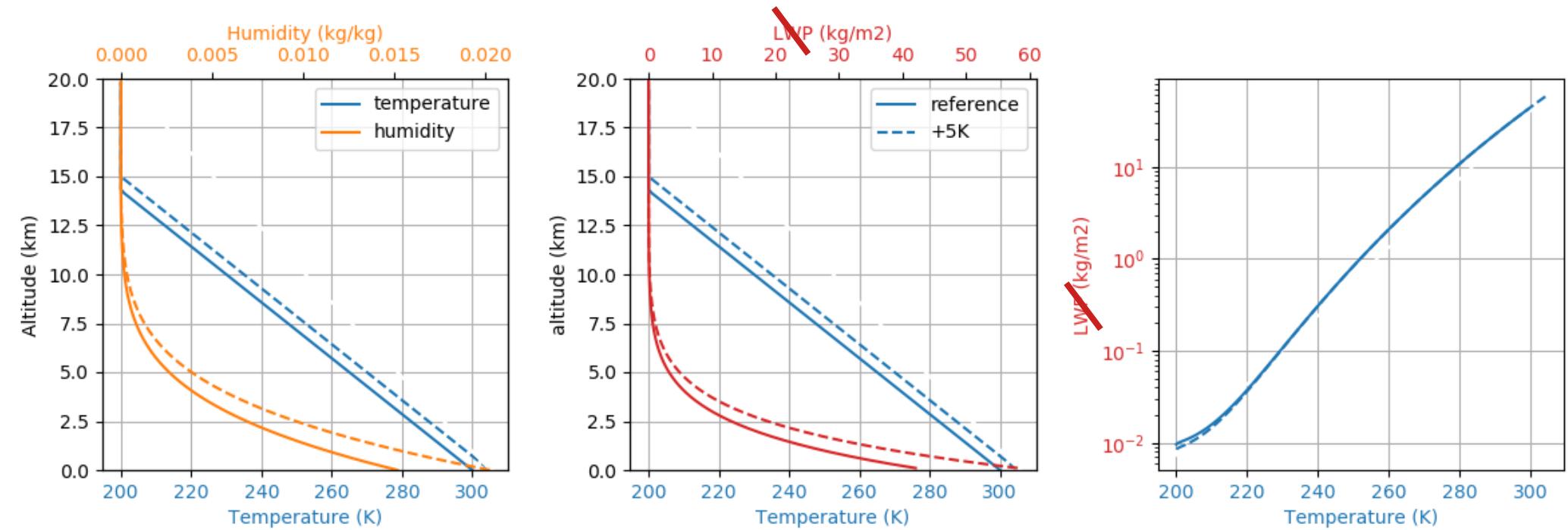
*For idealized clear sky tropical atmospheres  
with **constant relative humidity***



# *Vertical profile of the column integrated amount of water vapour*

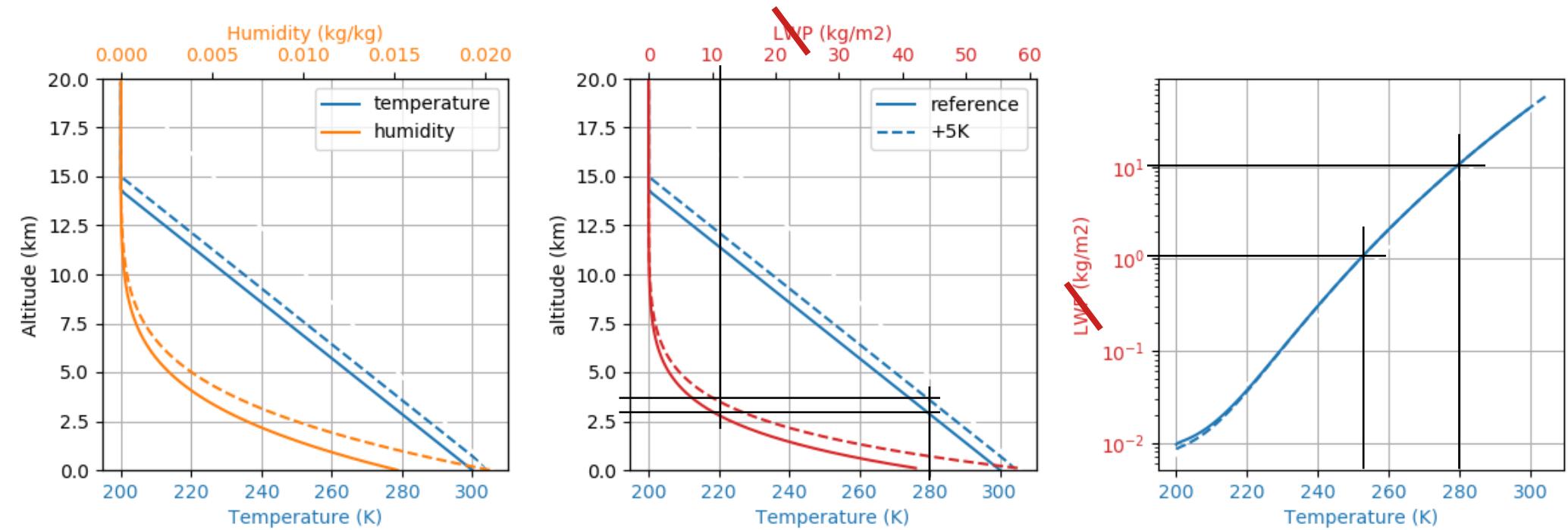


# *Vertical profile of the column integrated amount of water vapour*



If the relative humidity RH is vertically uniform in the troposphere (here 0.7), the **column integrated amount of H<sub>2</sub>O** from the TOA to a given altitude is an increasing function than **only depends on the temperature at that altitude**

# *Vertical profile of the column integrated amount of water vapour*

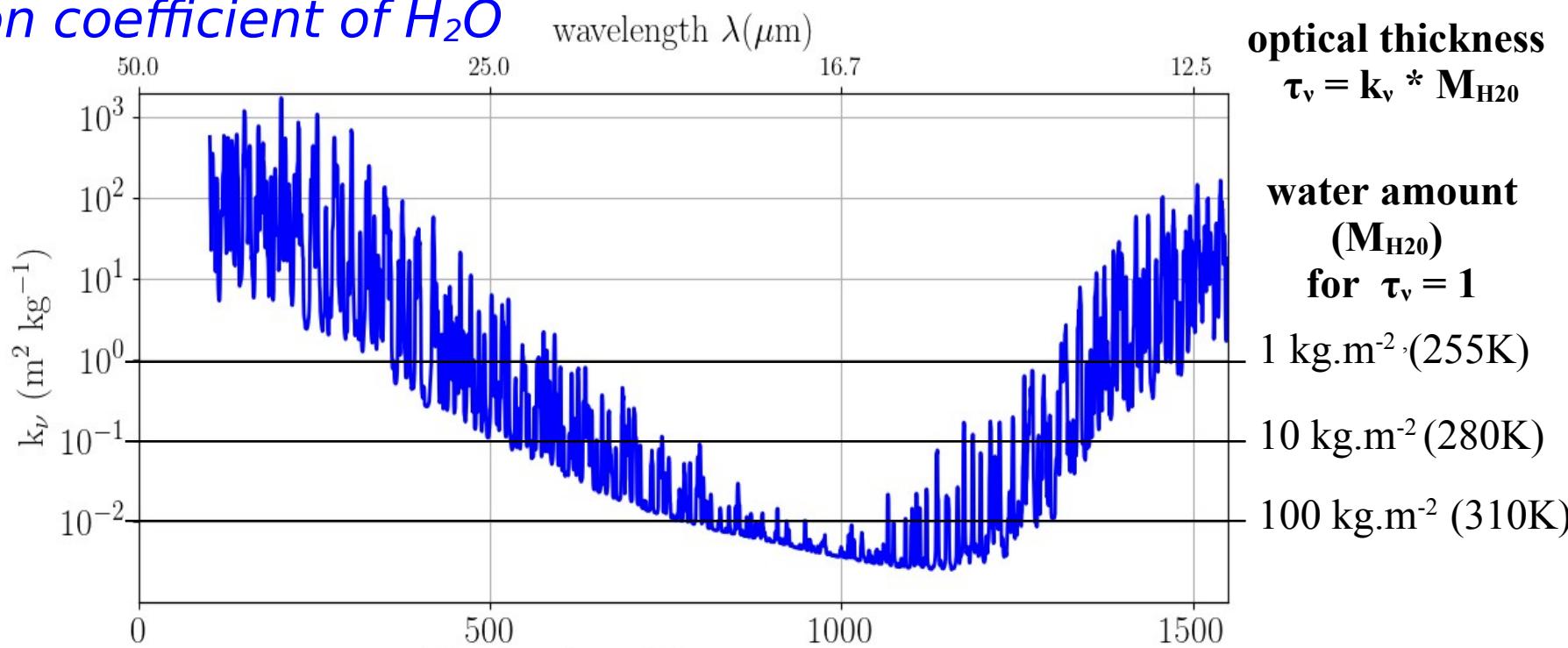


If the relative humidity RH is vertically uniform in the troposphere (here 0.7), the column integrated amount of H<sub>2</sub>O from the TOA to a given altitude is an increasing function than only depends on the temperature at that altitude

$$T = 255K \Rightarrow LWP = 1 \text{ kg.m}^{-2}$$

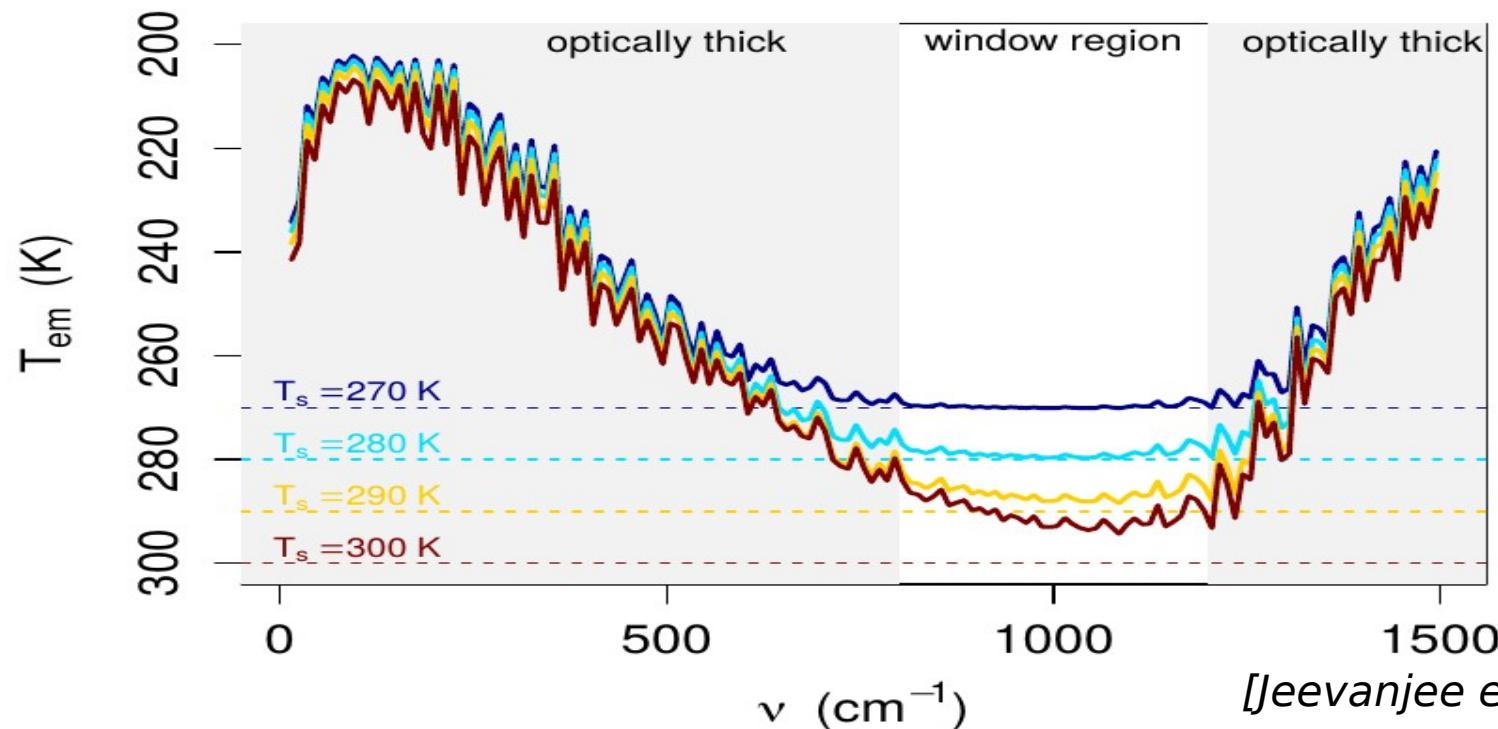
$$T = 280K \Rightarrow LWP = 10 \text{ kg.m}^{-2}$$

# Absorption coefficient of $H_2O$



Emission temperature

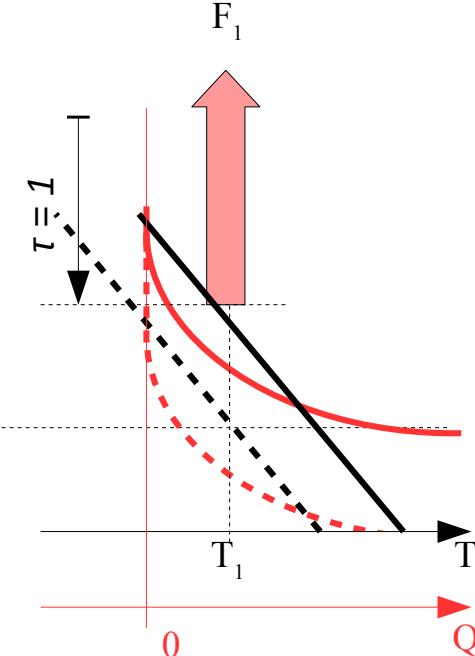
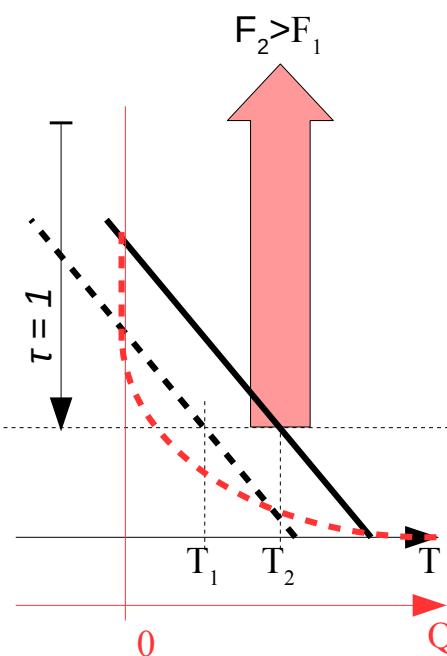
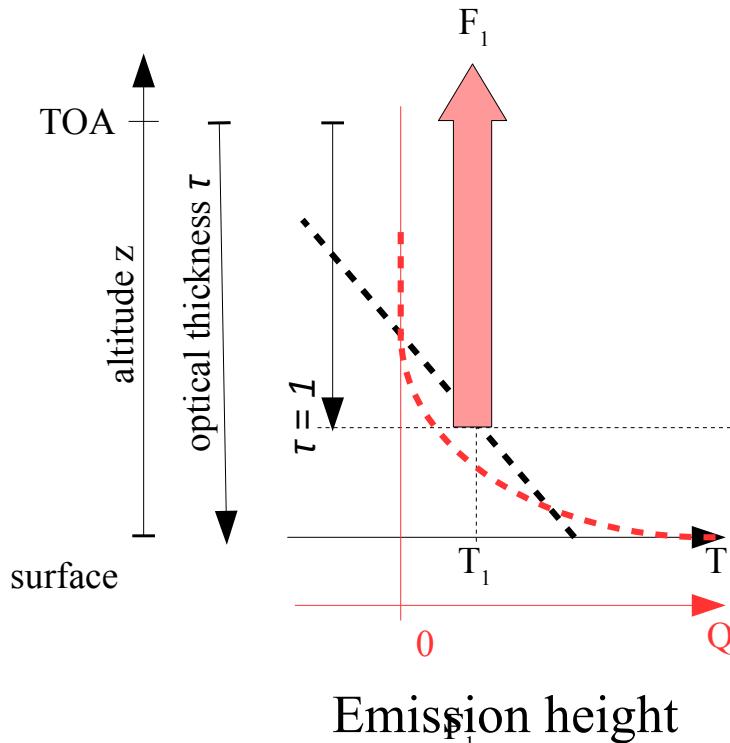
Emission Temperatures



# Simpson's law

[Simpson 1928, Ingram W. 2010, Jeevanjee et al. 2021]

In spectral regions where gases are highly absorbent of an atmosphere whose properties vary continuously and smoothly with altitude and pressure...



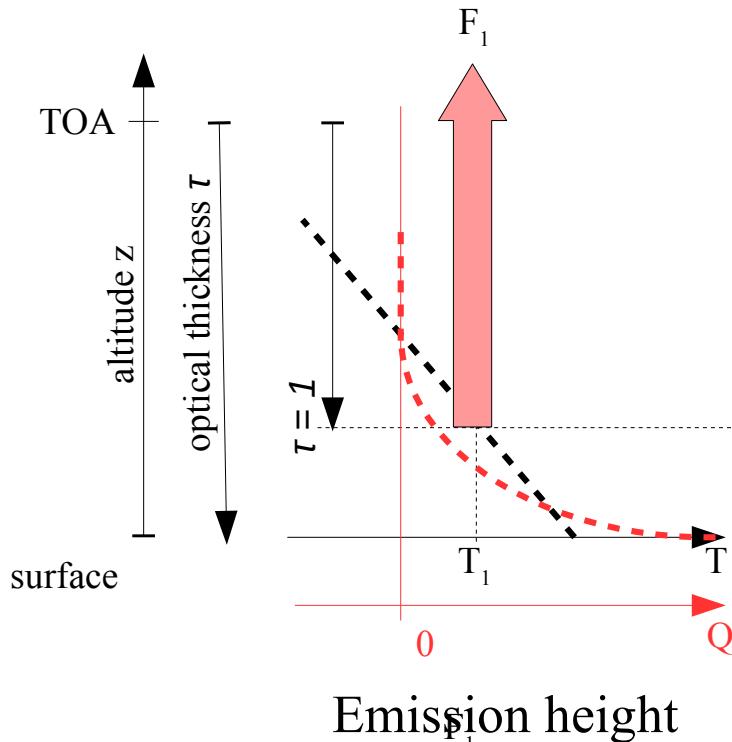
=> *the emission temperature (the flux emitted) does not change with a uniform increase in temperature if the relative humidity remains const*

=> *If these conditions are met over the entire infrared domain, the feedback is infinite, we have a runaway effect*

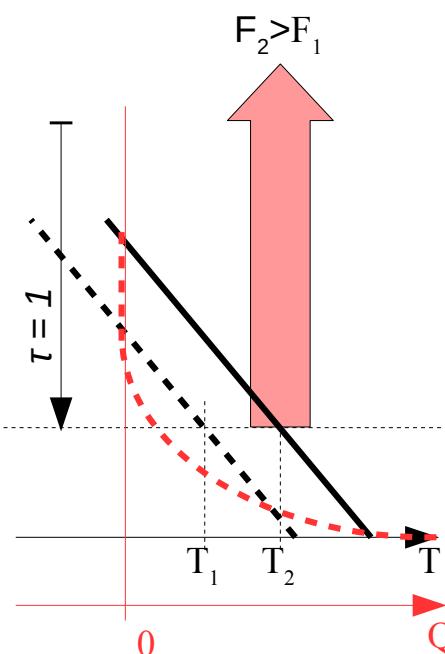
# Simpson's law

[Simpson 1928, Ingram W. 2010, Jeevanjee et al. 2021]

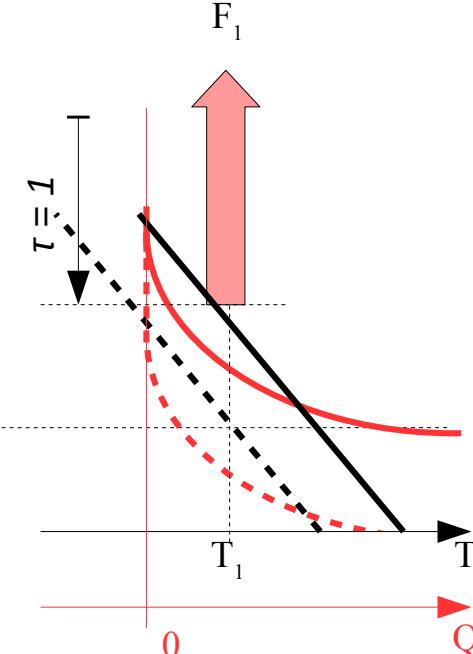
In spectral regions where gases are highly absorbent of an atmosphere whose properties vary continuously and smoothly with altitude and pressure...



Emission height



A warmer atmosphere  
with fixed GHG profile



A warmer atmosphere with  
fixed relative humidity profile

=> *the emission temperature (the flux emitted) does not change with a uniform increase in temperature if the relative humidity remains constant*

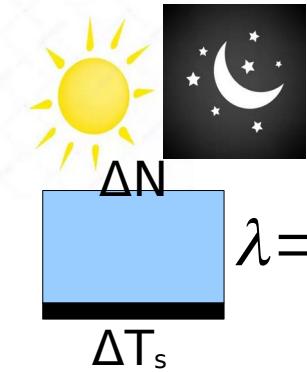
*Key hypothesis:*

- Spectral domain with  $H_2O$  strong absorption, no other GHGs, no clouds
- Relative humidity is vertically uniform, as is the temperature change
- The gas absorption properties do not depend on temperature and pressure

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# Climate feedbacks



## *Classical decomposition (specific humidity)*

$$\lambda = \lambda_P + \lambda_L + \lambda_W + \lambda_C + \lambda_\alpha$$

Planck      lapse      water      clouds      surface  
rate            vapor                vapor            albedo

## *Relative humidity decomposition (Held & Shell, 2012)*

$$\underbrace{\lambda_W}_{\text{water vapor}} = \underbrace{\lambda_{QP} + \lambda_{QL}}_{\text{At constante relative humidity}} + \lambda_R \leftarrow \text{Change in relative himidity}$$

At constante relative humidity, change in humidity du to change, in verically uniform temperature ( $\lambda_{QP}$ ) and lapse rate ( $\lambda_{QL}$ )

$$\lambda = \underbrace{\lambda_P^* + \lambda_L^*}_{\text{Planck lapse rate}} + \lambda_R + \lambda_C + \lambda_\alpha$$

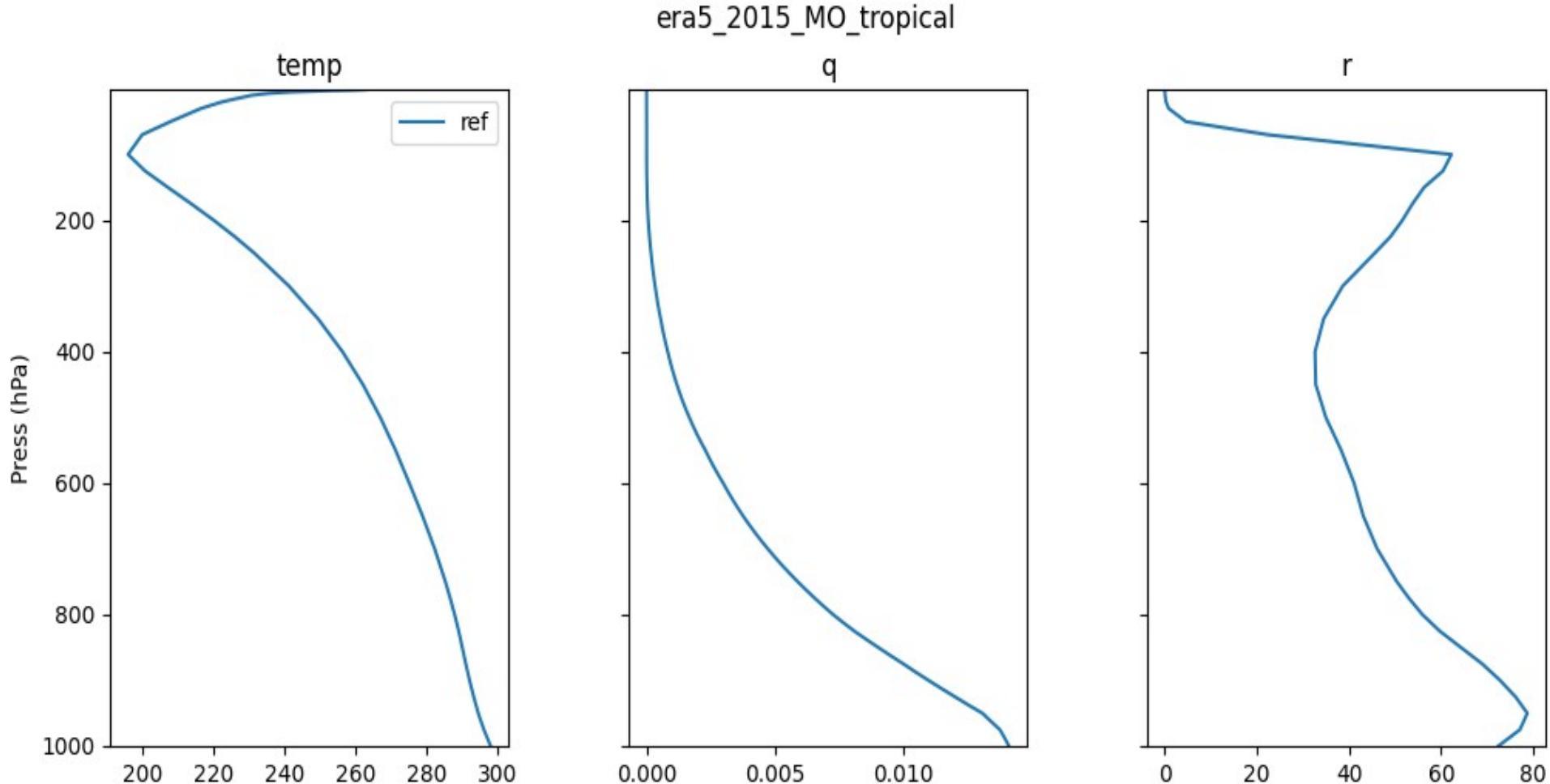
relative      clouds      surface  
humidity            albedo

at constante relative humidity

$$\lambda_P^* = \lambda_P + \lambda_{QP}$$

$$\lambda_L^* \doteq \lambda_L + \lambda_{QL}$$

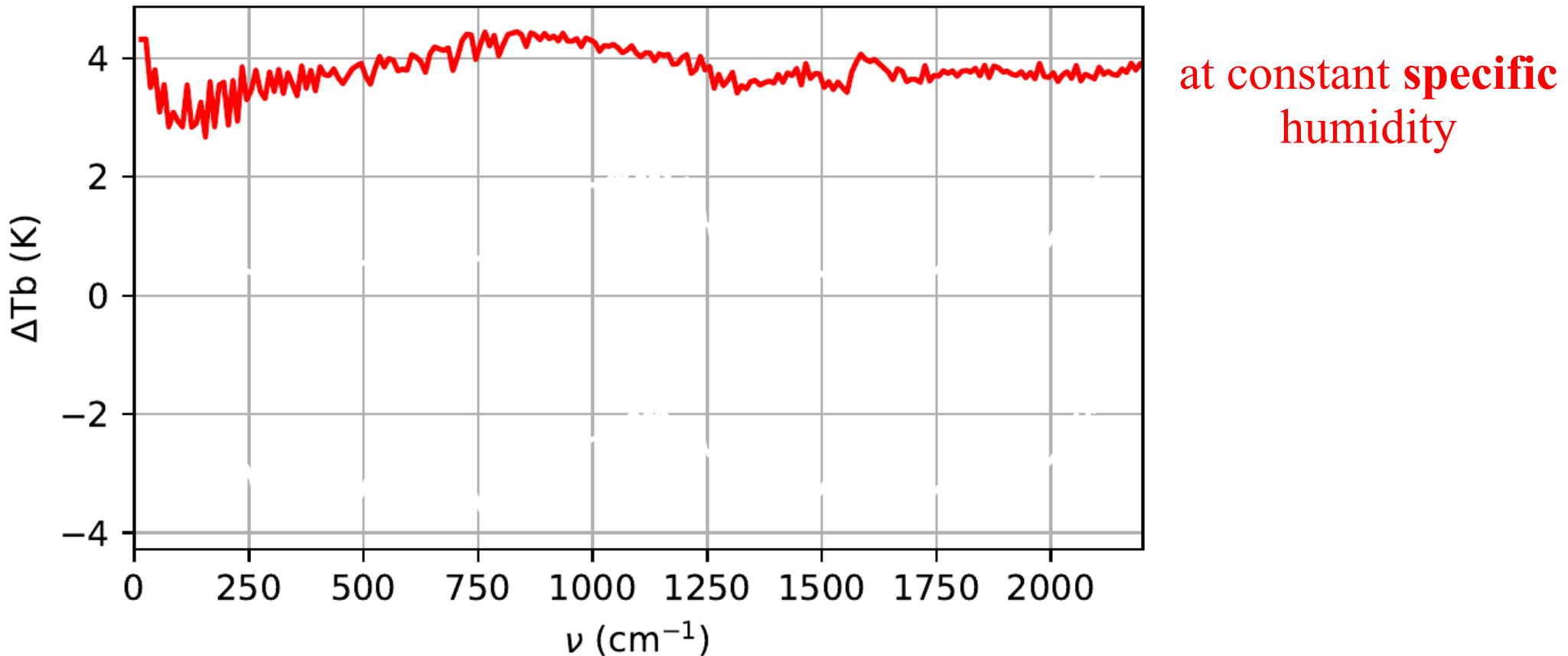
# *For a mean tropical atmosphere (ERA5)*



# *For a mean tropical atmosphere (ERA5)*

Change in brightness temperature  
in response to a vertically **uniform +4K increase of the troposphere**

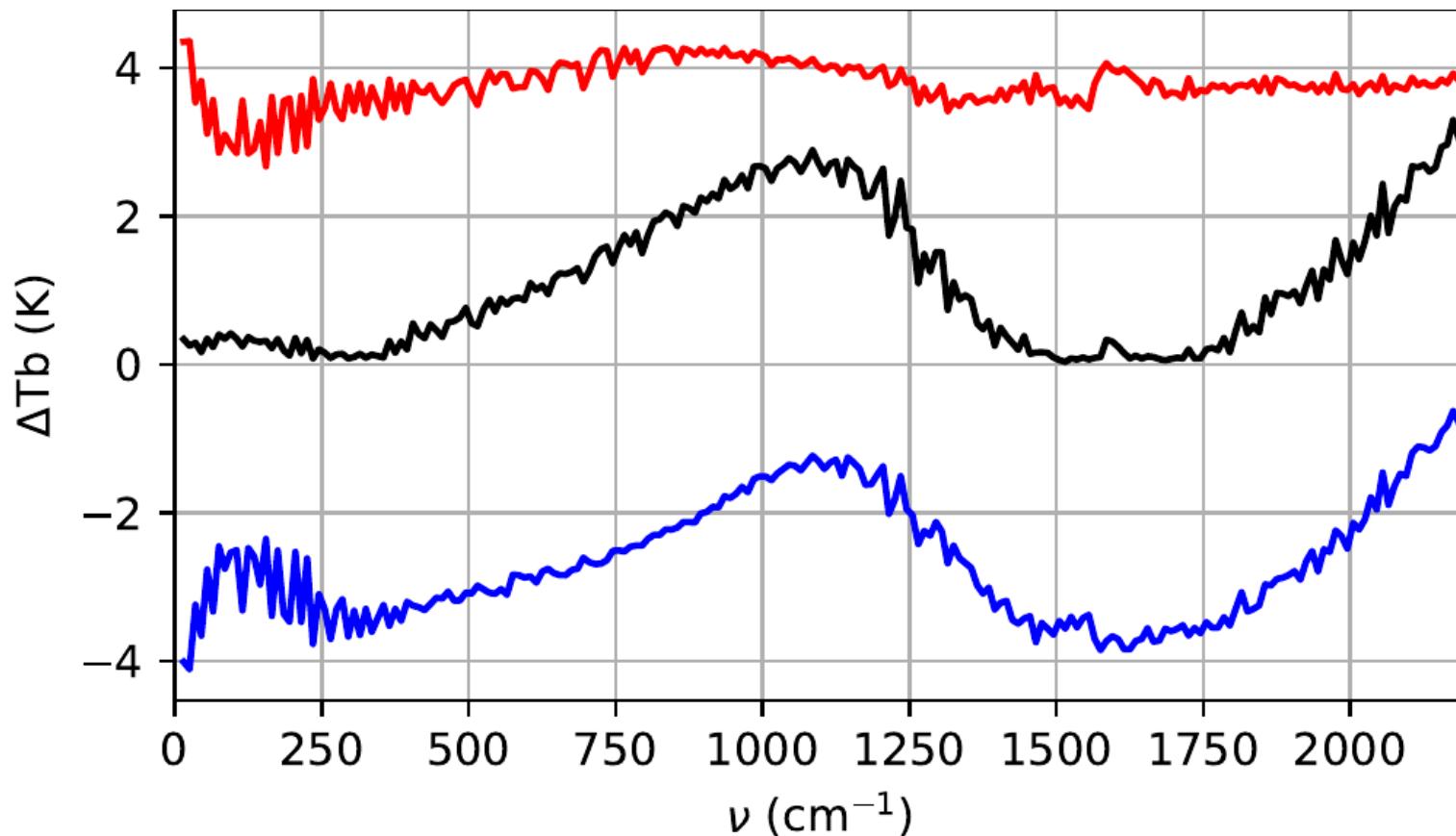
GHG: Only H<sub>2</sub>O



# *For a mean tropical atmosphere (ERA5)*

Change in brightness temperature  
in response to a vertically **uniform +4K increase of the troposphere**

GHG: Only H<sub>2</sub>O



at constant specific  
humidity

at constant relative  
humidity

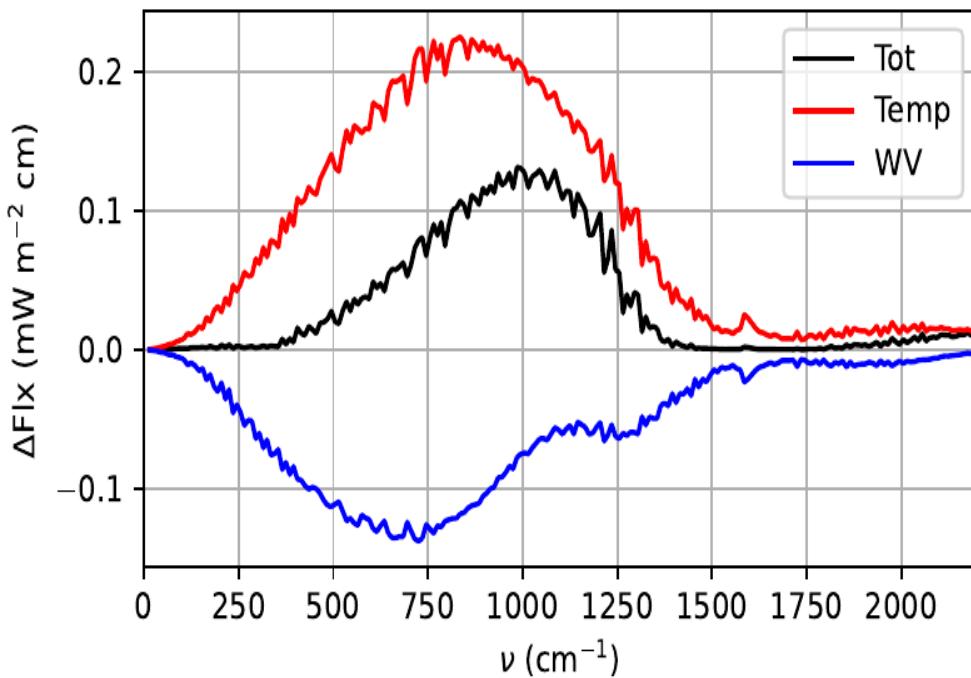
due to change in q to  
keep relative  
humidity constant

# *For a mean tropical atmosphere (ERA5)*

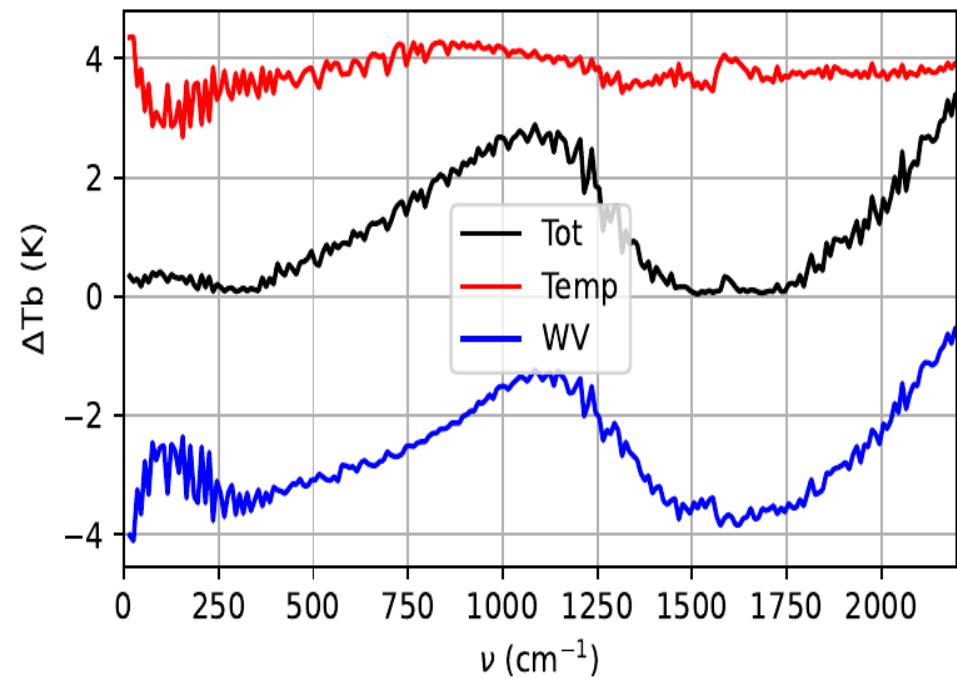
Change in brightness temperature  
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GHG: Only H<sub>2</sub>O

Flux at the TOA



Brightness temperature

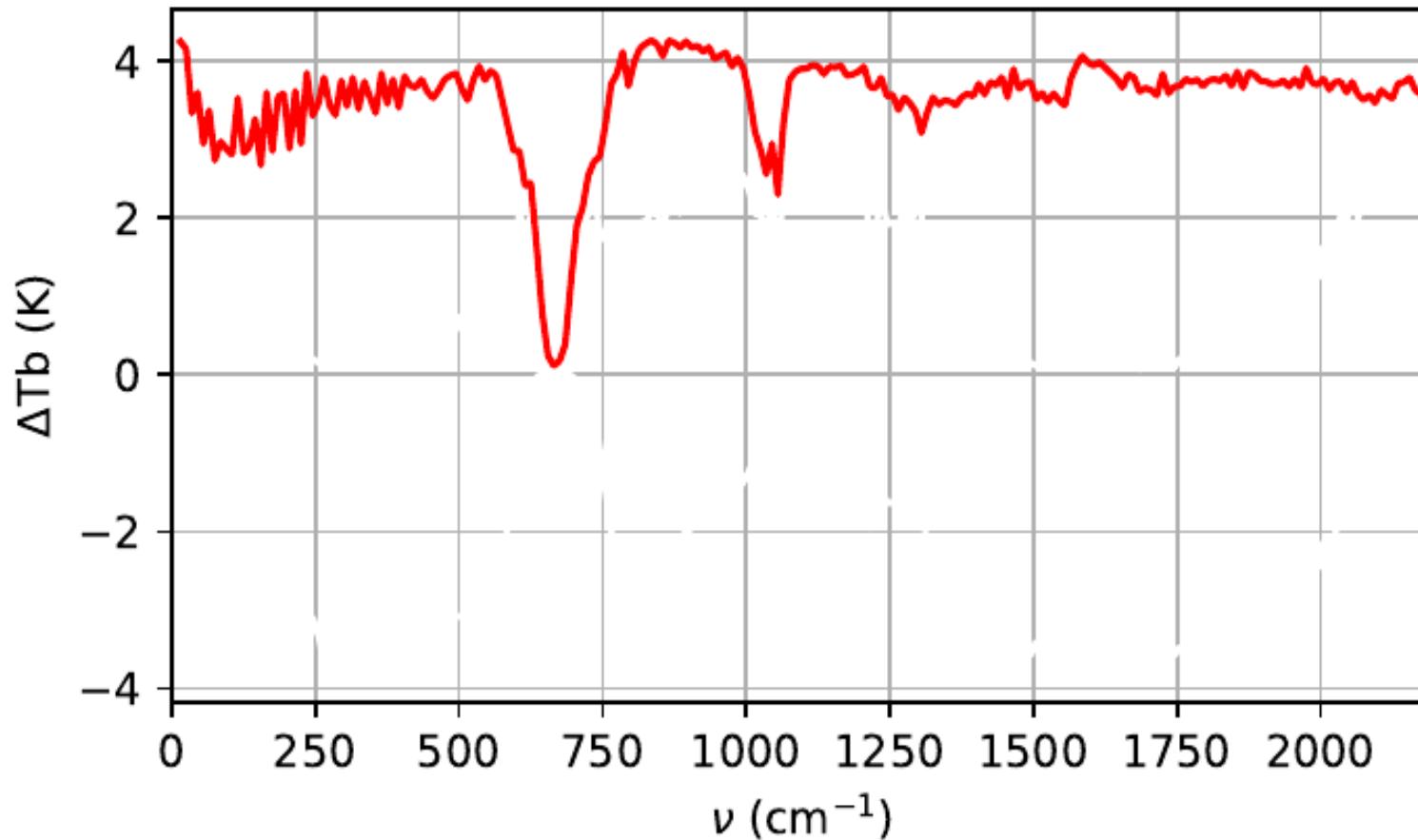


For a mean tropical atmosphere with only H<sub>2</sub>O, the **increase in water vapour to keep the relative humidity constant reduces by 60%** the increase in outgoing radiative flux due to the increase in temperature if the specific humidity would remain constant.

# *For a mean tropical atmosphere (ERA5)*

Change in brightness temperature  
in response to a vertically **uniform +4K increase of the troposphere**

GHG: Only H<sub>2</sub>O + CO<sub>2</sub> + O<sub>3</sub>

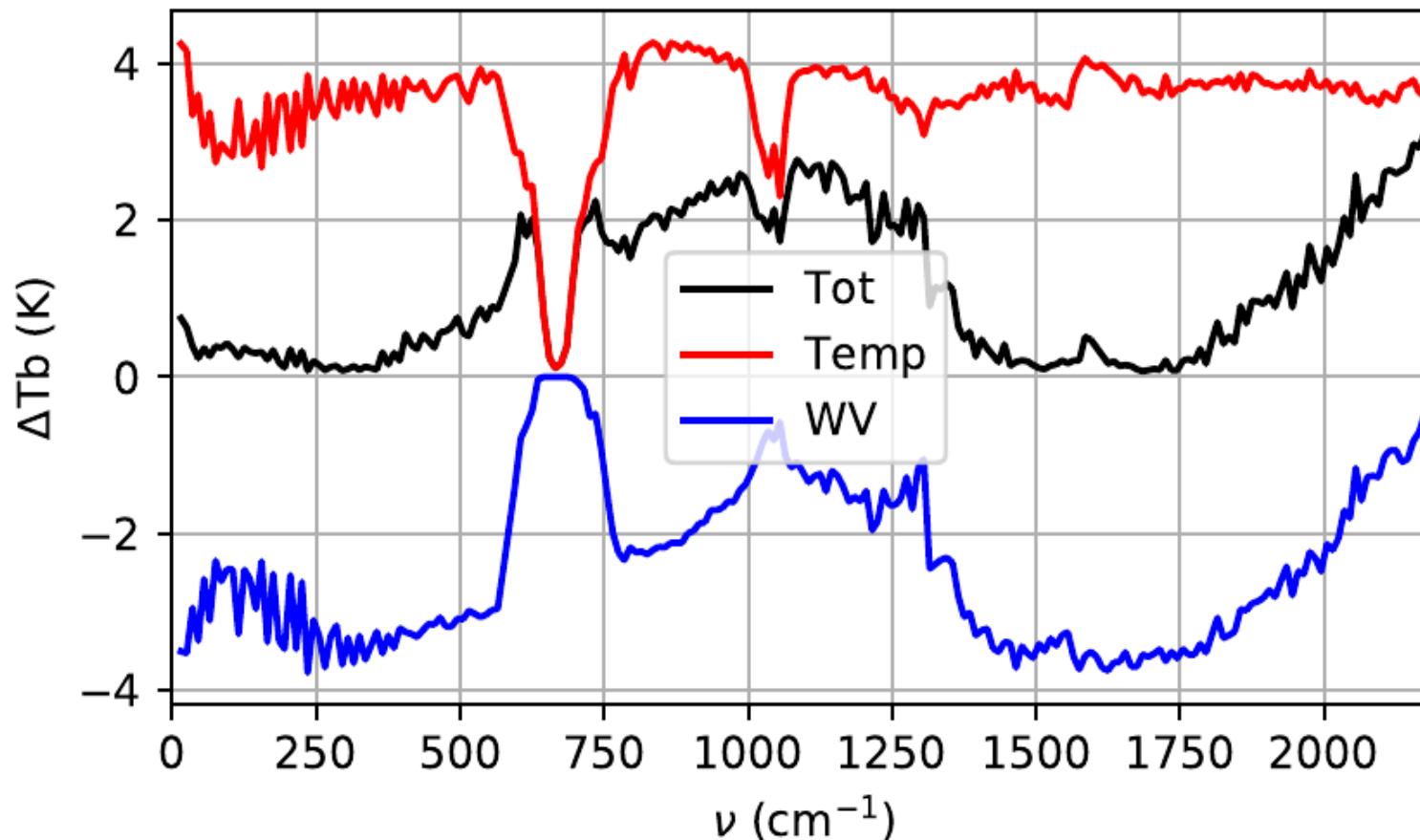


at constant specific  
humidity

# *For a mean tropical atmosphere (ERA5)*

Change in brightness temperature  
in response to a vertically **uniform +4K increase of the troposphere**

GHG: Only H<sub>2</sub>O + CO<sub>2</sub> + O<sub>3</sub>



at constant **specific humidity**

at constant **relative humidity**

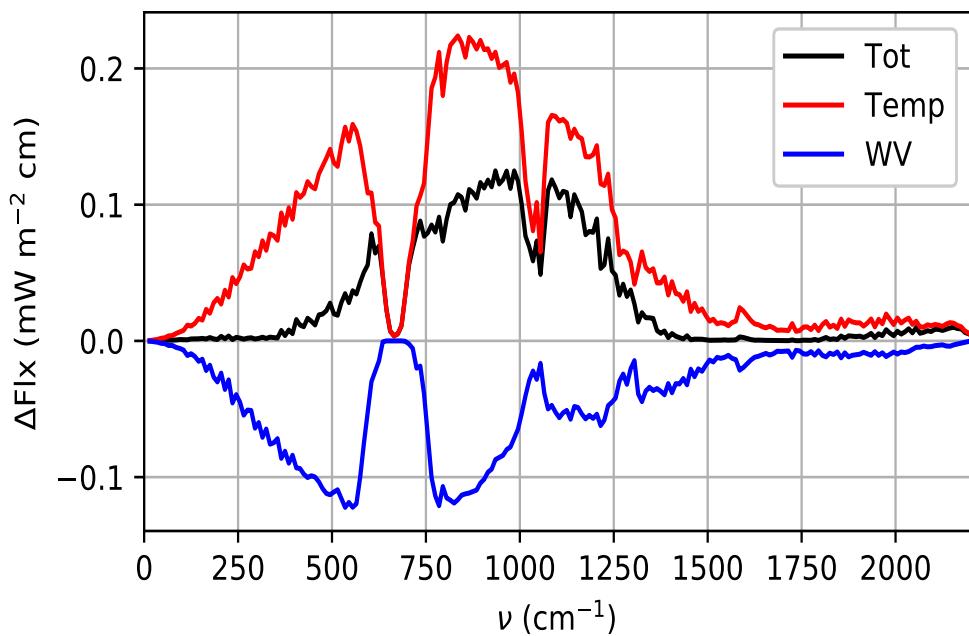
due to change in  $q$  to  
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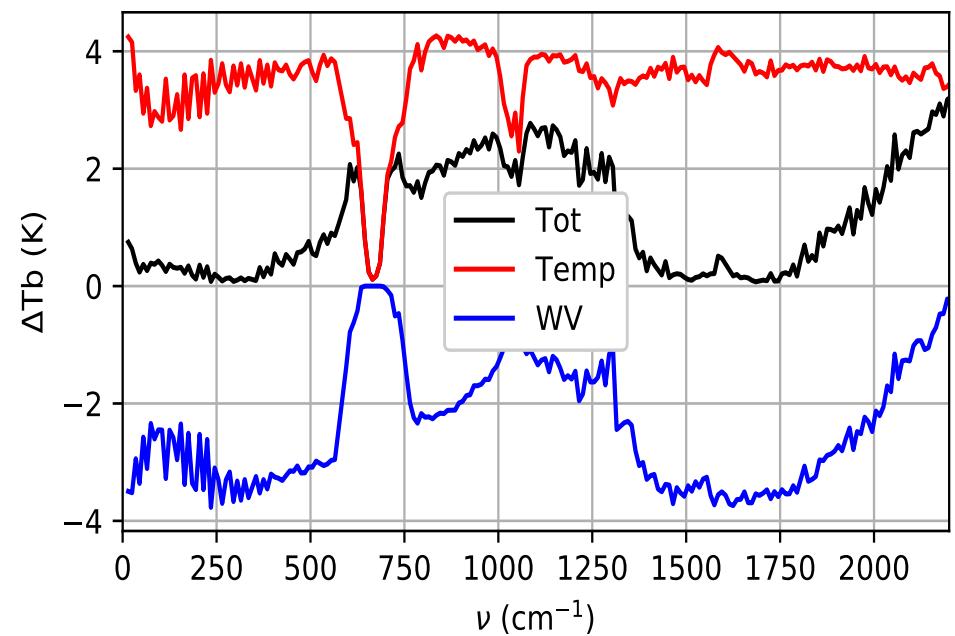
Change in response to a vertically uniform +4K increase of the troposphere

GHG: Only H<sub>2</sub>O + CO<sub>2</sub> + O<sub>3</sub>

Flux at the TOA



Brightness temperature



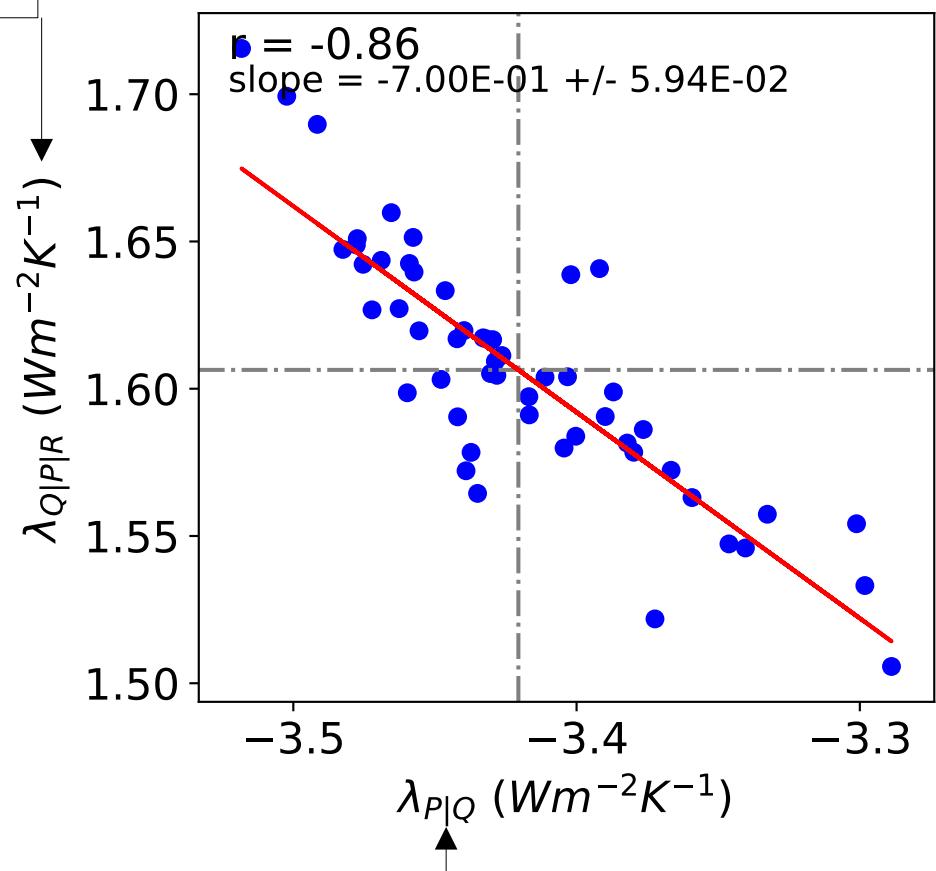
For a mean tropical atmosphere, the **increase in water vapour to keep the relative humidity constant reduces by 56%** the increase in outgoing radiative flux due to the increase in temperature if the specific humidity would remain constant.

# Multimodel analysis (50 CMIP6 models)

*Clear sky, whole globe*

Sensitivity of TOA flux to water vapour change to keep the relative humidity constant

- On average, the increase in water vapour to keep the relative humidity constant reduces the Planck response by 47%
- This partial cancelation is also present when looking at the spread among models



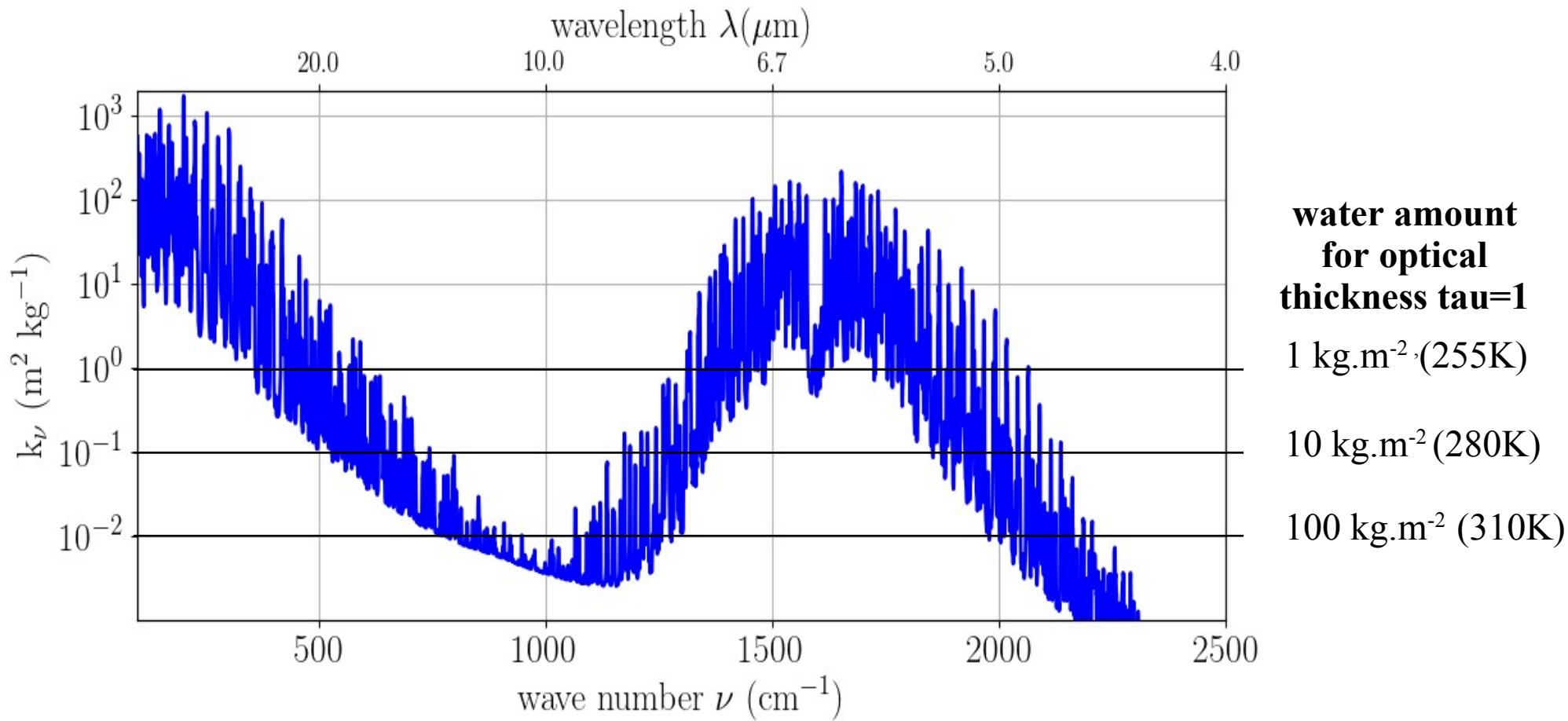
Sensitivity of TOA flux to vertically uniform temperature change at constant specific humidity (Planck response)

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## *Absorption coefficient of $H_2O$*

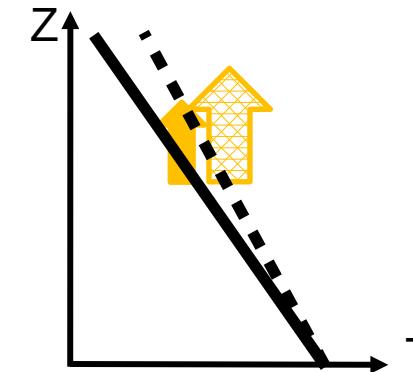
optical thickness  
 $Tau = \kappa * M_{H_2O}$



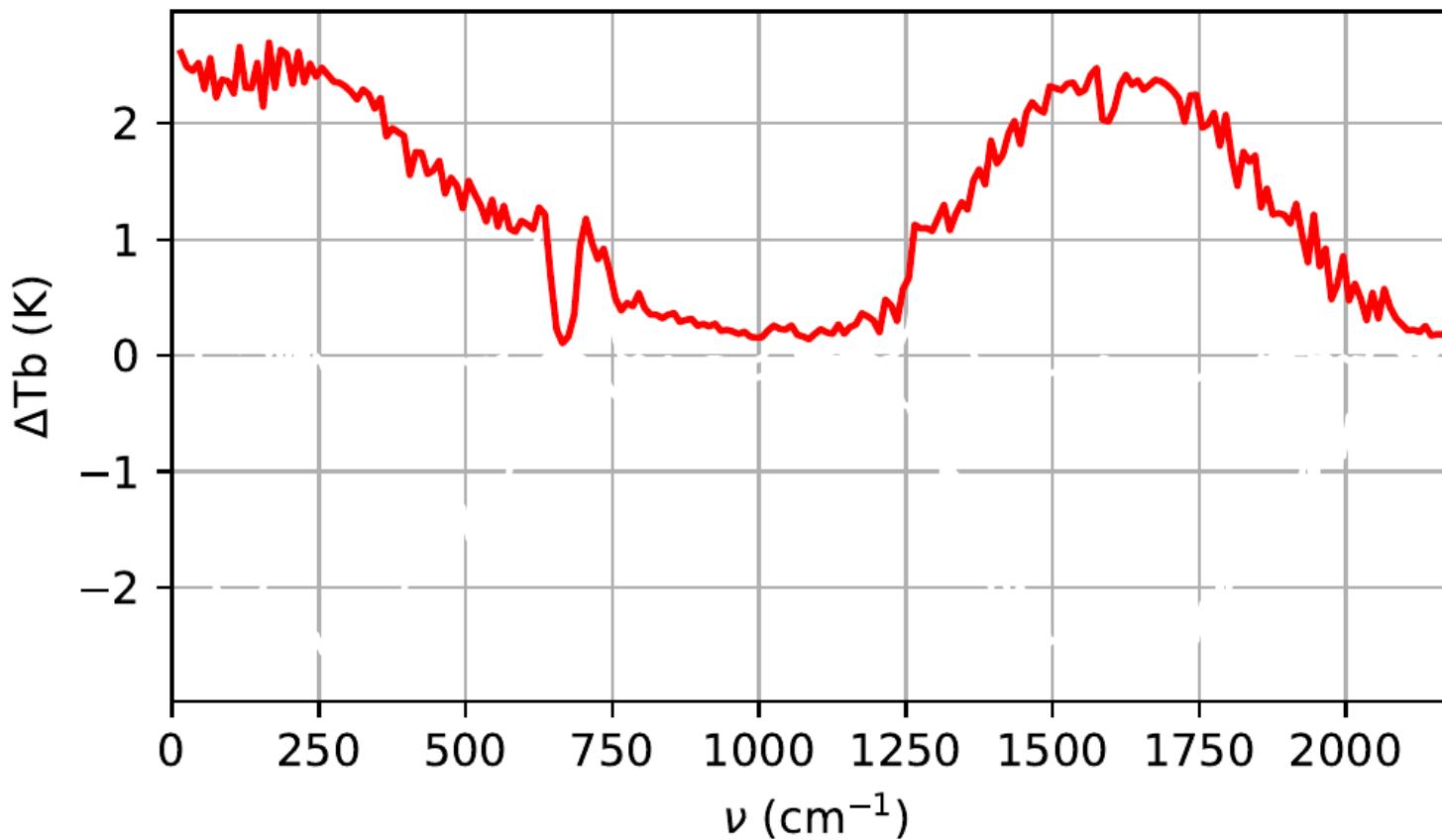
# *For a mean tropical atmosphere (ERA5)*

Change in brightness temperature  
in response to a **change in vertical temperature  
gradient** (lapse rate):

0 at surface, +4K at the tropopause,  $\text{H}_2\text{O}+\text{CO}_2+\text{O}_3$



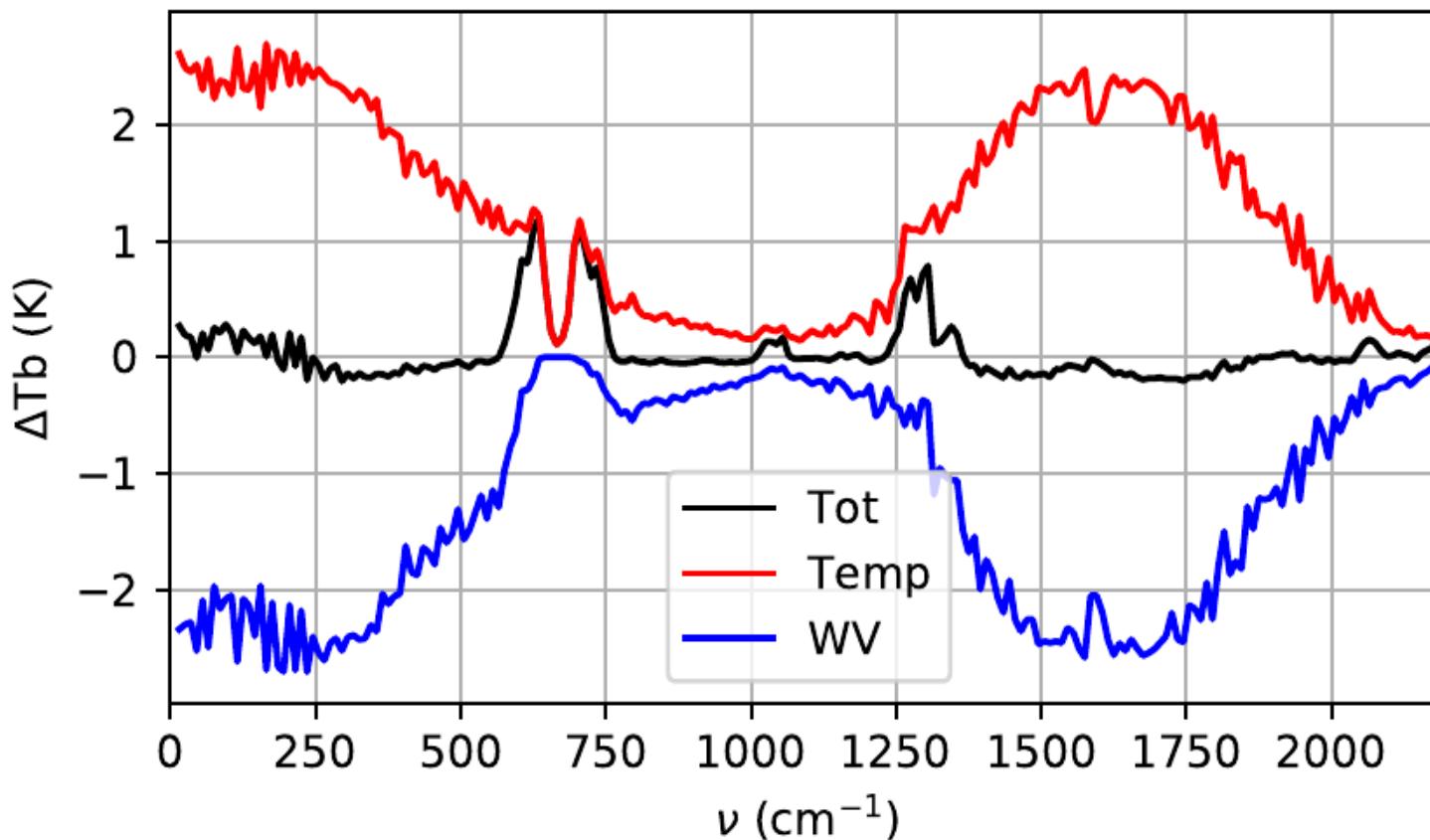
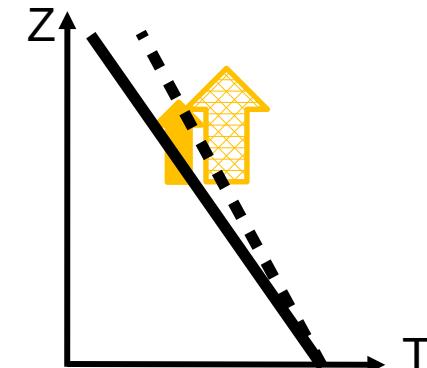
at constant specific  
humidity Q



# *For a mean tropical atmosphere (ERA5)*

Change in brightness temperature  
in response to a **change in vertical temperature  
gradient** (lapse rate):

0 at surface, +4K at the tropopause,  $\text{H}_2\text{O}+\text{CO}_2+\text{O}_3$



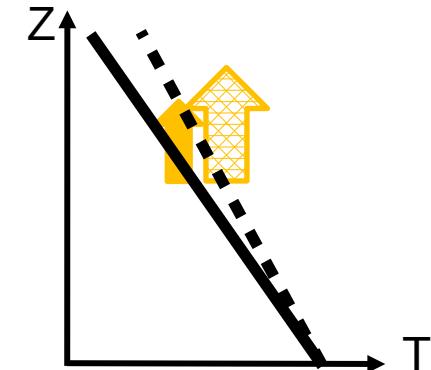
at constant **specific  
humidity Q**

at constant **relative  
humidity**

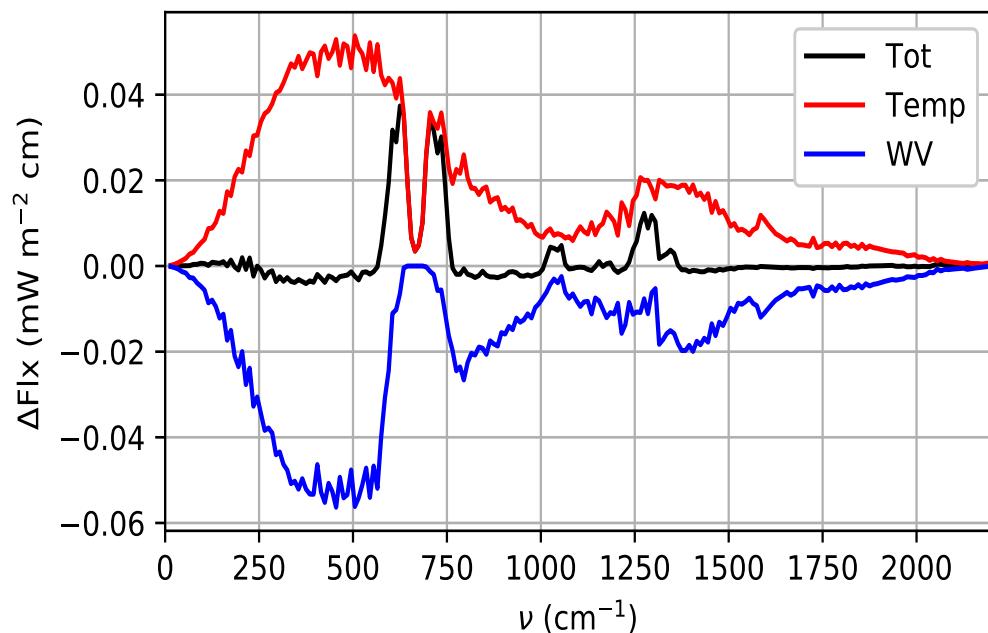
due to change in Q  
to keep relative  
humidity constant

# *For a mean tropical atmosphere (ERA5)*

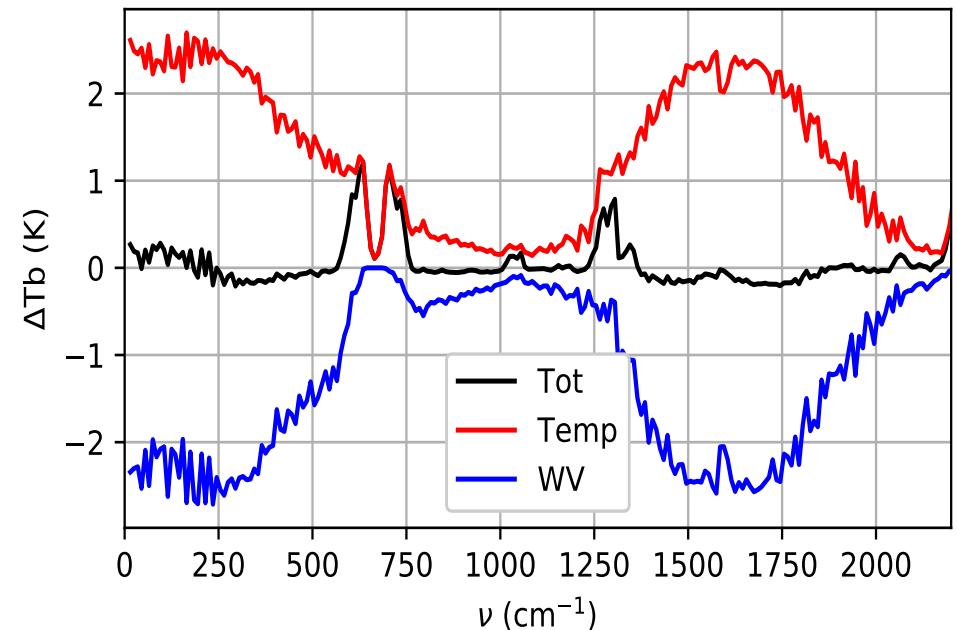
Change in brightness temperature  
in response to a **change in vertical temperature  
gradient** (lapse rate):  
0 at surface, +4K at the tropopause,  $\text{H}_2\text{O}+\text{CO}_2+\text{O}_3$



Flux at the TOA



Brightness temperature



For a mean tropical atmosphere, the **increase in water vapour to keep the relative humidity constant reduces by 90%** the increase in outgoing radiative flux due to change in lapse rate if the specific humidity would remain constant.

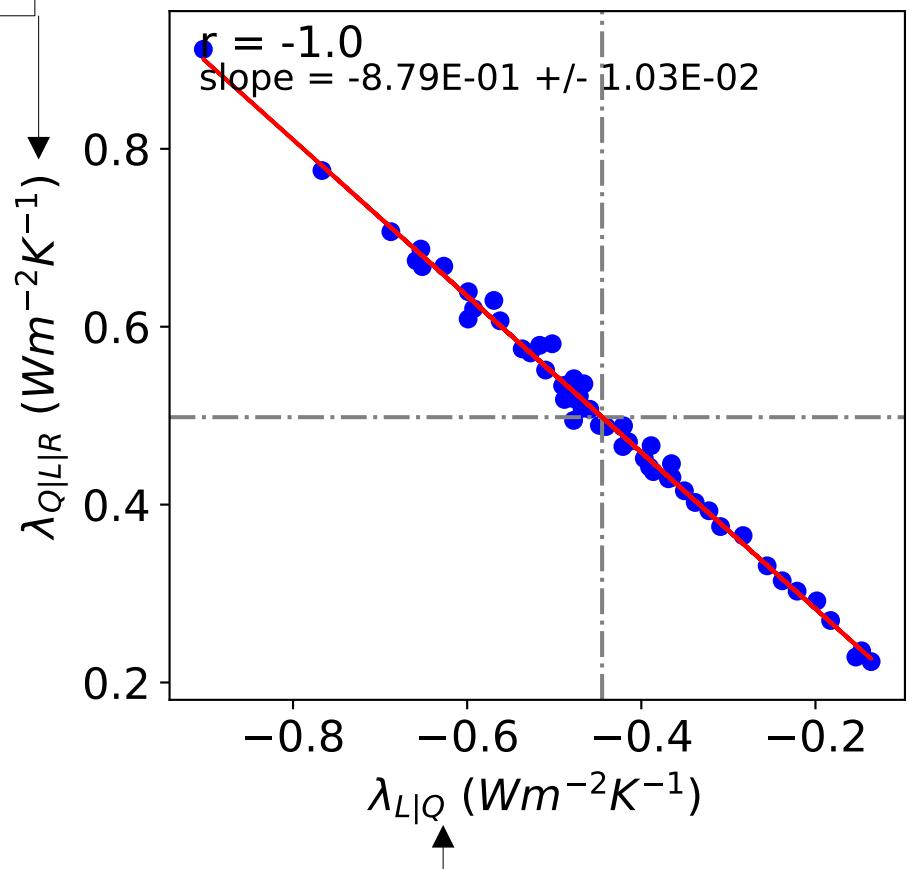
# Multimodel analysis (50 CMIP6 models)

*Clear sky, whole globe, temperature lapse rate*

Sensitivity of TOA flux to water vapour change to keep the relative humidity constant

- On average, the increase in water vapour to keep the relative humidity constant **more than compensate the lapse rate feedback** (110%)
- A strong cancellation is also present when looking at the spread among models

• **The clear sky lapse rate feedback at fixed relative humidity in the LW is almost nul**

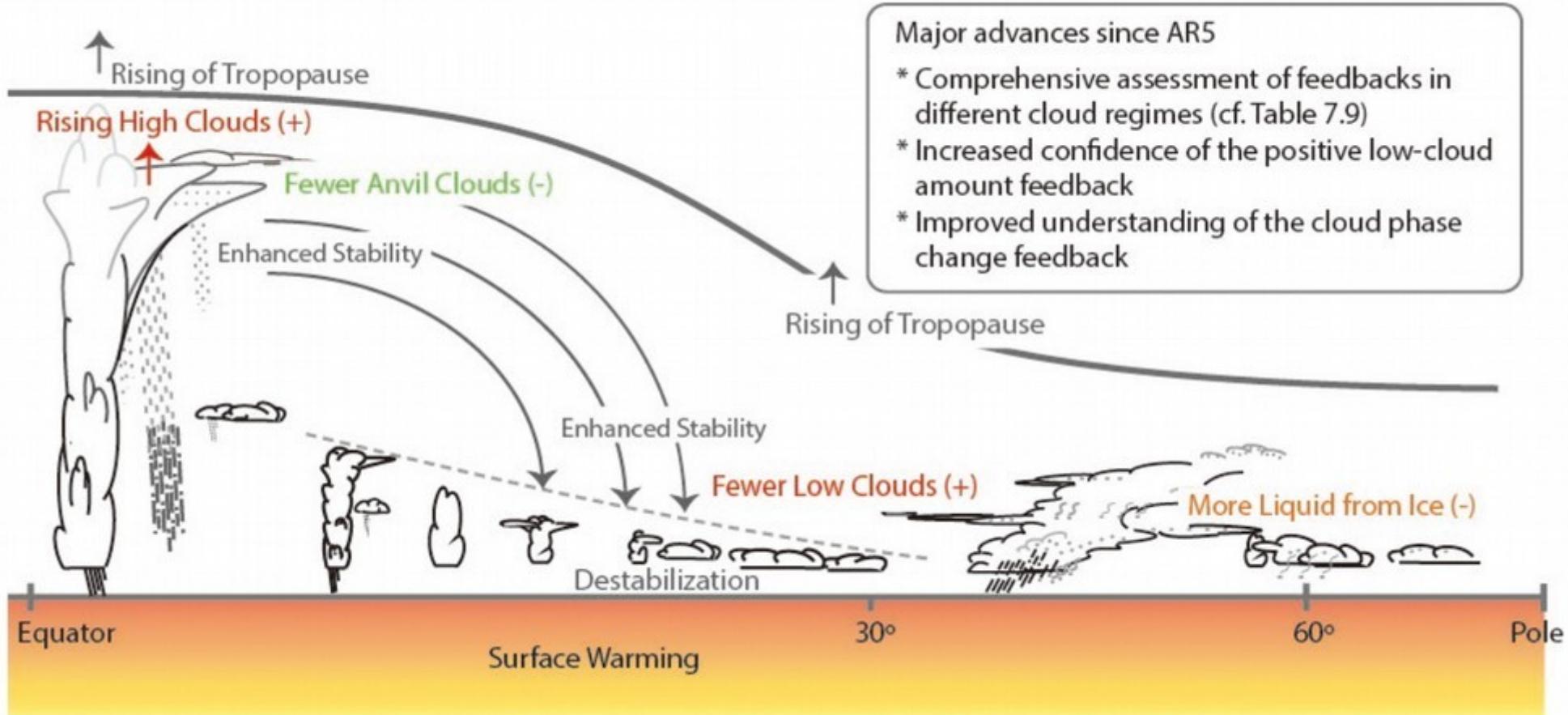


Sensitivity of TOA flux to **change in temperature lapse rate at constant specific humidity**

# Outlook

- Background
- Water vapour feedbacks in idealized cases :The “Simpson law”
- Clear-sky water vapour feedbacks in realistic cases
- Implication for the clear-sky lapse-rate feedback
- **All sky multi-model results**
- Conclusion

# Cloud feedbacks



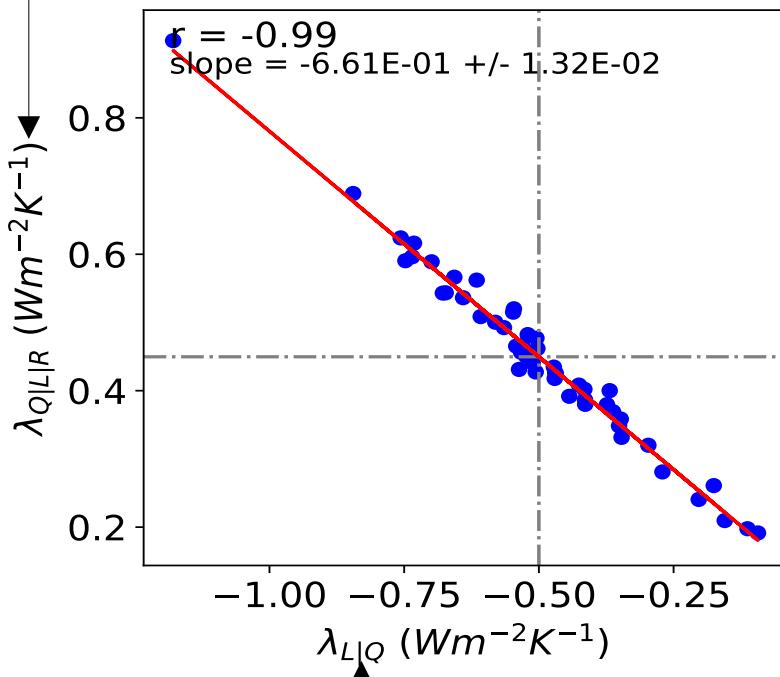
Schematic cross section of diverse cloud responses to surface warming. Thick solid and dashed curves indicate the tropopause and the subtropical inversion layer. Thin grey text and arrows represent robust responses. Text and arrows in red, orange and green show the major cloud responses assessed with high, medium and low confidence, respectively, and the sign of their feedbacks to the surface warming is indicated in the parenthesis.

# Multimodel analysis (50 CMIP6 models)

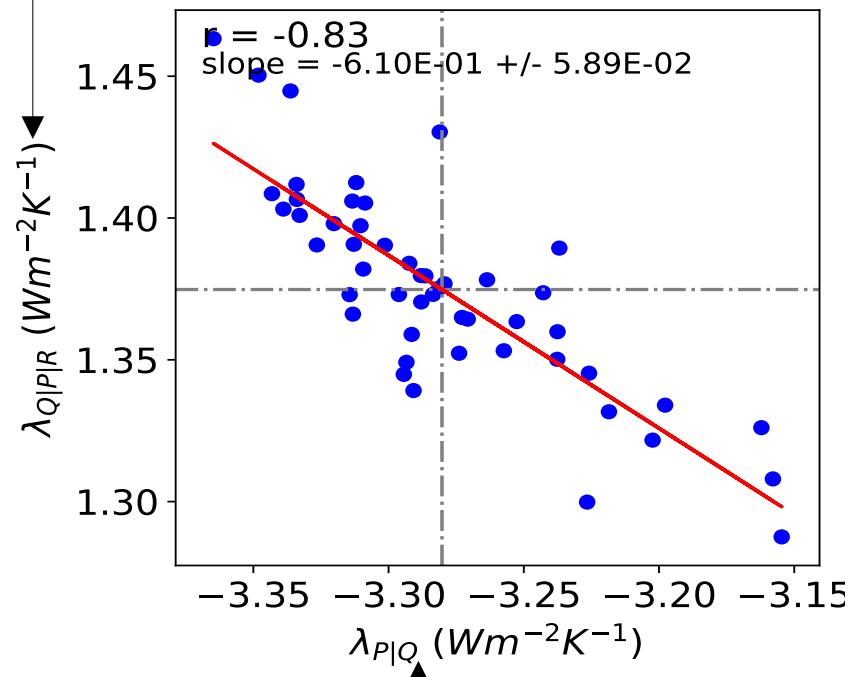
All sky, whole globe

Sensitivity of TOA flux to water vapour change to keep the relative humidity constant

Change in temperature lapse rate



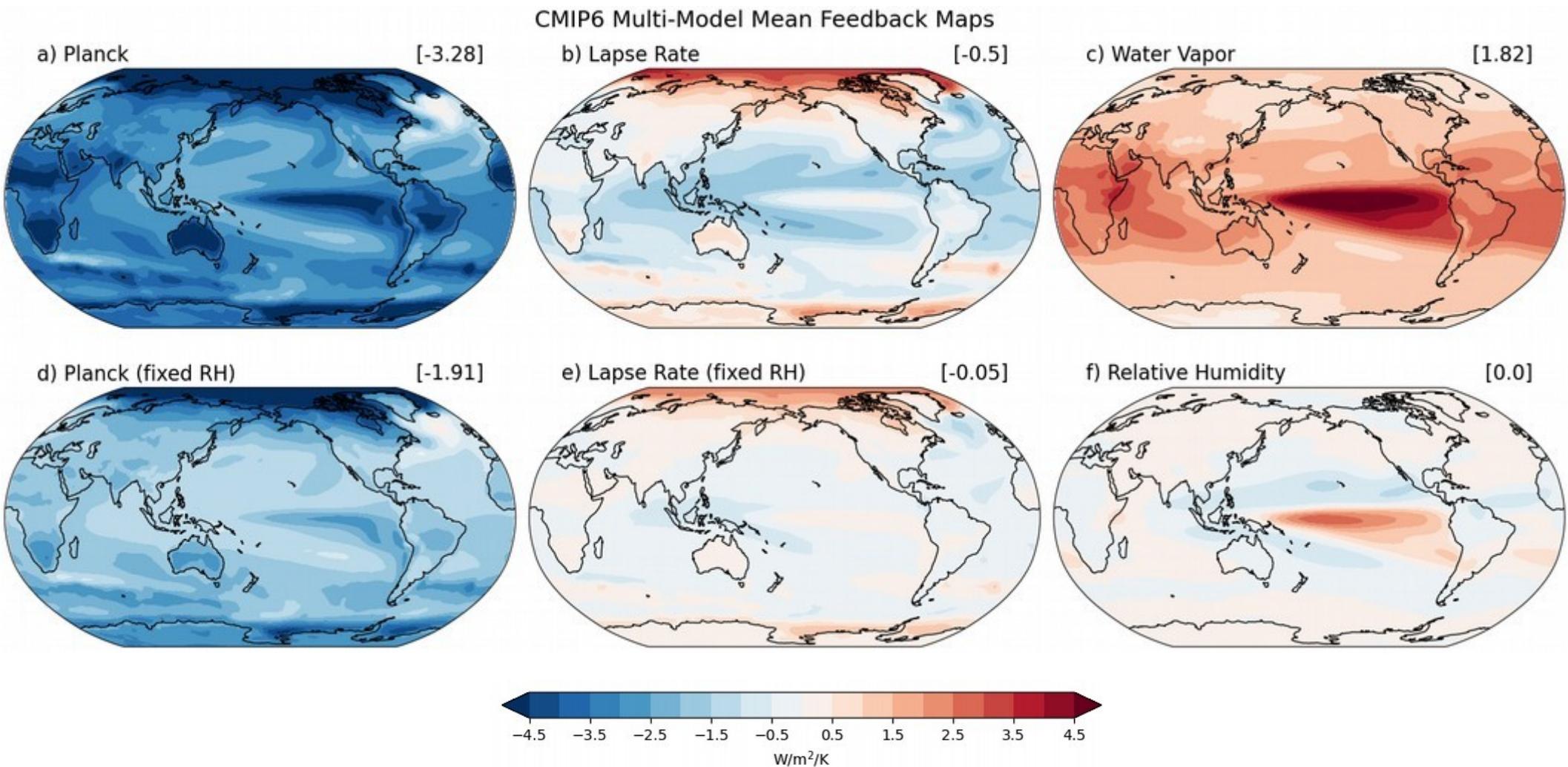
Vertically uniform temp. change (Planck)



Sensitivity of TOA flux to temperature change at constant specific humidity

- On average, the increase in water vapour to keep the relative humidity constant **reduces the Planck response by 40%**, and the **lapse-rate feedback by 90%**
- This partial cancellation is also present when looking at the spread among models

# Climate feedbacks with the absolute and relative humidity decompositions



[courtesy of M. Zelinka 2021]  
(<https://doi.org/10.5281/zenodo.5206851>)

# Multimodel analysis (50 CMIP6 models)

## Climate feedbacks

	$\lambda_{\theta W}$	absolute humidity decomposition			
		$\lambda_{P Q}$	$\lambda_{L Q}$	$\lambda_{Q \theta}$	QSum
mean	-1.95	-3.28	-0.50	1.83	-
std. dev. among models	0.10	0.05	0.19	0.16	0.25

*Temperature + WV feedback*  
*Planck response*  
*Lapse-rate feedback*  
*Specific humidity feedback*  
*Square root of quadratic sum*

# Multimodel analysis (50 CMIP6 models)

## Climate feedbacks

	$\lambda_{\theta W}$	absolute humidity decomposition				relative humidity decomposition			
		$\lambda_{P Q}$	$\lambda_{L Q}$	$\lambda_{Q \theta}$	QSum	$\lambda_{P R}$	$\lambda_{L R}$	$\lambda_{R \theta}$	QSum
mean	-1.95	-3.28	-0.50	1.83	-	-1.91	-0.05	0.01	-
std. dev. among models	0.10	0.05	0.19	0.16	0.25	0.03	0.07	0.06	0.10

Temperature + WV feedback  
 Planck response  
 Lapse-rate feedback  
**Specific humidity**  
 Square root of quadratic sum

Planck response  
 Lapse-rate feedback  
**Relative humidity**  
 Square root of quadratic sum

## **Conclusion**

- In spectral ranges where  $H_2O$  is the main absorber and the atmosphere is optically thick, a change in atmospheric temperature does not induce a change in LW fluxes at the top of the atmosphere if the relative humidity remains constant
- This result is based on the fundamental laws of radiation
- The lapse rate feedback at fixed relative humidity in the LW is almost null (clear-sky and all sky)
- This allows a simple physically based estimate of the water vapour feedback
- The relative humidity feedback decomposition is much more relevant than the specific humidity decomposition
- Interest of using temperature as “vertical coordinate” instead of pressure (altitude)

## This presentation is mainly based on:

- Simpson, G. (1928). Some studies in terrestrial radiation. *Memoirs of the Royal Meteorological Society*, 2(16), 69–95.
- Jeevanjee, N., Koll, D., & Lutsko, N. (2021). Simpson's law and the spectral cancellation of climate feedbacks. *Geophys. Res. Lett.*.
- Ingram, W. (2010). A very simple model for the water vapour feedback on climate change. *QJRMS*, 136 (646), 30-40. doi: 10.1002/qj.546
- Held, I. M., & Shell, K. M. (2012, April). Using relative humidity as a state variable in climate feedback analysis. *J. Clim.*, 25 (8), 2578–2582. doi: 10.1175/JCLI-D-11-00721.1
- Ongoing work with M. Zlinka, S. Bony, R. Armante, etc.

Thank you for your attention



Thank you for your attention

- Dans les domaines spectraux où H<sub>2</sub>O est le principal absorbant et l'atmopshère est optiquement épaisse, un changement de la température de l'atmosphère n'induit pas un changement des flux au sommet de l'atmosphère si l'humidité relative reste constante
- L'utilisation du couple température – humidité relative (T-RH) est plus pertinente celle température – humidité spéciifique (T-q)

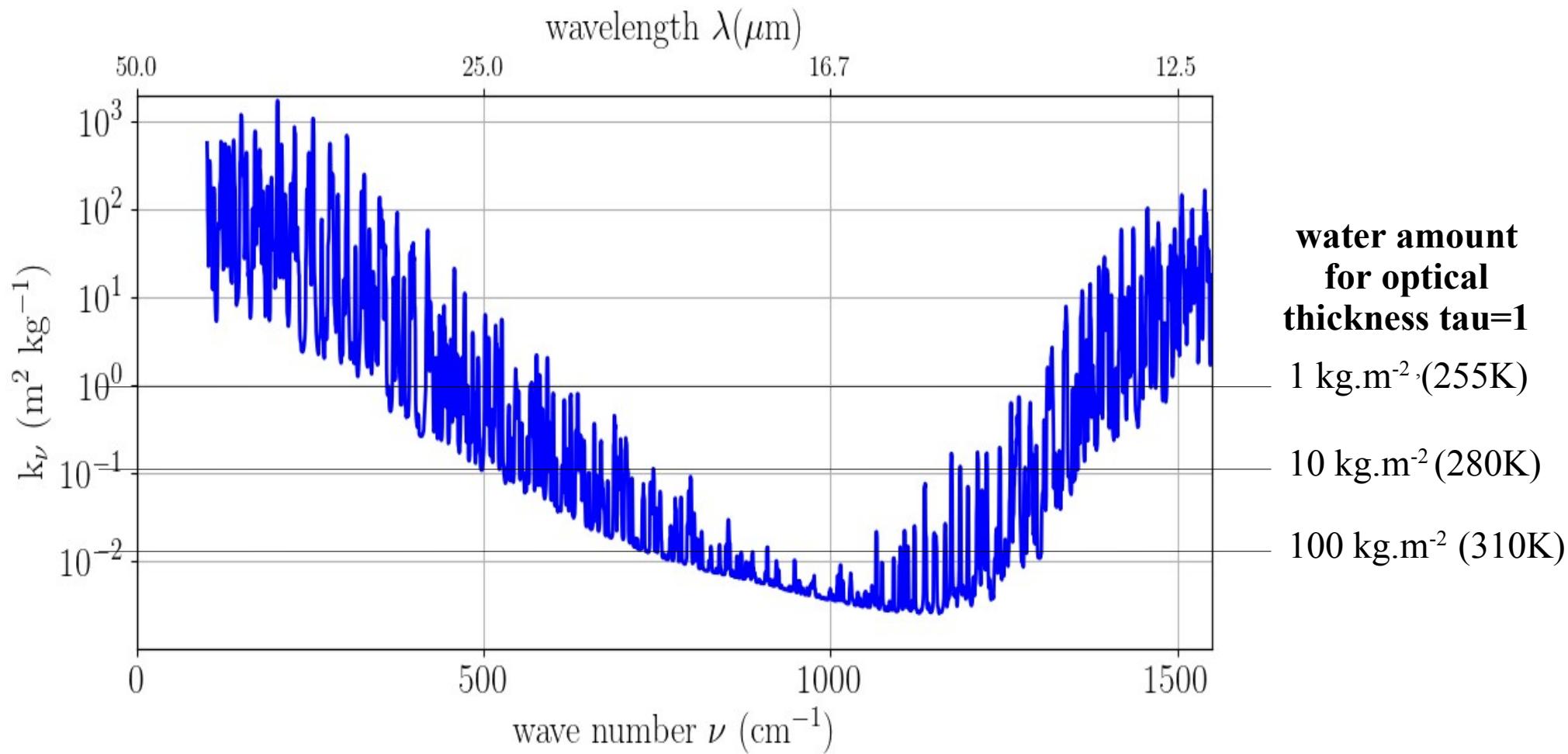
## **Analyse multimodèle:**

- *Analyse des différences: recherche de problèmes, des origines des désaccords*
- *Analyse des ressemblances: plusieurs planètes légèrement différentes mais obéissant aux mêmes lois physiques*

## **Conclusion**

- Dans les domaines spectraux où H<sub>2</sub>O est le principal absorbant et l'atmosphère est optiquement épaisse, un changement de la température de l'atmosphère n'induit pas un changement des flux au sommet de l'atmosphère si l'humidité relative reste constante
- L'utilisation du couple température – humidité relative (T-RH) est plus pertinente celle température – humidité spécifique (T-q)
- Ces propriétés se retrouvent dans un contexte multi-modèle pour des changement du gradient vertical de température et pour un changement verticalement uniforme de la température
- Les incertitudes les plus importantes proviennent de l'humidité relative aussi bien en terme d'état moyen que de variation lors d'un changement climatique

**optical thickness**  
**Tau =  $\kappa * M_{H_2O}$**



# Emission height

$\omega(z)$  : conditional probability that photons emitted at  $z$  reach the TOA

$$\omega(z) = \frac{1}{1 - \Gamma_s} \frac{\partial \Gamma(z)}{\partial z}$$

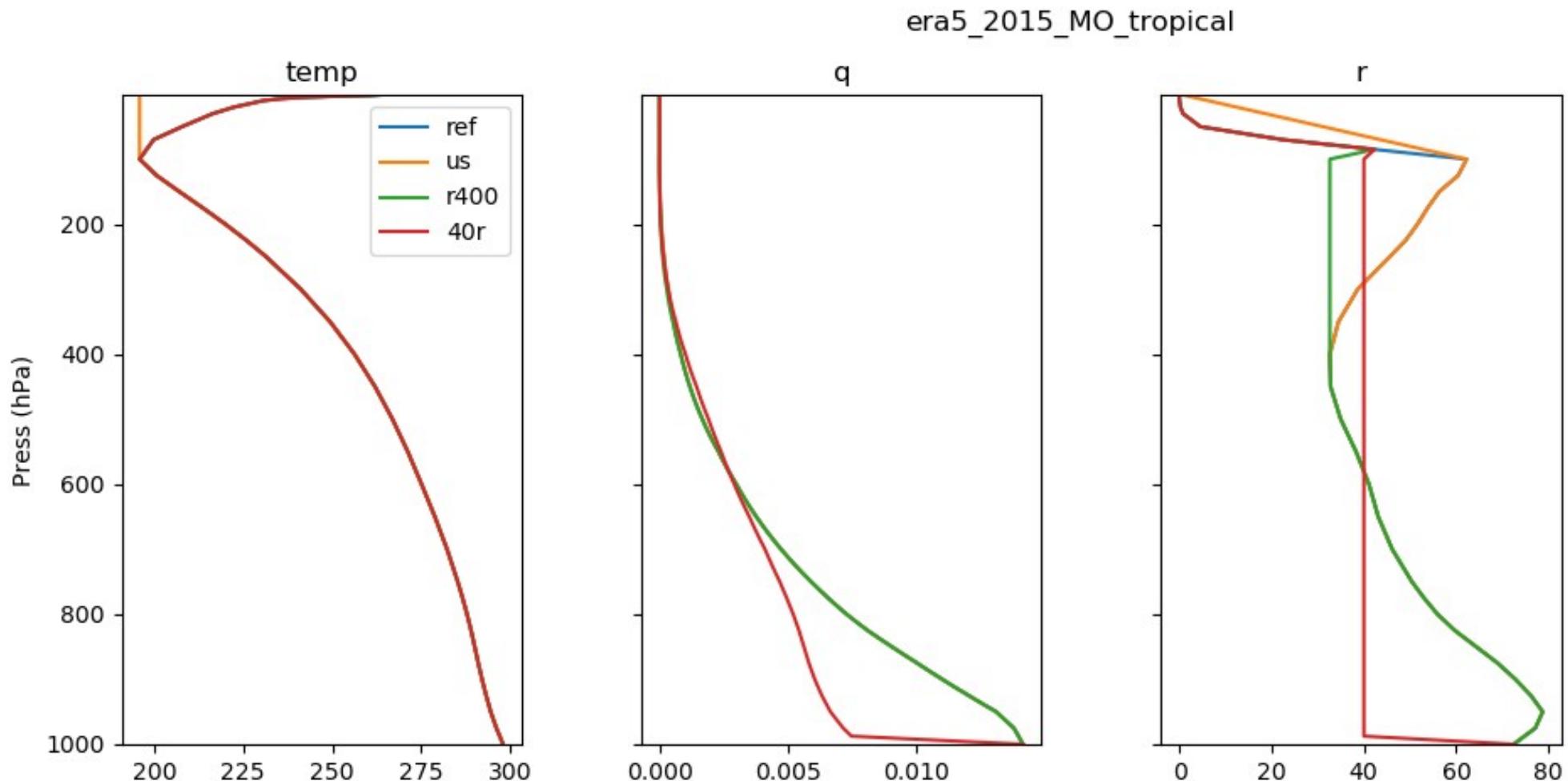
**$\Omega(z)$ : Probability that photons emitted by the atmosphere and that reach the TOA have been emitted at altitude  $z$**

$$\Omega(z) = \frac{1}{(1 - \Gamma_s)B_e} \frac{\partial \Gamma(z)}{\partial z} B(z)$$

The **mean altitude** where these photons have been emitted is then:

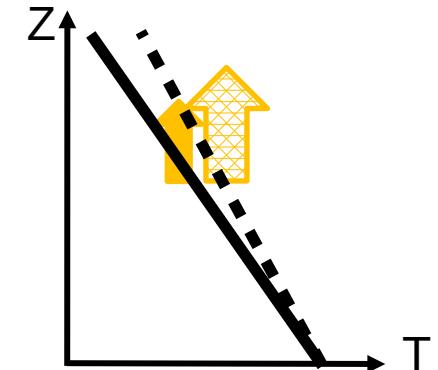
$$\bar{Z}_e = \int_0^H z \Omega(z) dz$$

# *For a mean tropical atmosphere (ERA5)*

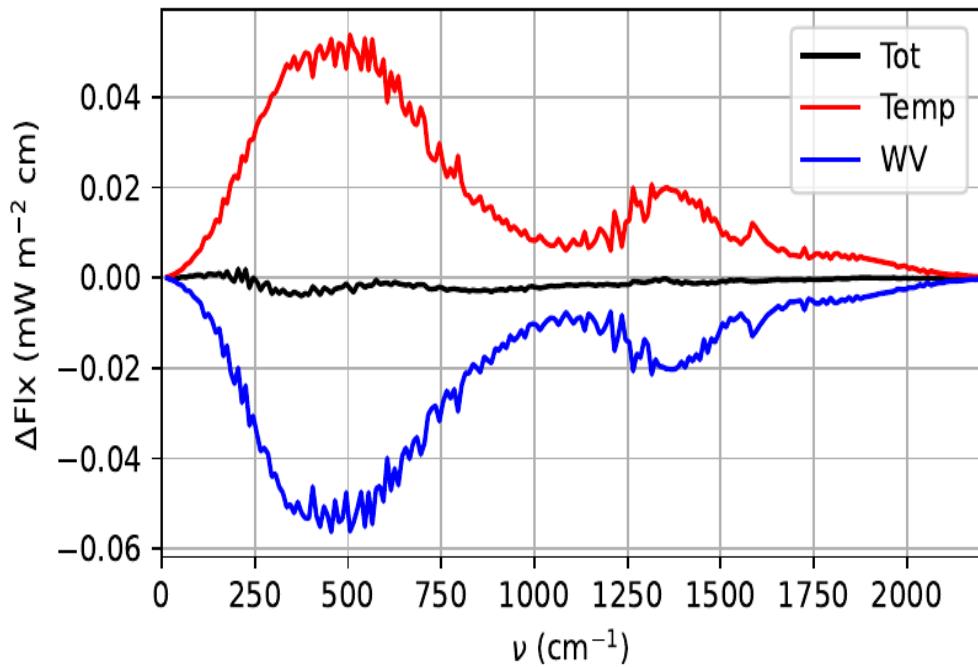


# *For a mean tropical atmosphere (ERA5)*

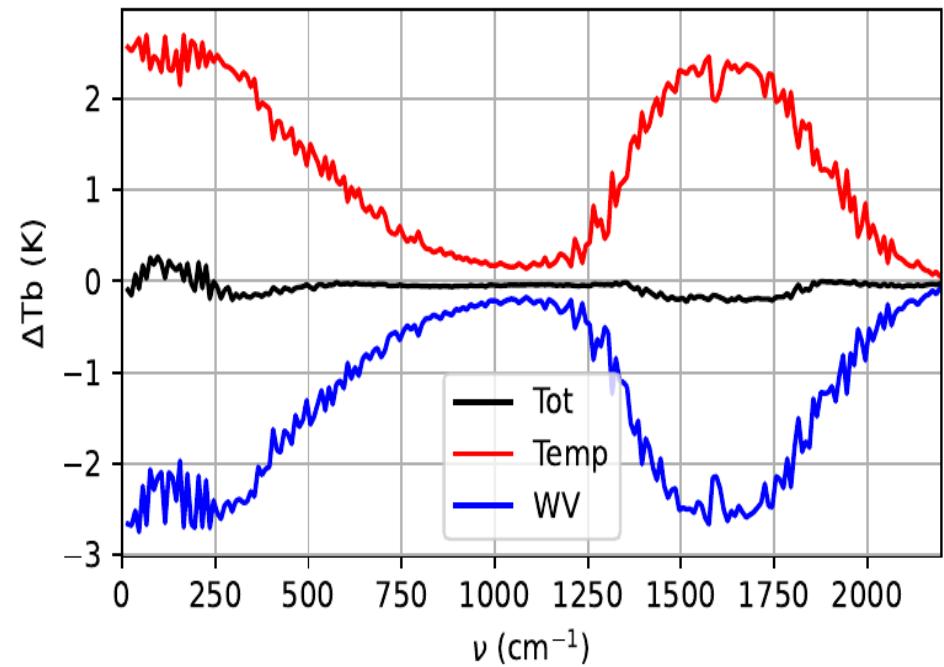
Change in brightness temperature  
in response to a **change in vertical temperature  
gradient** (lapse rate):  
0 at surface, +4K at the tropopause, H<sub>2</sub>O only



Flux at the TOA



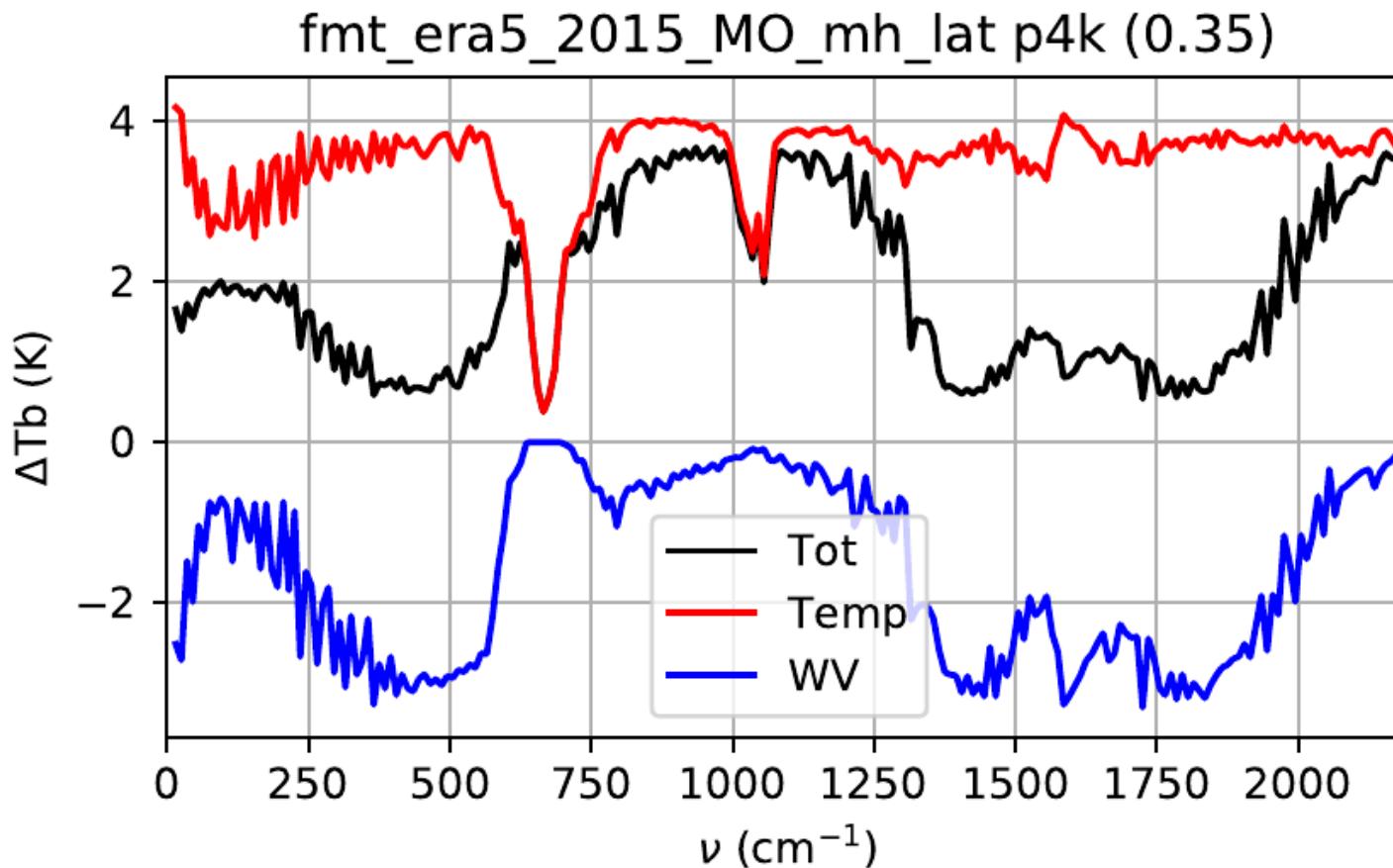
Brightness temperature



For a mean tropical atmosphere with only H<sub>2</sub>O, the **increase in water vapour to keep the relative humidity constant reduces by 107%** the increase in outgoing radiative flux due to change in lapse rate if the specific humidity would remain constant.

# *For mean mid-high latitude atmosphere*

Change in brightness temperature  
in response to a vertically **uniform +4K increase**:



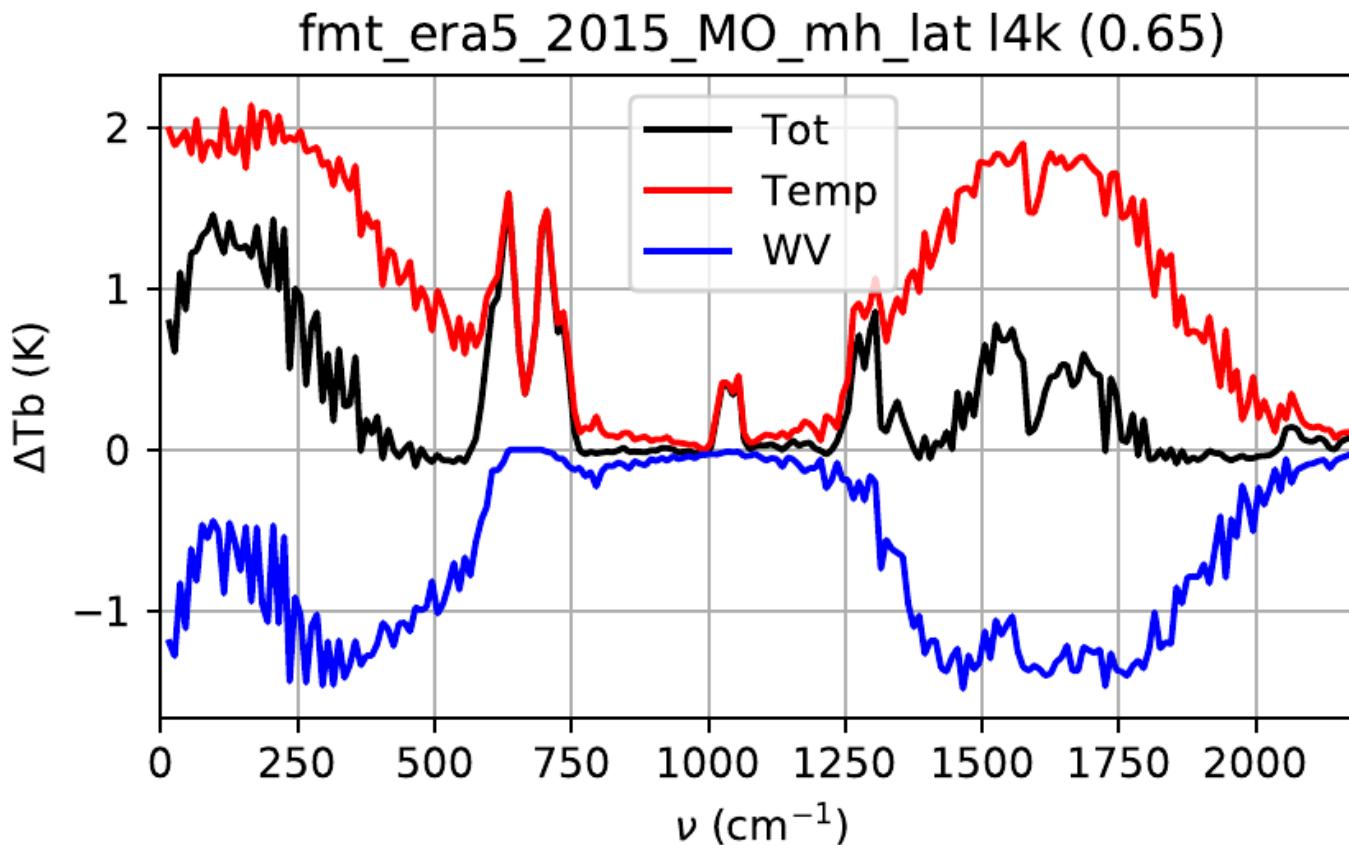
at constant **specific**  
humidity

at constant **relative**  
humidity

due to change in  $q$  to  
keep relative  
humidity constant

# *For mean mid-high latitude atmosphere*

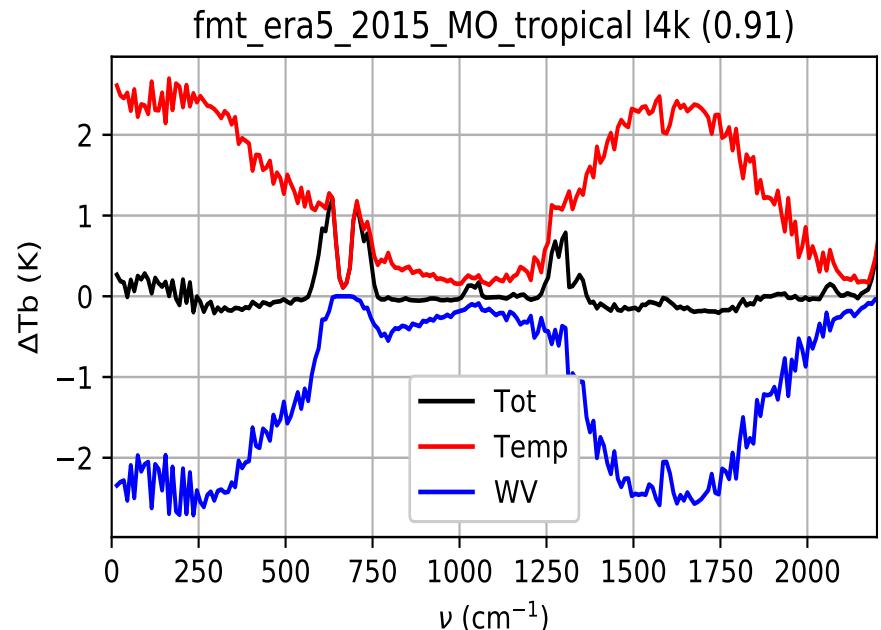
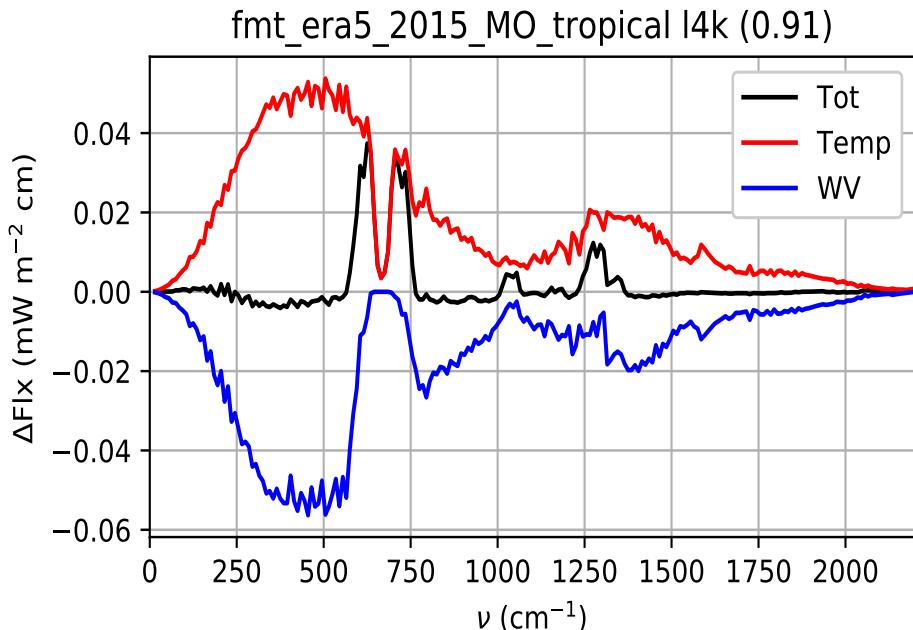
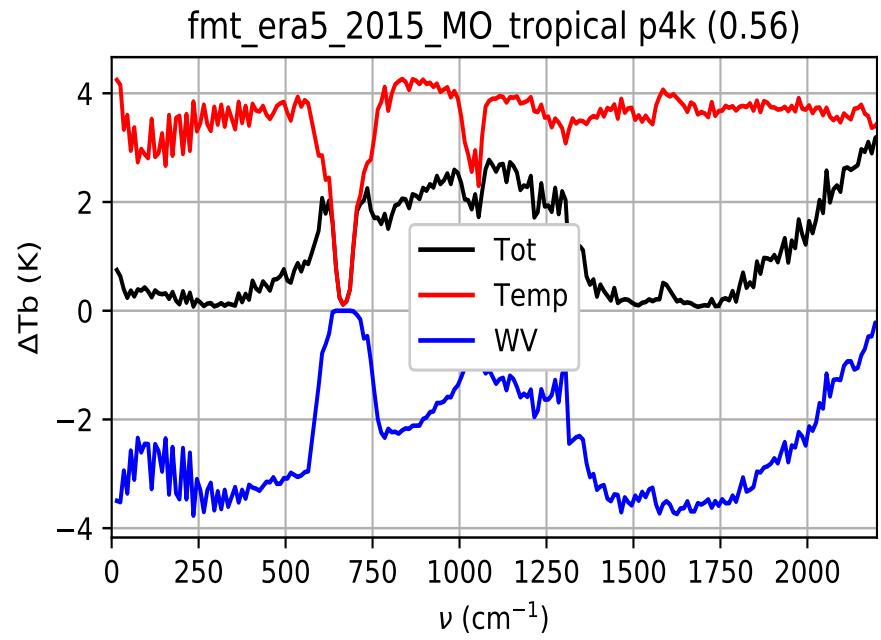
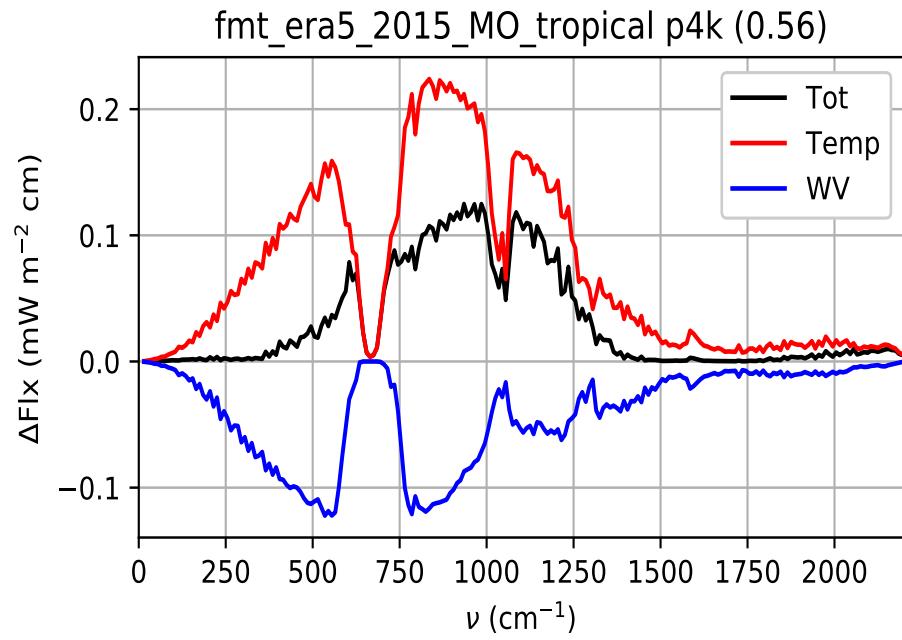
Change in brightness temperature  
in response to a **change in vertical temperature gradient (lapse rate):**  
0 at surface, +4K at the tropopause

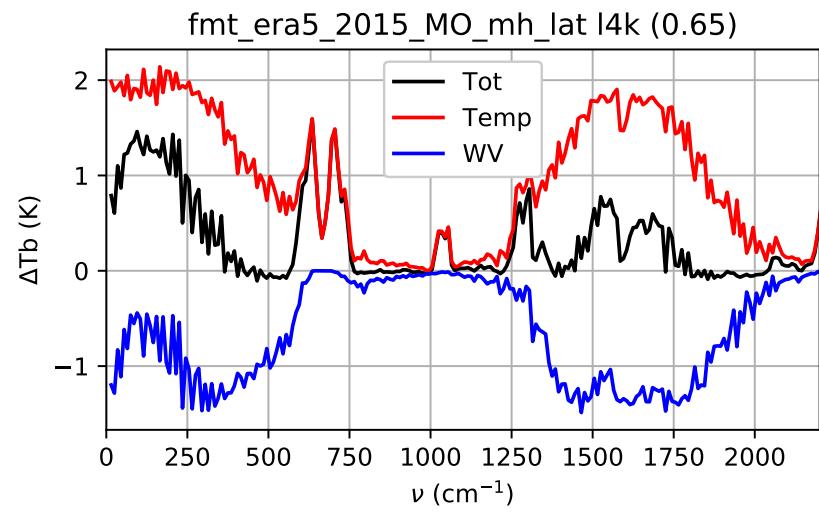
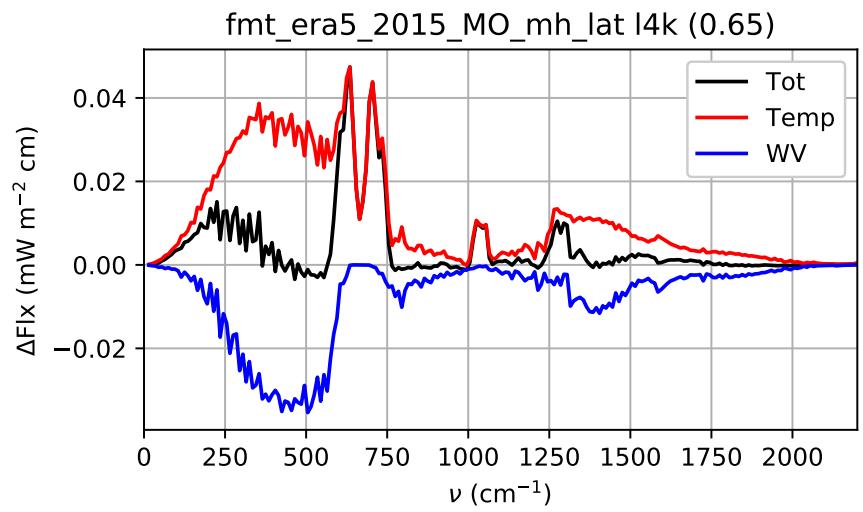
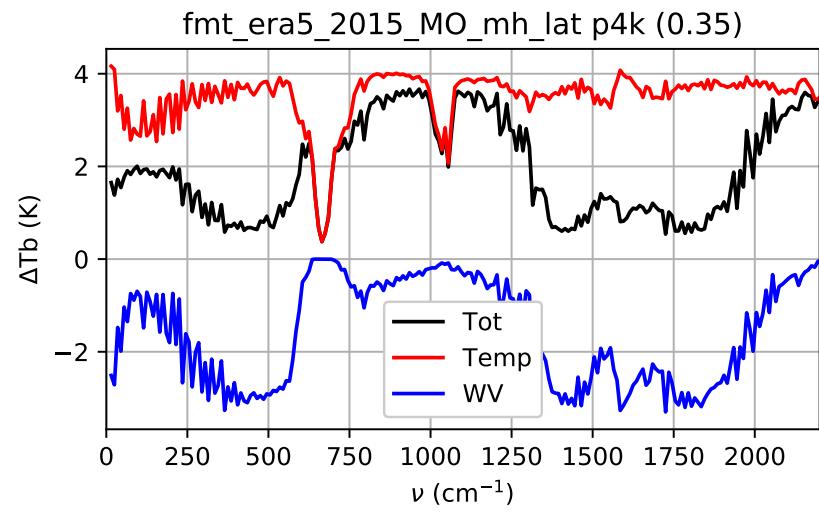
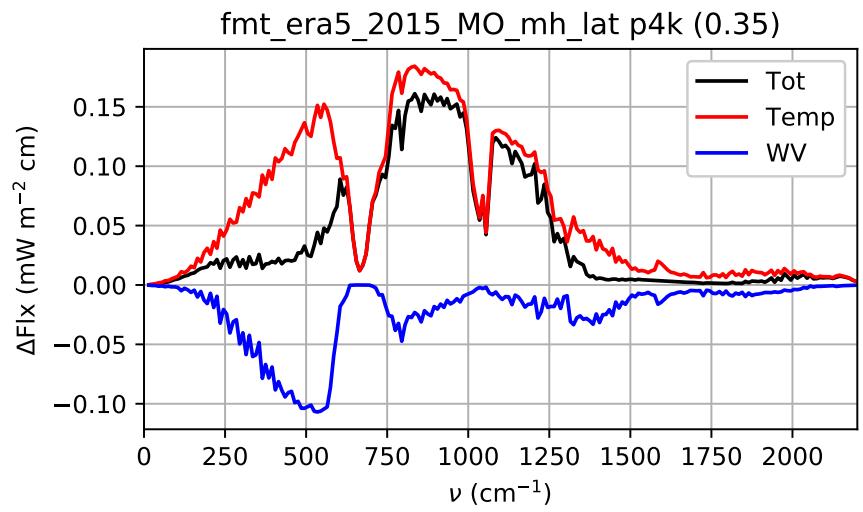


at constant specific humidity

at constant relative humidity

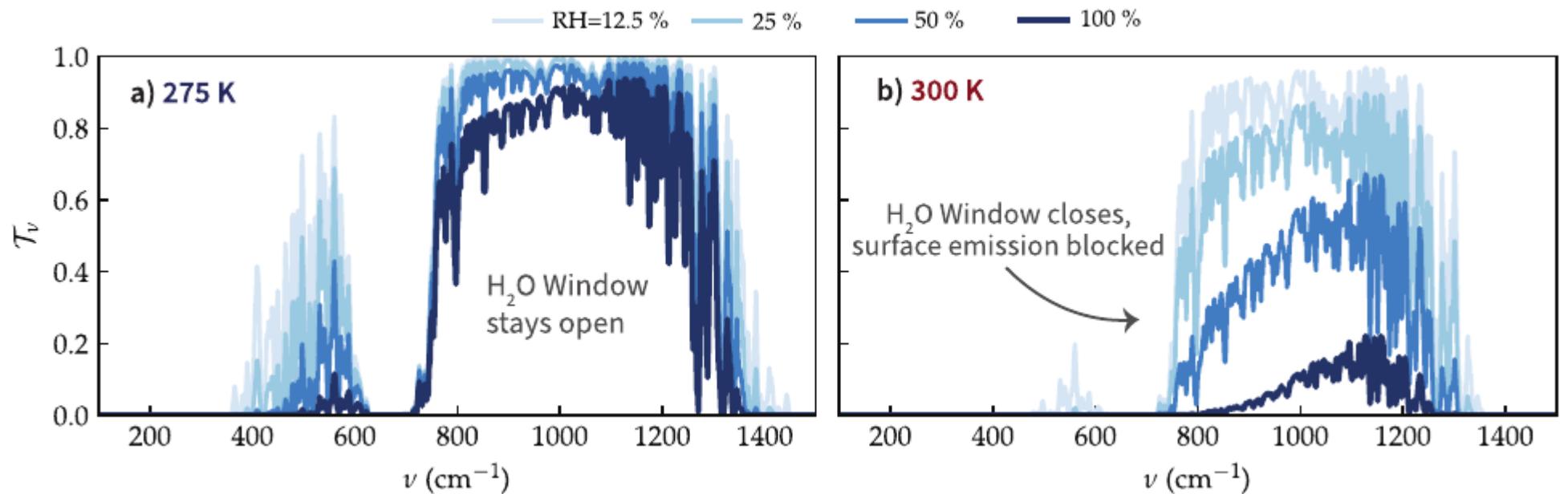
due to change in  $q$  to keep relative humidity constant



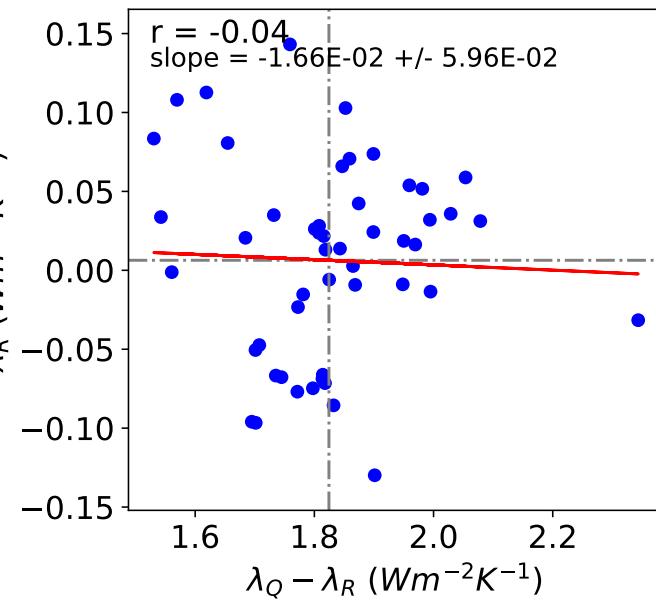
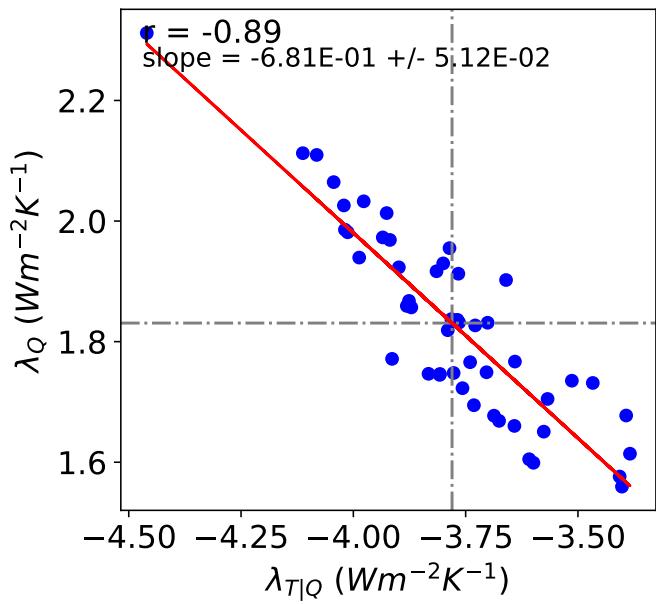
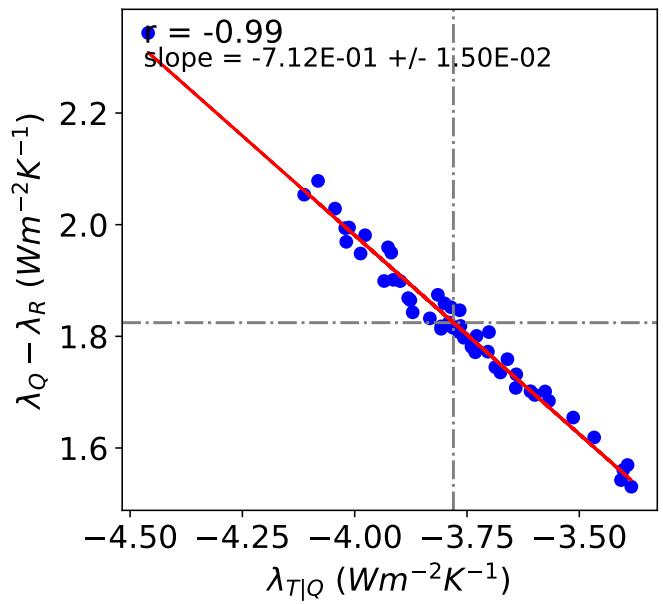


# *For idealized clear sky tropical atmospheres with constant relative humidity*

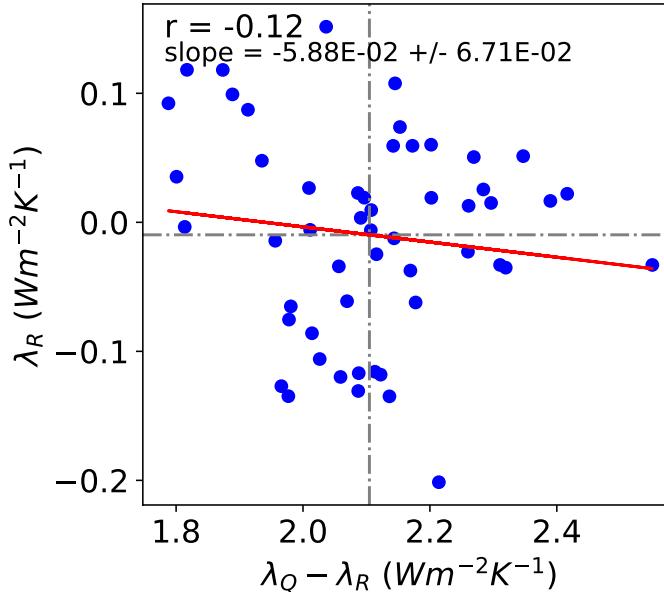
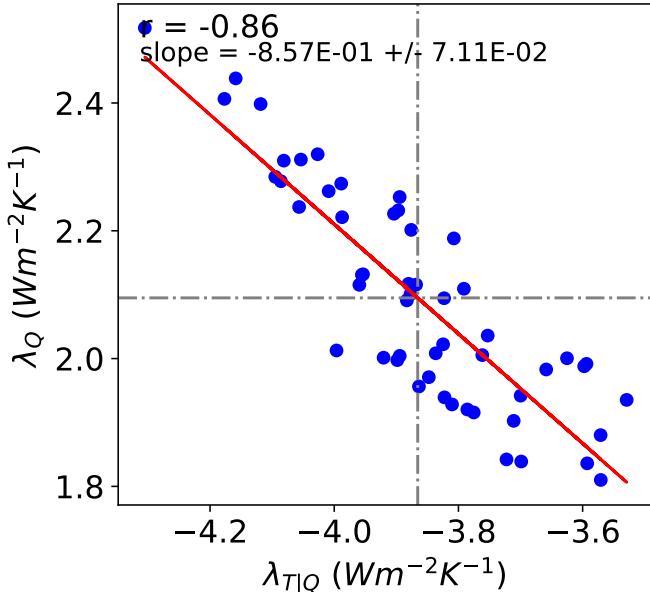
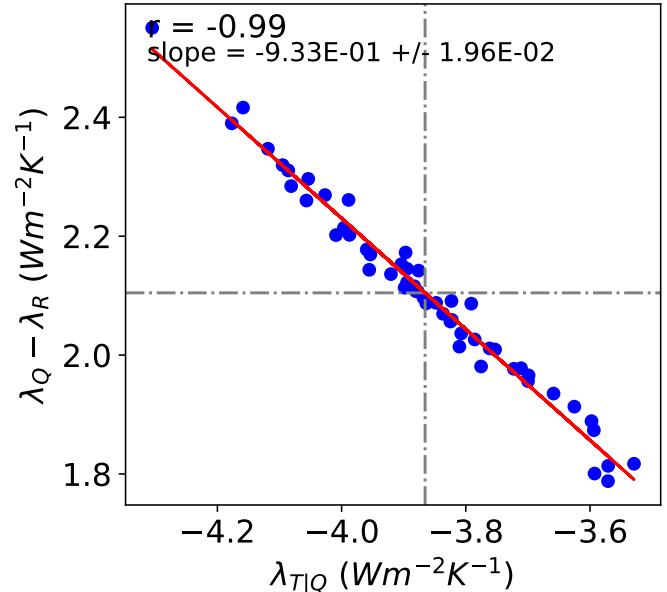
## Clear sky transmittivity



## All sky

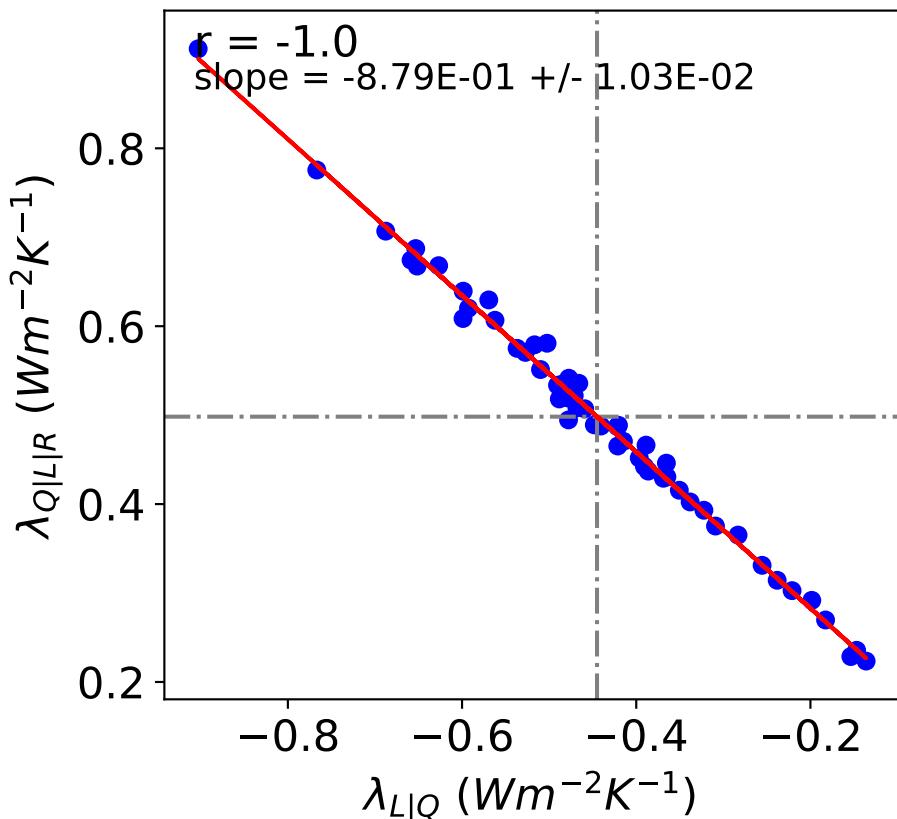


## Clear sky

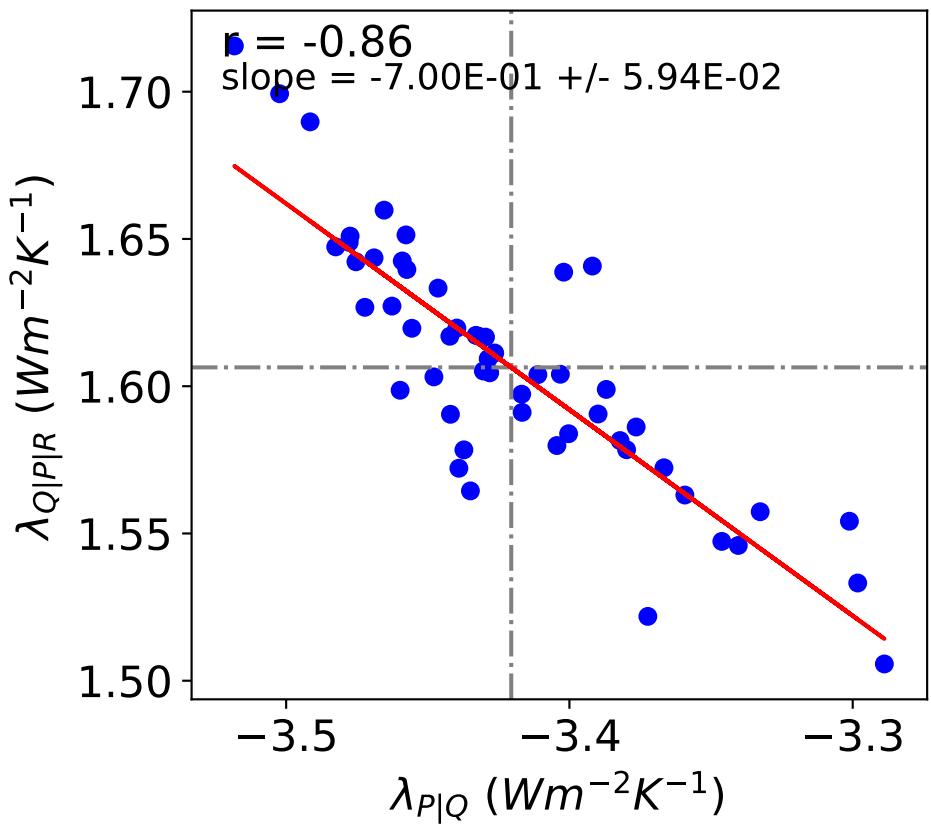


# Analyse multimodèle

*Clear sky, constant RH*  
*For 50 CMIP6 models*



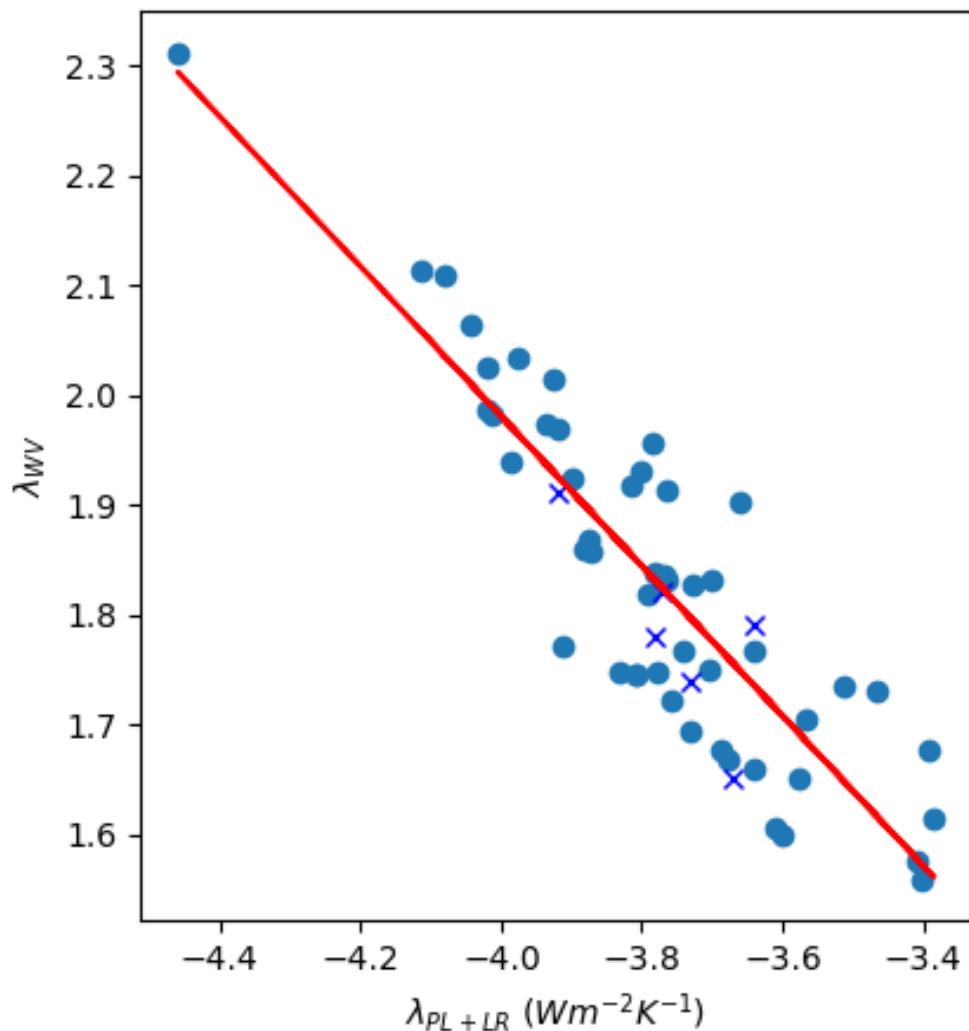
Sensibilité du flux TOA à un changement de lapse-rate à humidité constante



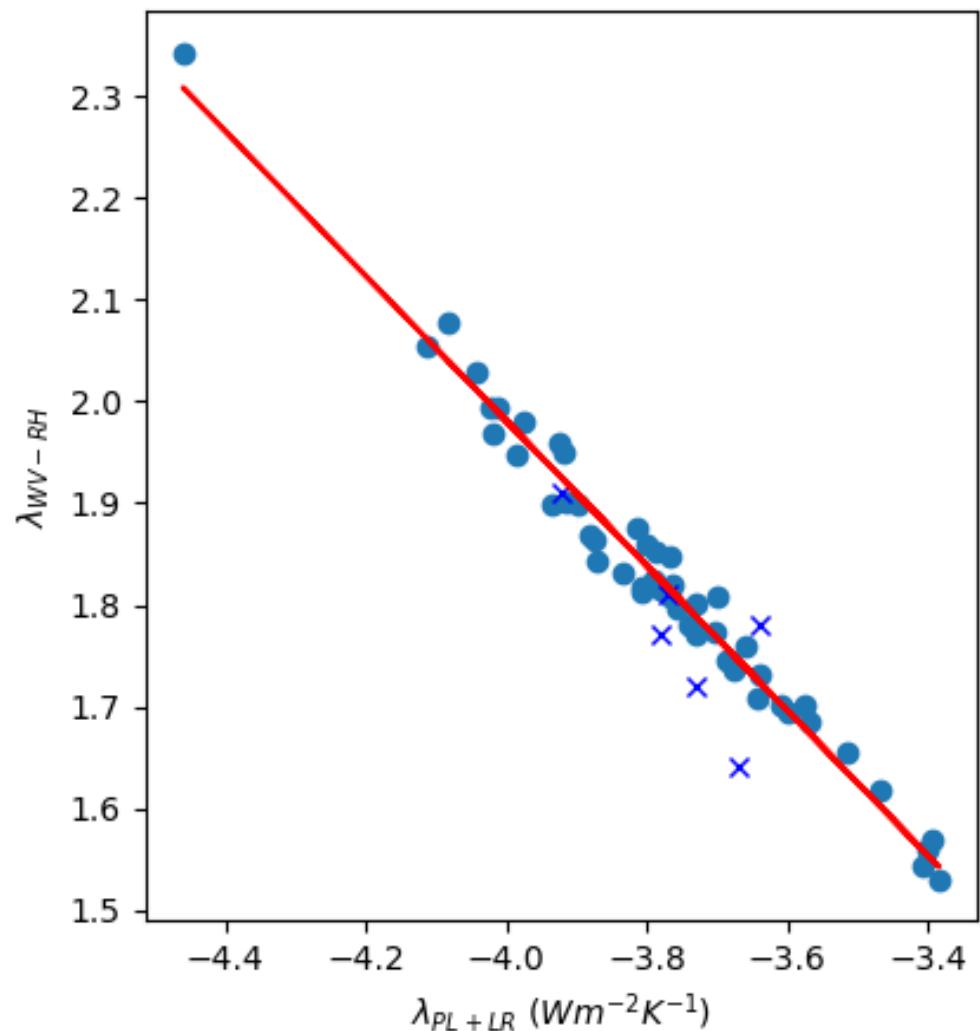
Sensibilité du flux TOA à un changement verticalement uniforme de T à humidité constante

# Feedback parameters for CMIP6 models

water-vapor vs  
temperature feedbacks



water-vapor with no RH change vs  
temperature feedbacks

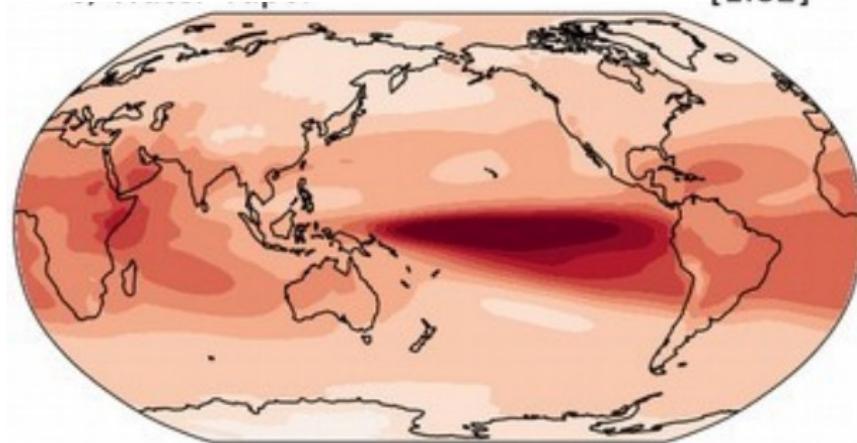


# Climate feedbacks with the absolute and relative humidity decompositions

**due to change in specific humidity**

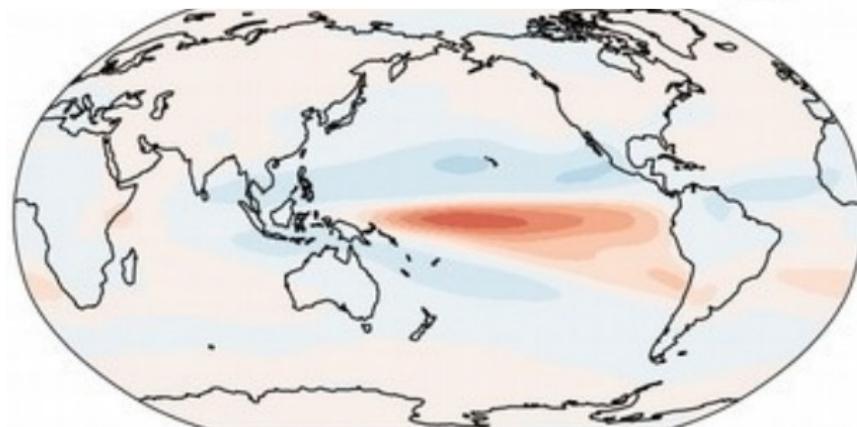
(kg/kg)

[1.82]



**due to change in relative humidity**

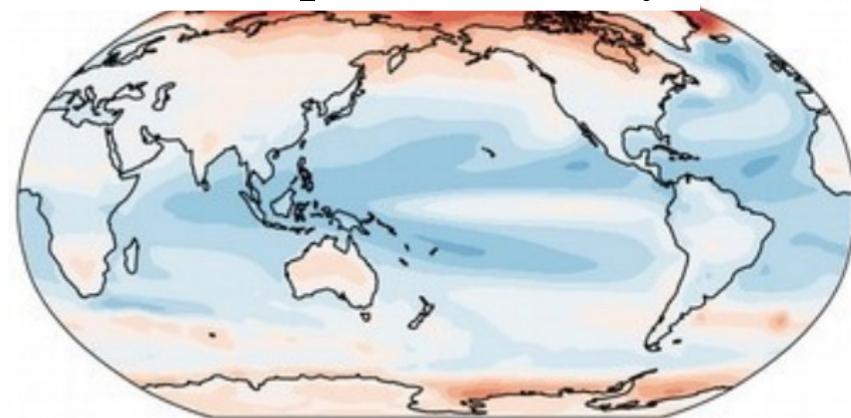
[0.0]



**due to change in temp.  
vert. gradient**

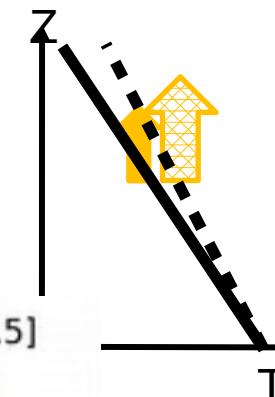
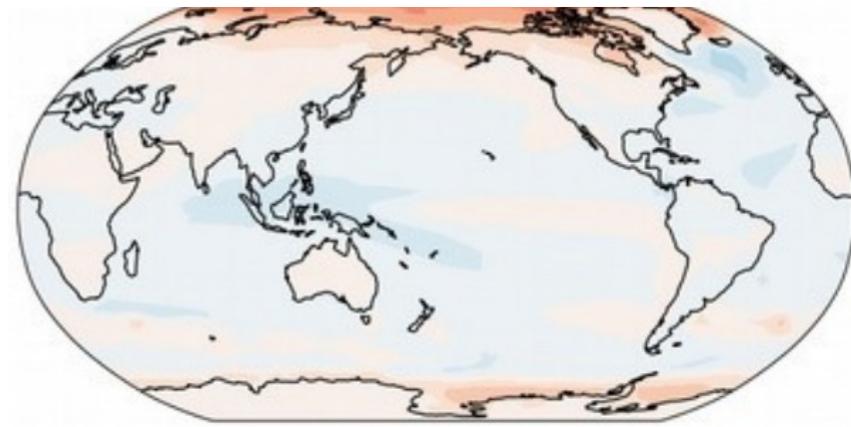
at constant specific humidity

[-0.5]



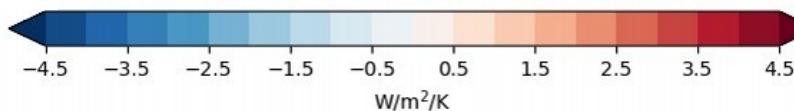
at constant relative humidity

[-0.05]



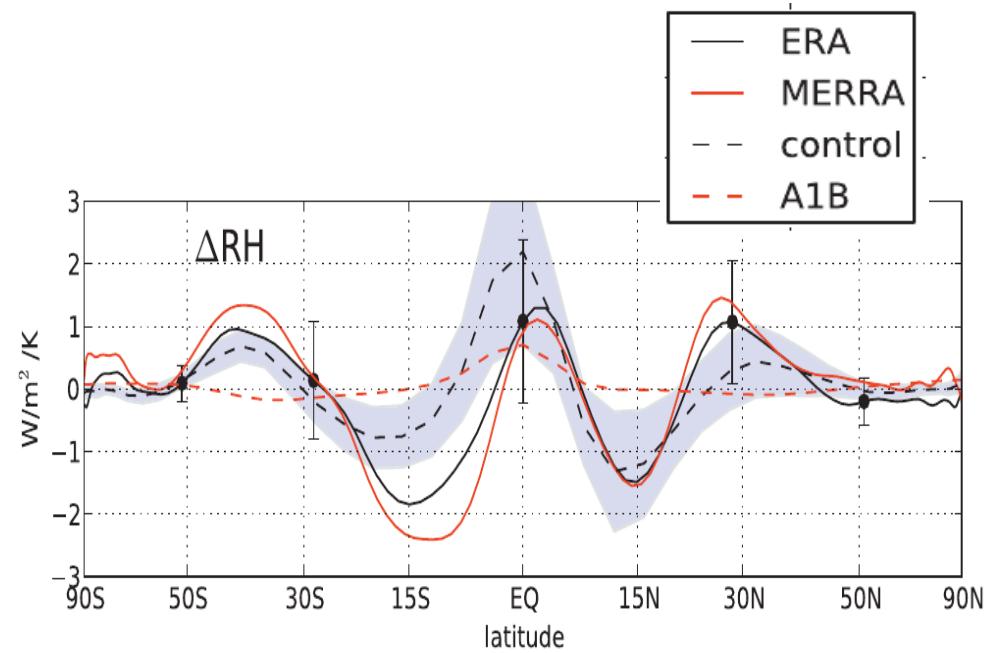
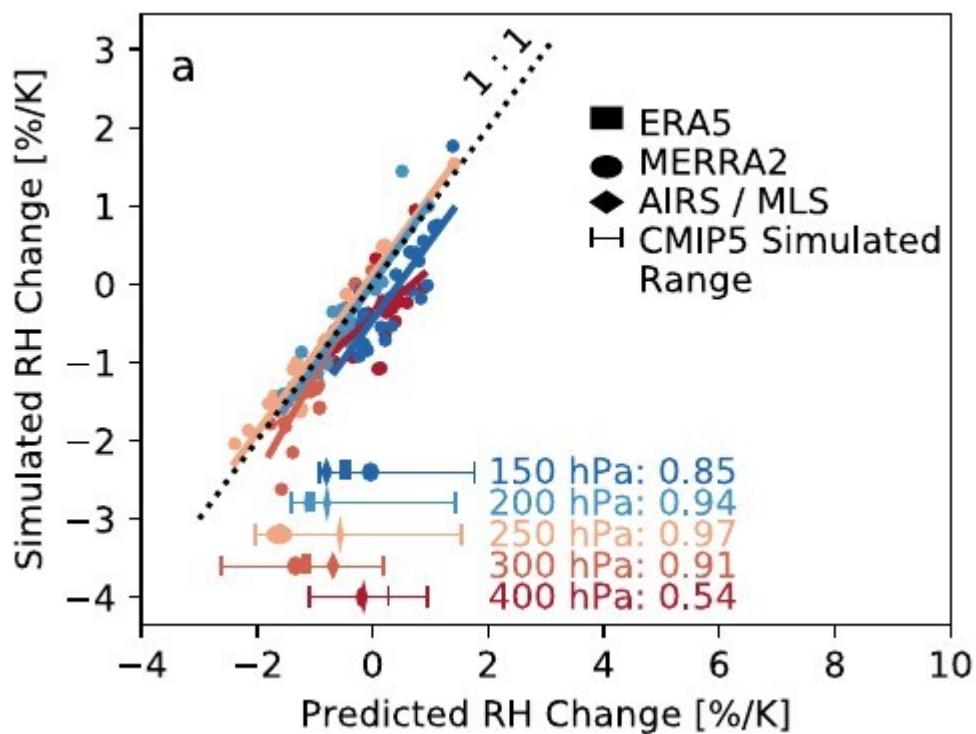
[courtesy of M. Zelinka 2021]

(<https://doi.org/10.5281/zenodo.5206851>)



# Water vapour feedback

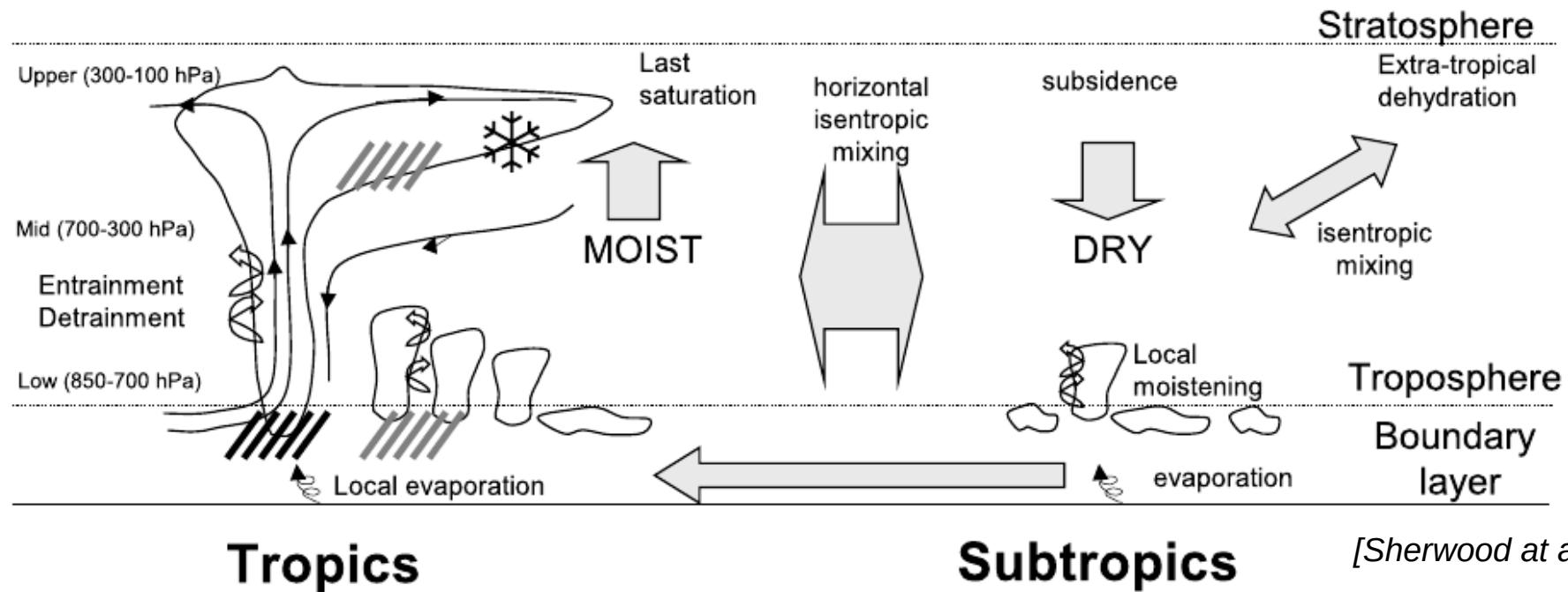
Little change of the relative humidity with temperature at inter-annual time scale



[Dessler et al., 2013 ]

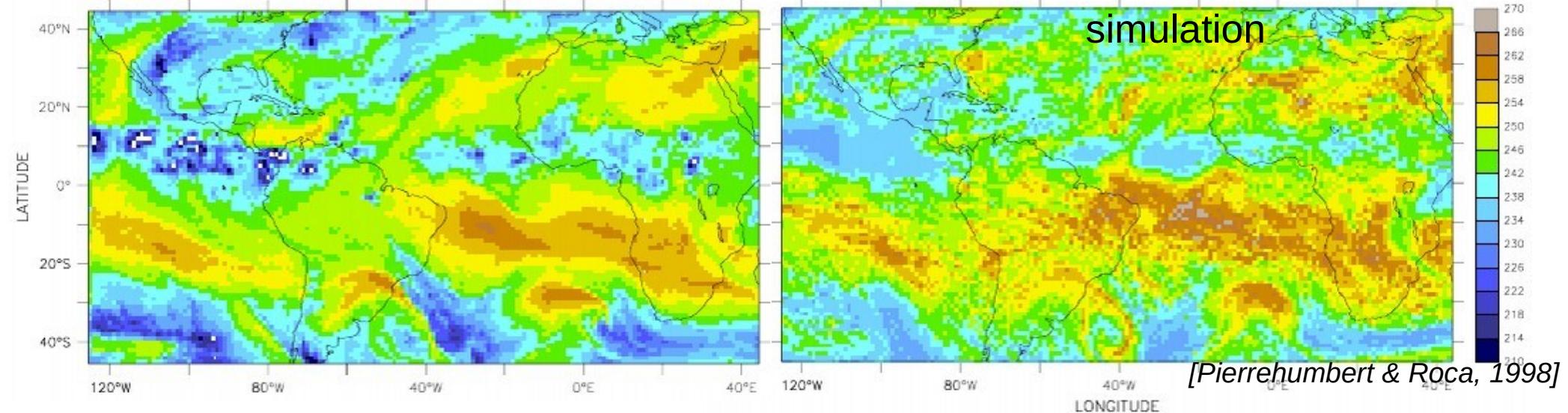
[Po-Chedley et al., GRL, 2019 ]

# Water vapour feedback : The last saturation paradigm



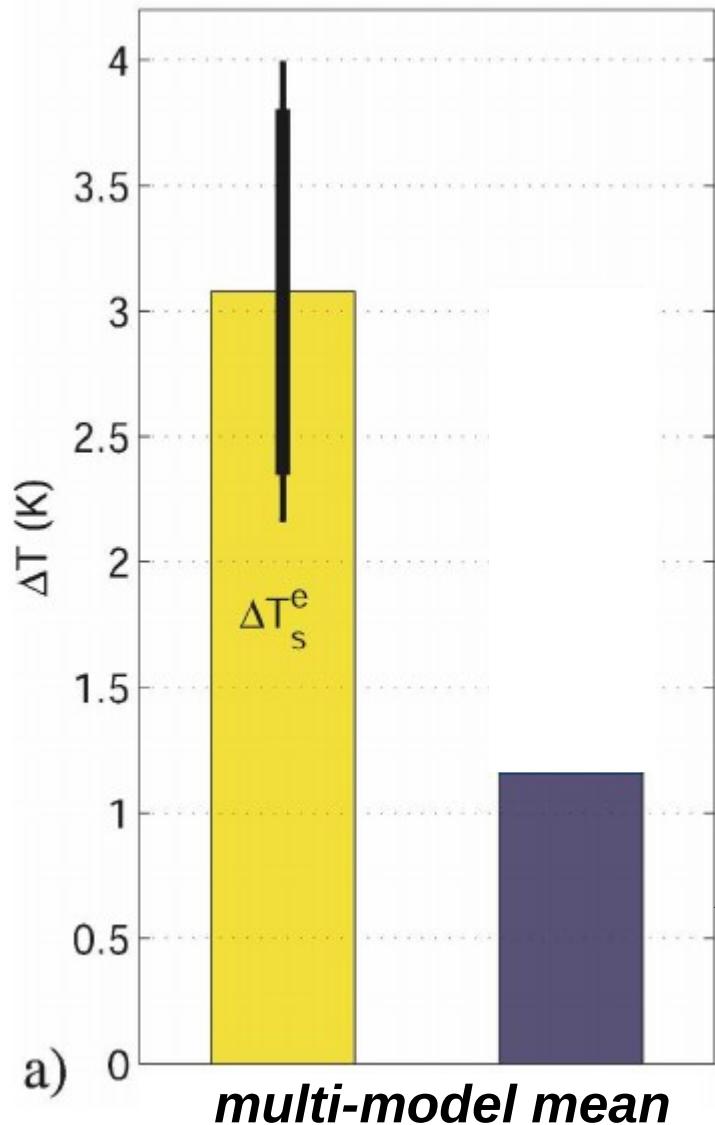
6.3  $\mu\text{m}$  brightness temperature (~ relative humidity)  
Observed (Meteosat)

reconstructed from the advective simulation



# How much individual feedbacks contribute to global warming

Equilibrium temperature response to a CO<sub>2</sub> doubling

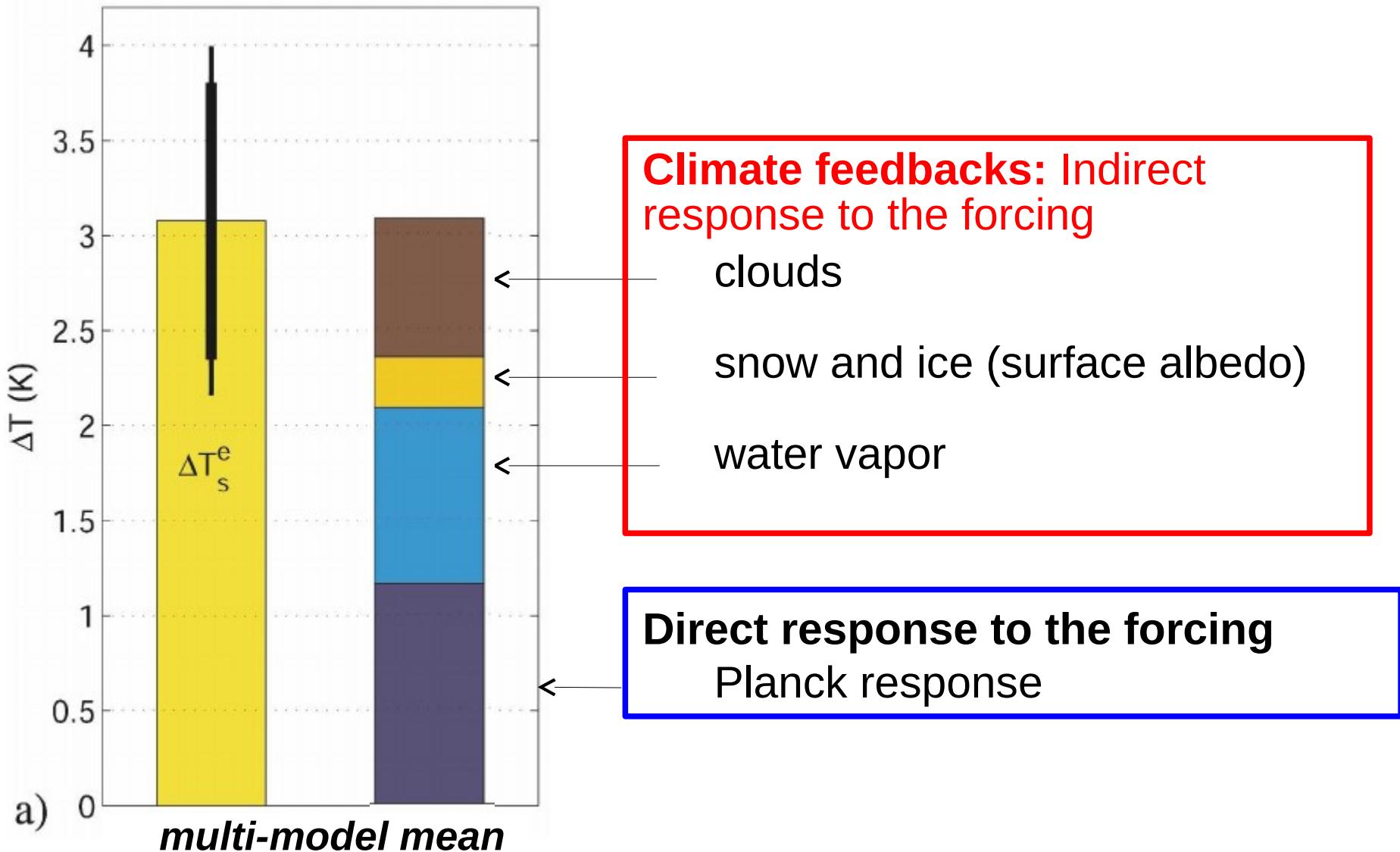


Direct response to the forcing  
Planck response

(Dufresne & Bony, 2008)

# How much individual feedbacks contribute to global warming

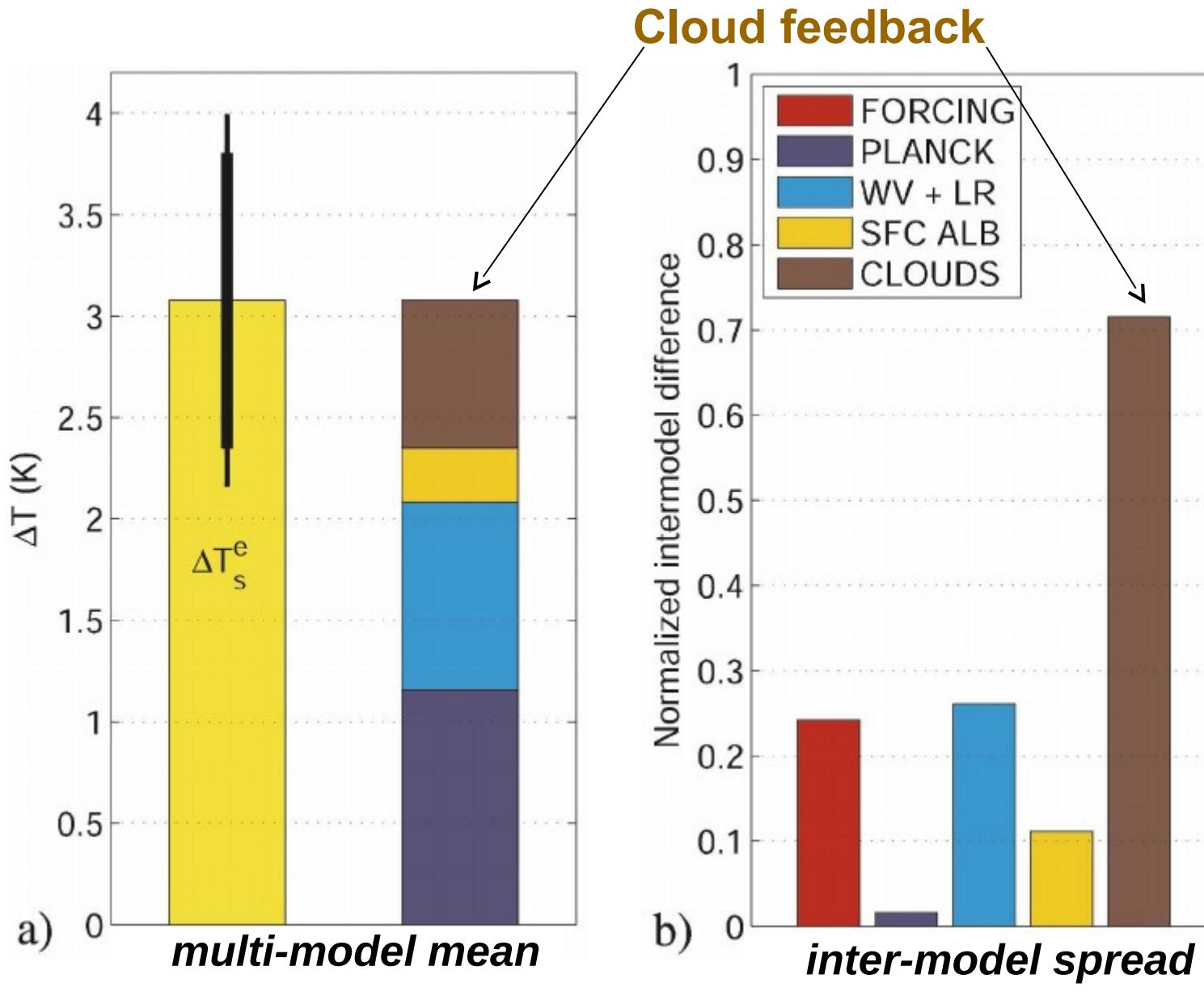
Equilibrium temperature response to a CO<sub>2</sub> doubling



(Dufresne & Bony, 2008)

# How much individual feedbacks contribute to global warming

## Equilibrium temperature response to a CO<sub>2</sub> doubling



# How to compute feedbacks ?

Diagnostic of feedback parameters through the Kernel approach

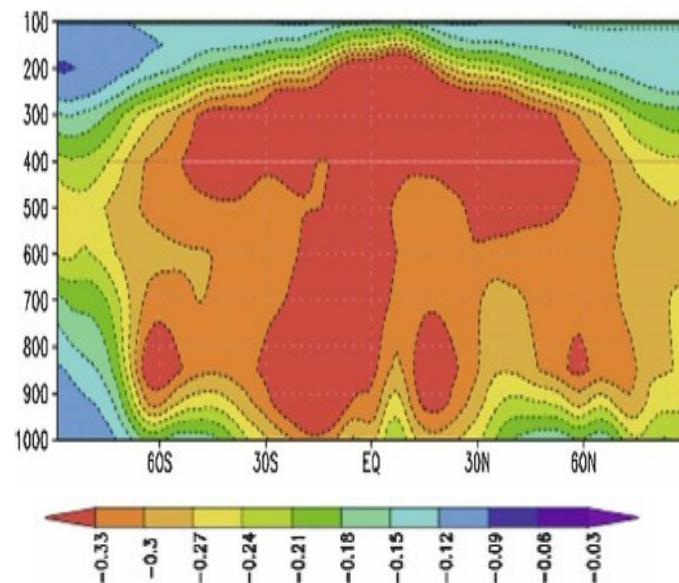
$$\lambda = \frac{dN}{dT_s} = \sum_x \frac{\partial N}{\partial x} \frac{\partial x}{\partial T_s}$$

radiative kernel computed by  
radiative codes

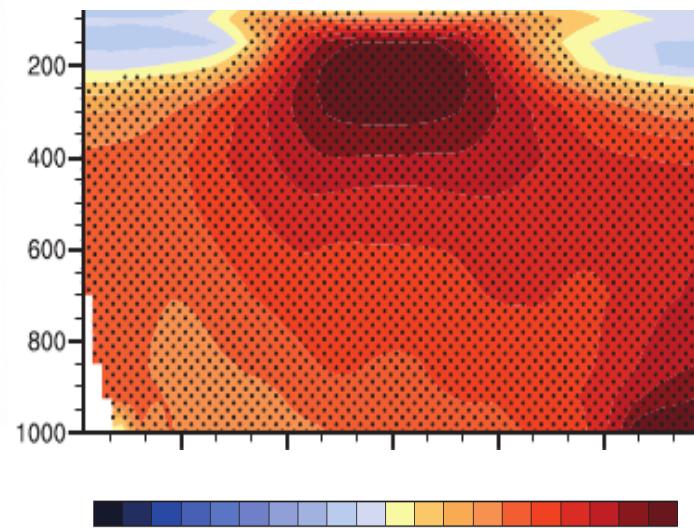
response to surface  
temperature change

e.g. for  $x = T$  :

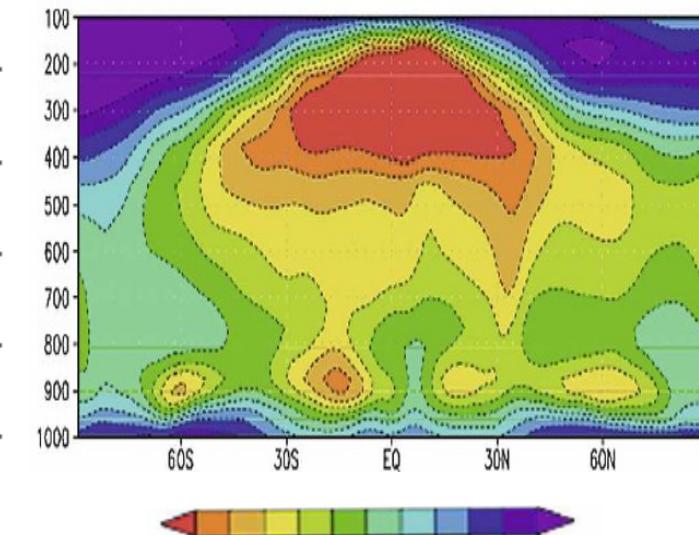
Temperature kernel  $\frac{\partial N}{\partial T}$



Temperature change  $\frac{\partial T}{\partial T_s}$



Temperature feedback parameter  $\lambda_T = \frac{\partial N}{\partial T} \frac{\partial T}{\partial T_s}$



$\text{W/m}^2/\text{K}/(100\text{hPa})$

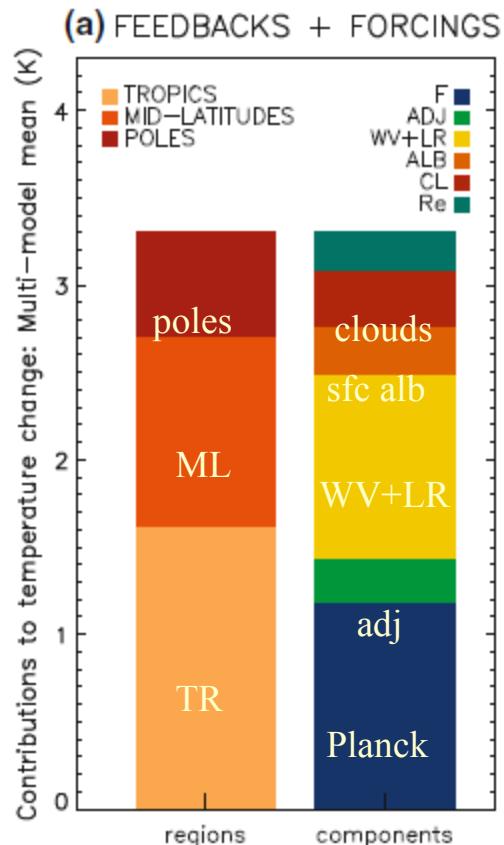
$0 \quad 1 \quad 2$   
 $\text{K/K (approximate)}$

$-0.55 \quad -0.5 \quad -0.45 \quad -0.4 \quad -0.35 \quad -0.3 \quad -0.25 \quad -0.2 \quad -0.15 \quad -0.1 \quad -0.05$   
 $\text{W/m}^2/\text{K}/(100\text{hPa})$

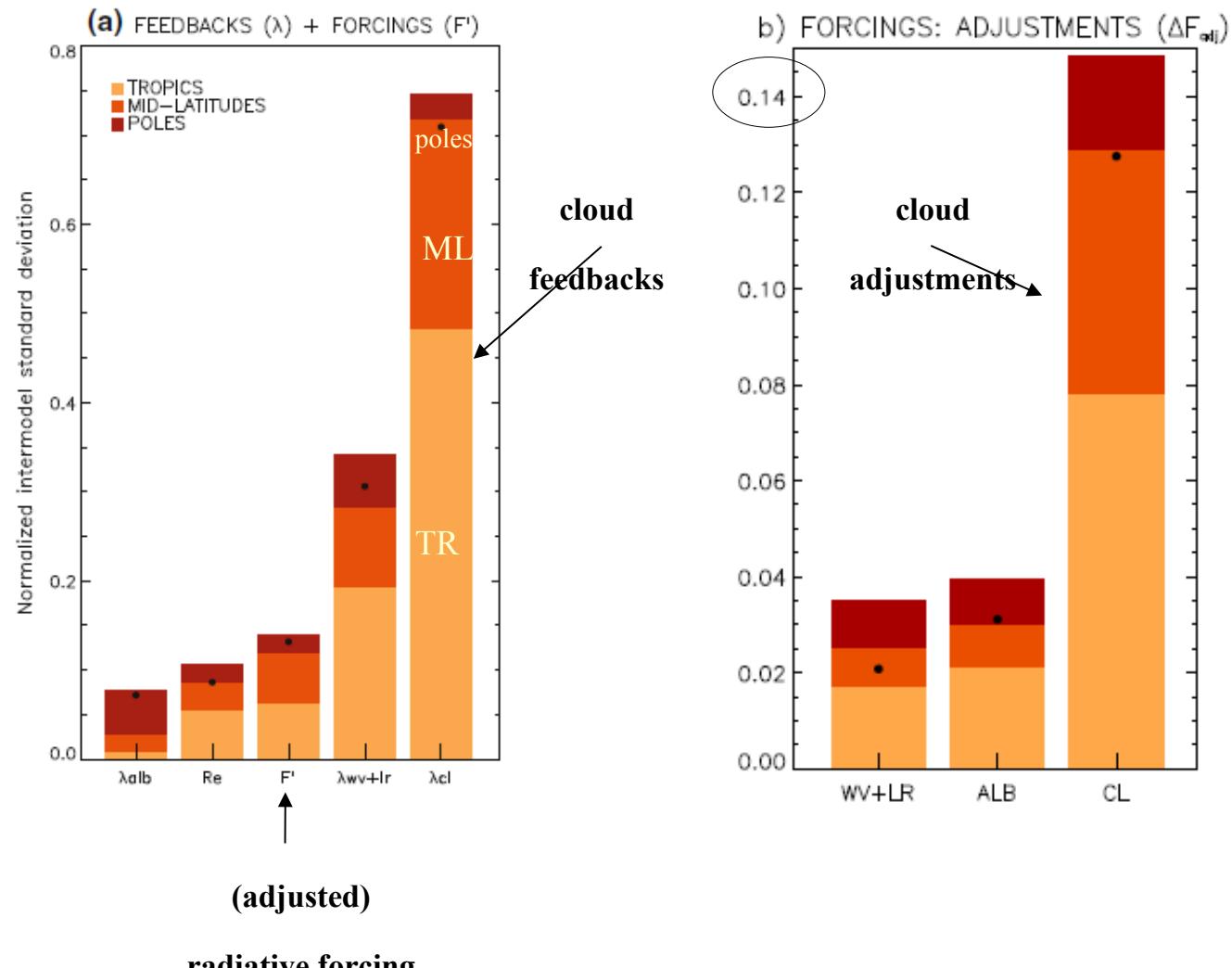
Soden et al., J. Climate, 2008

# Decomposition of CMIP5 climate sensitivity estimates

Multi-Model Mean



Inter-Model Spread



Cloud feedbacks still constitute a leading source of uncertainty.

# Revised Framework

let's assume that  $R = R(\varphi, T_s, X)$        $X = X(\varphi, T_s)$

$$\Delta R = \left[ \left( \frac{\partial R}{\partial \varphi} \right)_{T_s, X} + \left( \frac{\partial R}{\partial X} \right)_{\varphi, T_s} \frac{\partial X}{\partial \varphi} \right] \Delta \varphi + \left[ \left( \frac{\partial R}{\partial T_s} \right)_{\varphi, X} + \left( \frac{\partial R}{\partial X} \right)_{\varphi, T_s} \frac{\partial X}{\partial T_s} \right] \Delta T_s$$

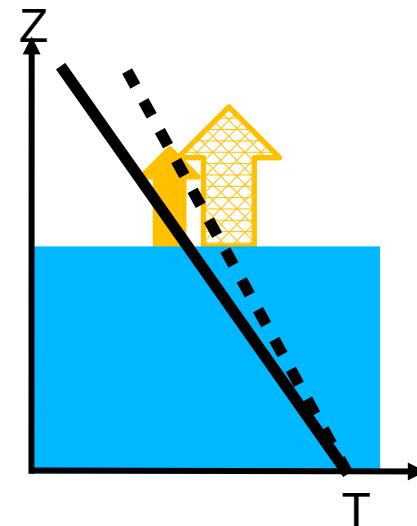
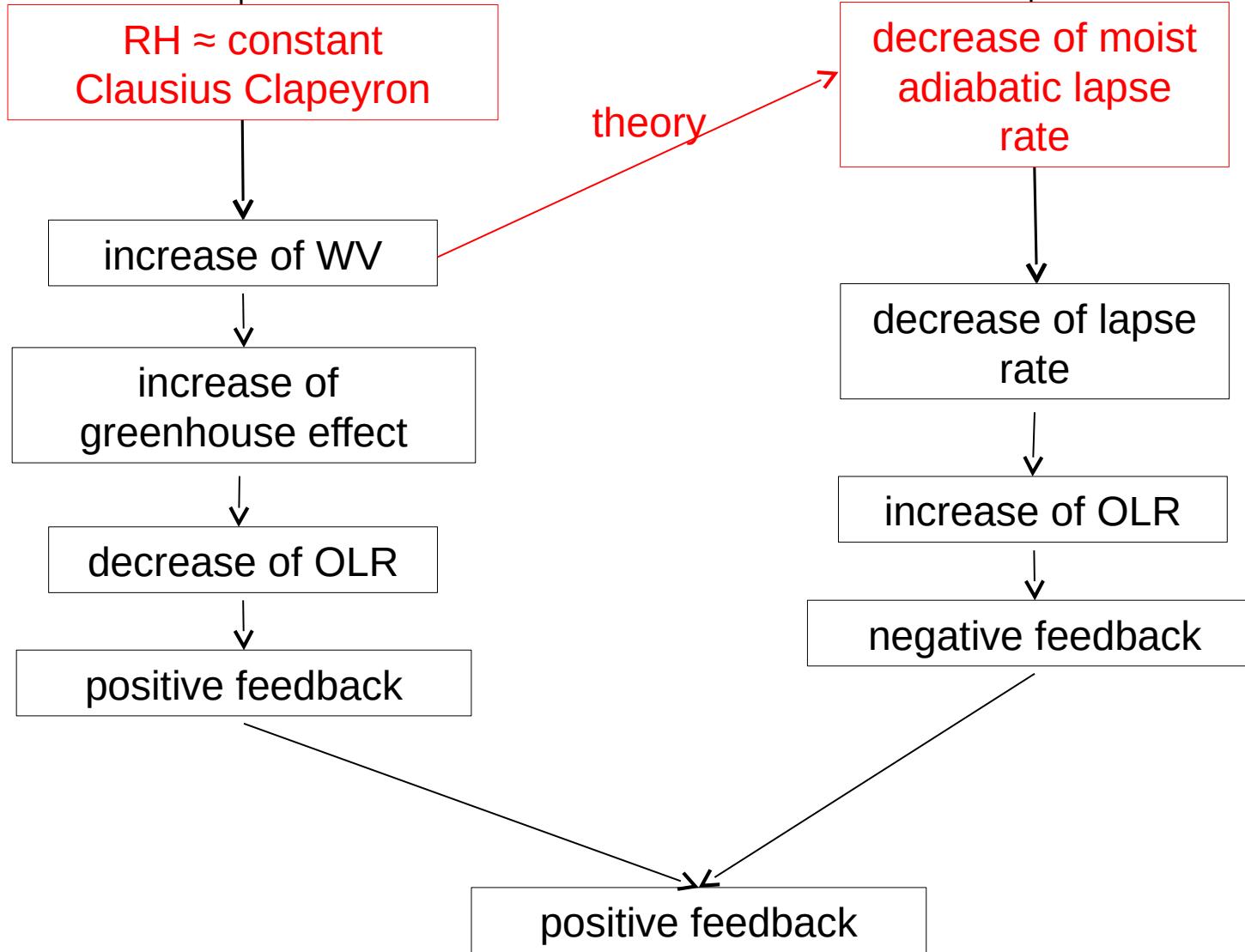
*instantaneous radiative change*    +    *adjustments to  $\varphi$*

*Planck response*    +    *radiative feedbacks*

*radiative forcing*  
*(named « effective radiative forcing » in AR5 )*

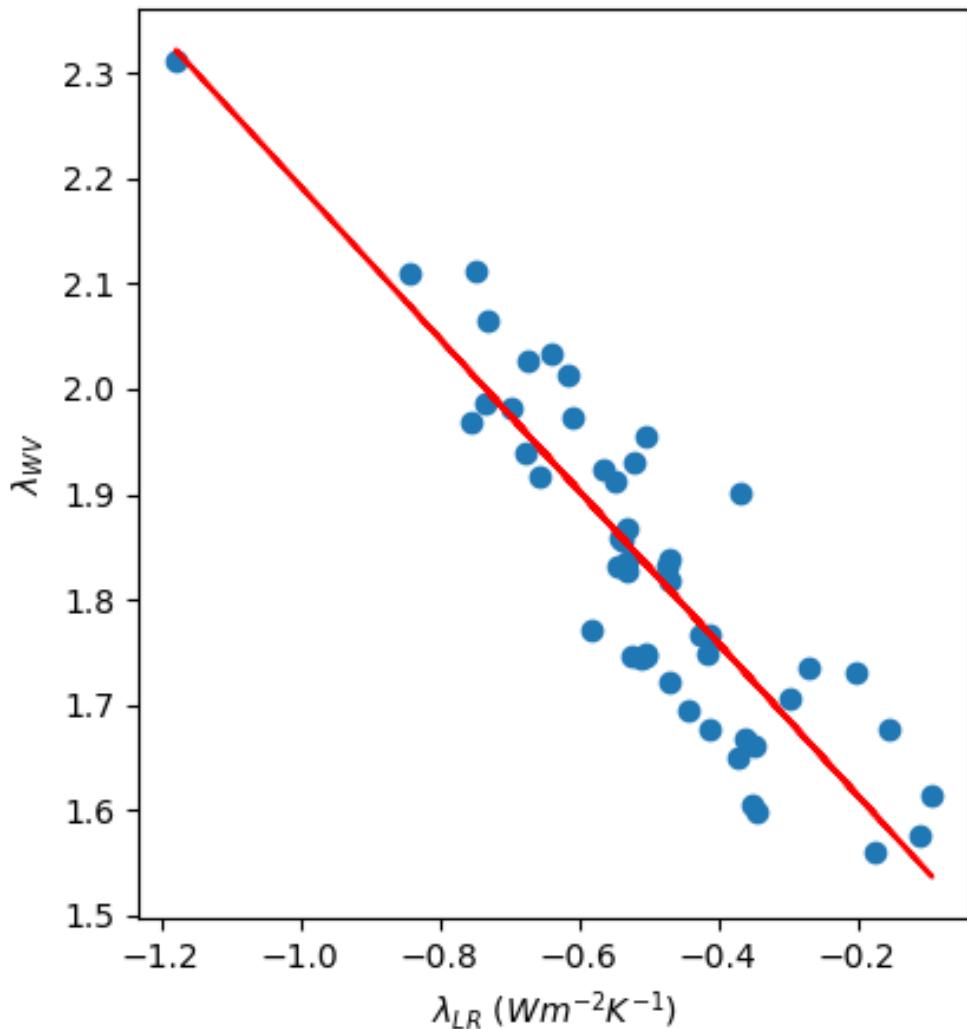
*climate response*

## Water vapor + lapse rate feedbacks

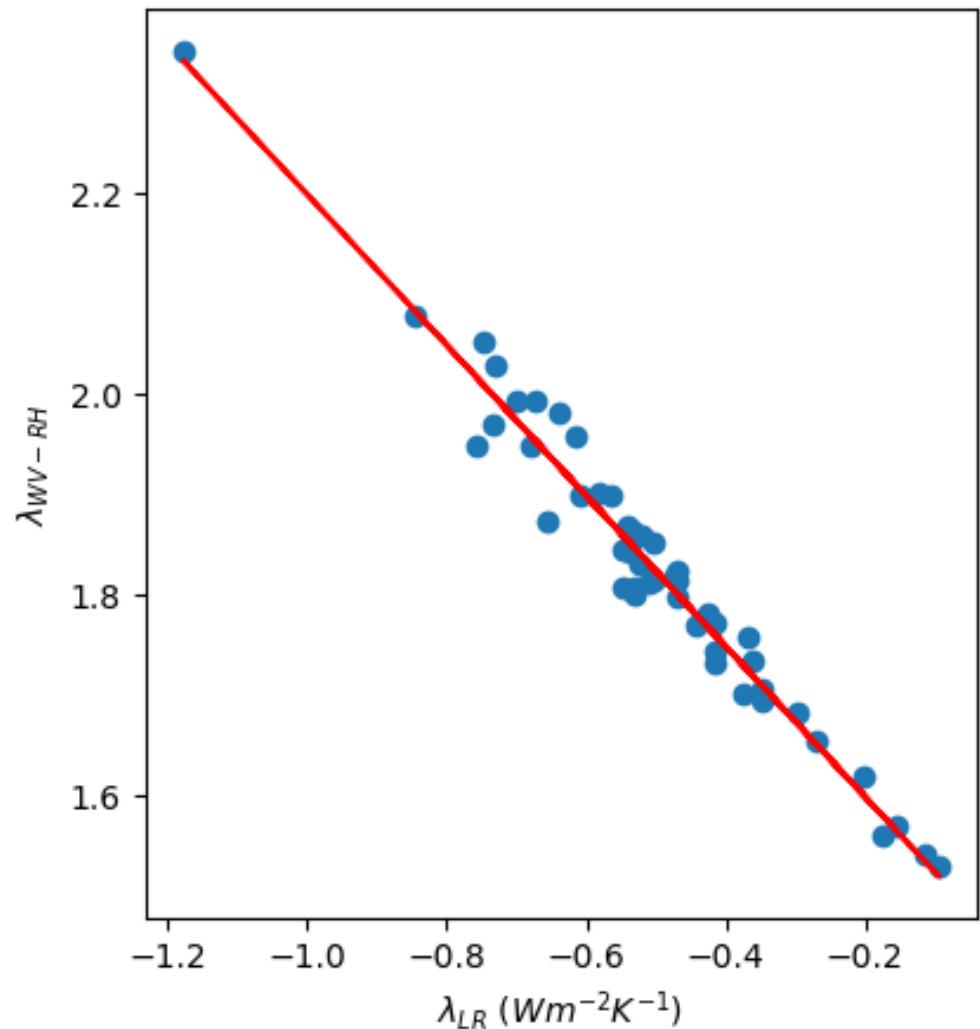


## Feedback parameters for CMIP6 models

**water-vapor vs  
temperature lapse rate feedbacks**



**water-vapor with no RH change vs  
temperature lapse rate feedbacks**



# Climate total feedback

